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Electron Penetration Range for Diverse Materials

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The penetration range of energetic electrons into diverse materials can be modeled approximately with a simple fit. This fit is a function of a single parameter, N_v, which describes the effective number of valence electrons. Using the Continuous-**Slow-Down-Approximation (CSDA) for energy deposition in a material, a composite analytical formula has been developed** which estimates the range or maximum penetration depth of incident electrons for energies from <10 eV to >10 MeV with an uncertainty of <20%. The fit also incorporates several common properties compiled for each material, including the mean atomic number, mean atomic weight, density, and band gap or Plasmon energy. The model has been fit to existing data for 247 materials collected from the ESTAR and IMFP databases compiled by NIST to determine N, values. Comparison of N_v with the material's properties from this large material database may lead to the prediction of N_v for **materials which have no supporting data.**

The range of a material describes the maximum distance electrons can travel through said material, given an initial incident energy, before losing the entirety of its kinetic energy. The penetration depth is the resulting depth at which the electrons have come to rest. 1,2 Two factors affect this range of any given material -- firstly, energy loss through inelastic interactions and collisions, and secondly, the loss of electron energy through elastic interactions or backscattering of electron emissions. 3

parameterizations as illustrated in Figure 6.

Weight (c) Effective Atomic Weight (d) Mean Excitation Energy

To further validate the range formulations and to lead to possible new discoveries in range penetration, the Material Physics Group's material database needed to be expanded. A spreadsheet had previously been compiled with information on a number of materials. The spreadsheet's minor errors were corrected and both the total number of materials in the database and parameters for each material were extended. (e.g. considerations such as phase, color, and conductivity were added). The greater number of materials allowed for a more exact fit to be discovered with the CDSA. Adding more parameters offered the opportunity of discovering possible trends that might enable a discovery of an even more exact function to describe the range. Table 1 offers a small selection of the compiled materials, along with some of the materials' applicable physical properties.

Materials **Nv Chromlum Gadolinium 12.0**
PI (Kapton) 3.6 Oxide Nickle 7.0 15.0 Radlum

Expansion of Materials Database

Future Work

Future work by the USU Materials Physics Group includes: • **Study fits based on the extended parameters of the material database.** • **Develop a user friendly application to calculate the range verses incident energy for all materials in the database and for other arbitrary materials.** • **Develop a general formula to predict values for** *N^v* **and the range for arbitrary materials, based on readily available materials properties.** • **Compile findings onto a user friendly website.**

References

Allowable Margin of Error

Fig. 1. Front (Left) and side (Right) views of a Lichtenberg discharge tree. The white line (Right) indicates the narrow distribution of deposited charge from a ~1 MeV electron beam at R≈3 mm in a PMMA sample.

In order to perform range calculations, a value for the electron bandgap was needed for each material. While some material bandgaps were easier to find than others, it was necessary for a comparison to be made to see how much the fitting factor would change with a varying bandgap value. These calculations gave desirable results, showing that the fitting factor varied minimally with changing bandgaps. For an example, see Table 2, which uses alumina (Al2O³) as our chosen material. It was also realized that the error between the values in our calculations and the NIST provided values increased as the bandgap's value increased in distance from the true value.

1. Wilson, G., & Dennison, J.R. (2010). *Approximation of range in materials as a function of incident electron energy.* **2. Teancum Quist (with Greg Wilson and JR Dennison), "Compilation and Comparison of Electron Penetration Ranges as a Function of Effective Number of Valence Electrons," Utah State University, Logan, UT, April 2013. 3. Starley, A., Phillipps, L., Dennison, J.R., "Electron Range Penetration for Various Materials" U.R.C.O Proposal, Utah State University, Logan, UT, 2015.**

4. J. Sempau, S.J. Wilderman, and A.F. Bielajew, 2000, "DPM, a fast, accurate Monte Carlo code optimizedfor photon and electron radiotherapy treatment planning dose calculations," Physics in Medicine and Biology 45, 8

This idea is illustrated by a Lichtenburg discharged tree pictured in Figure 1. This "tree" is an example of a situation where an accelerated high voltage comes to rest and deposits electrons at a given range in an insulating material. 3 The side view of the Lichtenburg figure displays the melted plastic caused by the energy of the deposited incident electrons at a uniform penetration depth. Here the stored charge is dissipated through a discharge. 1

Original Model

A model previously developed by the Material Physics Group predicts the range 3, and 4) have been found¹ to describe the energy-dependent range, R(E)_T. as a function of **incident electron energy for known materials. In a continuous composite analytic approximation to the range with a single fitting parameter spanning incident energies, E, from <10 eV to > 10 MeV, the following functions (Figure 2, 3, and 4) have been found¹ to describe the energy-dependent range, R(E).**

Fig. 2. Range formula for low energy, medium energy and high energy.

$$
E_m = 2.8 \left[E_{gap}^2 + E_p^2 \right]^{\frac{1}{2}}
$$

Fig. 3. Formula for geometric mean energy lost per collision.

$$
E_p = \hbar \left(\frac{NVMA\rho_m q_e^2}{m_e \varepsilon_0 M_A}\right)^{\frac{1}{2}}
$$

Fig. 4. Formula for plasmon energy.

Fits to these initial equations and optimum values of *N^v* **were found only using data for only a handful of wellknown elements and compounds and were able to predict known** *N^v* **. Figure 5 demonstrates some of the fitting parameters that can be applied using known data selected from ESTAR database.**

² Figure 5. Comparison between several range approximations and the data from the ESTAR database for Au. The IMFP data for Au are also plotted along with the TPP-2M IMFP formula for λIMFP(E).

Table 1. Representative materials and specific material properties.

at room temperature.

In order to put the fitting factor variances into perspective, Figure 8 shows what alumina's fit would look like if we had used a fitting factor of 0.10, 4.05 (the calculated value), and 8.00. Even with significant variance in the fitting factor, we can expect to find values that are reasonably accurate for most applications.

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Table 2. Alumina's variation in a fitting factor as the bandgap fluctuates.

and 8.00), and the fits compared.

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