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P. W. Lommen

D. C. Wilkin

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1975/76 PROGRESS REPORT

**PROGRAMMING PHASE OF
WATER RESPONSE ECOSYSTEM MODEL:
II. ABIOTIC SUBMODELS**

P. W. Lommen* and K. A. Marshall
Utah State University

(*now at HDR Ecosciences, Santa Barbara, California)

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Ecology Center, Utah State University, Logan, Utah 84322

This report describes a portion of the Desert Biome Water Response Ecosystem Model. Five Research Memoranda comprise the full description: Introduction and support programs (RM 76-36); Abiotic submodels (RM 76-37); Animal submodel (RM 76-38); Perennial plant, nitrogen and decomposition submodels (RM 76-39); and Annual plant submodel (RM 76-40). The objectives of the Water Response Model, information on the arrangement of material distributed among the five Research Memoranda and descriptions of program MAIN and support programs F1, F3 and FTAVE are contained in Research Memorandum 76-36, **Programming phase of water response ecosystem model: I. Introduction and support programs.** The relationships between various sections of the model, their interactions and location in the report series are summarized in Table 1 of RM 76-36.

INTRODUCTION

This research memorandum describes submodels PSWG, HEAT and WATER (and their support programs) of the Desert Biome Water Response Model. These submodels provide environmental (or driving) variables to the plant, animal and soil-microbe submodels. PSWG (for Pseudo Stochastic Weather Generator) provides meteorological variables (air temperature, precipitation, plus several

others). HEAT calculates soil temperature profile, given soil heat flow characteristics and air temperature. WATER determines soil water potential profile given initial conditions, soil moisture flow characteristics and several water inputs and outputs (precipitation, evaporation, transpiration, runoff-runoff). Transpiration, through its effect on soil water potential, is the only biological effect on any of the ten or so environmental variables determined in these submodels.

A. PSWG
 (including support programs EVAP, RINT,
 IPROB, RNOR)
 K. A. Marshall and P. W. Lommen

GENERAL DESCRIPTION OF PSWG SUBMODEL

PSWG is a submodel which generates driving variables for the Water Response Model. (The name PSWG is generated from Pseudo Stochastic Weather Generator).

These variables are maximum, minimum and mean time-step air temperature at 2 m; precipitation and its intensity for the time-step; potential evaporation for the time-step; and mean values for the time-step of relative humidity, wind speed, fraction of possible sunlight and photoperiod.

For any run, one of two versions is used depending on data availability. Version I is used for debugging, tuning and validation runs. For debugging runs, all driving variables are stochastically generated. For tuning and

validation runs where driving variables must correspond to the weather of a given year or years, daily temperature and precipitation records for the site are used. The remaining driving variables are chosen stochastically because daily records for the site are either not available at all or are not complete enough. Variables are stochastically chosen with the aid of random numbers and parameters generated from six years' data of the variable in question obtained from the United States Weather Bureau at the nearest complete weather station to our site. For Curlew Valley simulation, data from Pocatello, Idaho, were used. For Rock Valley simulations, Las Vegas, Nevada, data were used. Refer to Table A-1 for definitions of variables for both versions of PSWG. Definitions will also be found in the complete program listings at the end of this section.

Version II of PSWG is used for five-year (or longer) simulations. It generates nothing stochastically. Instead, it reads temperature, precipitation, wind speed, fraction of possible sunlight and relative humidity data from a weather data file. (For five-year Curlew Valley runs, data were used from the U.S. Weather Bureau station at Pocatello.)

Table A-1. Variable dictionary for PSWG, Versions I and II

AMT(6)	AMT(I) IS AMOUNT OF PRECIPITATION IN MM IN EVENT CLASS I.
DECL	ANGLE CALCULATED IN PHOTOPERIOD CALCULATION.
EVAP	SUBROUTINE WHICH CALCULATES POTENTIAL EVAPORATION.
FACTOR	PRECIPITATION FACTOR BY WHICH EACH EVENT IS MULTIPLIED.
HUM(10,13)	INTEGRATED PROBABILITY DISTRIBUTION OF RELATIVE HUMIDITY CLASS BY PERIOD OF YEAR.
IPROB	FUNCTION WHICH DETERMINES DEPENDENT VARIABLE GIVEN INTEGRATED PROBABILITY DISTRIBUTION, BY RANDOMLY CHOOSING INDEPENDENT VARIABLE IN RANGE 0-1.
ISEED	SEED FROM WHICH RNOR GENERATES NEXT RANDOM NUMBER.
IYEST	EQUALS 1 IF THERE WAS NO PRECIPITATION YESTERDAY. IF EQUALS 2 THEN THERE WAS PRECIPITATION YESTERDAY AND PROBABILITY OF PRECIPITATION TODAY IS INCREASED.
J	CLASS INDEX, USED IN PRECIP, WIND, SUN, HUM GENERATION.
JDAY	JULIAN DATE AT BEGINNING OF TIMESTEP.
LAT	LATITUDE OF SITE.
MDAY	CURRENT JULIAN DAY (INCREMENTED IN PSWG FROM JDAY TO JDAY+PMDT).
HTIME	INDEX OF 4 WEEK PERIOD OF YEAR IN WHICH MDAY FALLS.
NNN	COUNTER TO DETERMINE WHEN TO START PRINTING ON NEXT PAGE.
PMDT	TIMESTEP LENGTH, DAYS.
PREC(6,13)	INTEGRATED PROBABILITY DISTRIBUTION OF PRECIPITATION CLASS BY PERIOD OF YEAR.
PRECIP	PRECIPITATION FOR CURRENT DAY, MM.
PMJDAT	JULIAN DATE AT BEGINNING OF TIMESTEP. VALUE DETERMINED IN MAIN PROGRAM.
PWFAC	FACTOR FOR ADJUSTING AVERAGE WIND SPEED IF SITE IS KNOWN TO HAVE DIFFERENT AVERAGE WIND SPEED.
RAIN(2,13)	ARRAY HOLDING VALUES OF (1, = PROBABILITY OF PRECIP, TODAY) GIVEN PERIOD OF YEAR AND WHETHER OR NOT WE HAD PRECIP, YESTERDAY.

Table A-1, continued

RCHECK(20)	VARIABLE USED TO READ AND WRITE COMMENTS IN WITH INITIAL DATA.
READ	IF =.TRUE., THEN READ TEMPERATURE PRECIPITATION DATA FROM SEPARATE DATA FILE.
RINT	SUBROUTINE WHICH CALCULATES PRECIPITATION INTENSITY.
RNOR	RANDOM NORMAL NUMBER GENERATOR (68% OF VALUES LIE BETWEEN -1 AND +1).
SHUM	RUNNING SUM OF UP TO PMDT DAYS' RELATIVE HUMIDITY.
SMAX	RUNNING SUM OF UP TO PMDT DAYS' MAXIMUM TEMPERATURES, DEGREES CELCIUS.
SMIN	RUNNING SUM OF UP TO PMDT DAYS' MINIMUM TEMPERATURES, DEGREES CELCIUS.
SPREC	RUNNING SUM OF UP TO PMDT DAYS' PRECIPITATIONEVENTS, MM.
SSUN	RUNNING SUM OF UP TO PMDT DAYS' PER CENT POSSIBLE SUNLIGHT
SUN(10,13)	INTEGRATED PROBABILITY DISTRIBUTION OF PER CENT POSSIBLE SUNLIGHT CLASS BY PERIOD OF YEAR,
SWIND	RUNNING SUM OF UP TO PMDT DAYS' AVERAGE WIND SPEEDS, KM/HR.
TMAX	MAXIMUM TEMPERATURE FOR CURRENT DAY, DEGREES CELCIUS.
TMIN	MINIMUM TEMPERATURE FOR CURRENT DAY, DEGREES CELCIUS.
TRAIN(20)	ARRAY WHICH HOLDS DAILY PRECIP VALUES FOR TIMESTEP (USED BY RAIN INTENSITY ROUTINE).
WIND(7,13)	INTEGRATED PROBABILITY DISTRIBUTION OF WIND SPEED CLASS BY PERIOD OF YEAR,
XMAX(1),XMAX(2)	PARAMETERS FOR SINE WAVE FIT TO SEVERAL YEARS' DAILY MAXIMUM TEMPERATURES, TAKEN AT NEAREST WEATHER BUREAU SITE.
XMAX(3)	STANDARD DEVIATION OF DATA ABOUT SINE WAVE FIT USING XMAX(1) AND XMAX(2).
XMIN(1),XMIN(2)	PARAMETERS FOR LINEAR REGRESSION BETWEEN TMAX AND TMIN.
XMIN(3)	STANDARD DEVIATION OF TMIN.
ZAIRT	AVERAGE DAILY AIR TEMPERATURE FOR TIMESTEP, DEGREES CELCIUS, DRIVING VARIABLE USED BY OTHER SUBMODELS.
ZEVAP	SUM FROM OCTOBER 1 OF ZEVAP, MM.
ZEVAP	POTENTIAL EVAPORATION, MM/TIMESTEP, DRIVING VARIABLE USED BY OTHER SUBMODELS.
ZPHPD	PHOTOPERIOD OF FIRST DAY IN TIMESTEP, HOURS, DRIVING VARIABLE USED BY OTHER SUBMODELS.
ZRAIN	TOTAL PRECIPITATION FOR TIMESTEP, MM, DRIVING VARIABLE USED BY OTHER SUBMODELS.
ZRH	AVERAGE DAILY RELATIVE HUMIDITY, DECIMAL FRACTION FROM 0-1, DRIVING VARIABLE USED BY OTHER SUBMODELS.
ZRINT	PRECIPITATION INTENSITY, MM/HR, DRIVING VARIABLE USED BY OTHER SUBMODELS.
ZRSUM	SUM FROM OCTOBER 1 OF ZRAIN, MM.
ZSUN	AVERAGE DAILY PER CENT POSSIBLE SUNLIGHT FOR TIMESTEP, DECIMAL FRACTION FROM 0-1, DRIVING VARIABLE USED BY OTHER SUBMODELS.
ZTHMAX	AVERAGE DAILY MAXIMUM TEMPERATURE FOR TIMESTEP, DEGREES CELCIUS, DRIVING VARIABLE USED BY OTHER SUBMODELS.
ZTHIN	AVERAGE DAILY MINIMUM TEMPERATURE FOR TIMESTEP, DEGREES CELCIUS, DRIVING VARIABLE USED BY OTHER SUBMODELS.
ZWIND	AVERAGE DAILY WIND SPEED FOR TIMESTEP, DRIVING VARIABLE USED BY OTHER SUBMODELS.

PROGRAM DESCRIPTION

PSWG, VERSION I

Only the important segments of the FORTRAN code are shown and described. Sequence numbers are shown to aid in reference to the full code listing which follows the Program Description. All comment cards, specification statements and bookkeeping sections have also been deleted. Definitions of variable names may be found in Table A-1, which also appears at the beginning of the program listing.

```
DO 3 I=1,PMDT
```

PSWG 183

Beginning of main loop in program. Go through loop once for each day of time-step in order to get daily weather information for appropriate average or summed value.

```
MTIME=MDAY/28+1
IF (MTIME .GT. 13) MTIME=13
```

PSWG 184
 PSGI 185

Determine MTIME, index of four-week period of year in which MDAY, current Julian day, falls.

```
IF(,NOT,READ)GOTO100
020 READ(6,25,END=500)TMAX,TMIN,PRECIP
025 FORMAT(7X,2F6.1,36X,F6.1)
      GOT030
```

PSWG 189
 PSGI 190
 PSGI 191
 PSGI 192

If flag is set (i.e., if READ is .TRUE.) then read temperature and precipitation data from separate weather file. Then check if data are reasonable.

```
500 READ=,FALSE,
      GOT0100
```

PSWG 194
 PSGI 197

If control reaches here then all data have been read and remainder of temperatures and precipitation amounts will be generated stochastically.

```
IF(TMAX.LT.TMIN)GOTO40
IF((TMAX,LT,-30.),OR,(TMAX,GT,45.))GOTO40
IF((TMIN,LT,-30.),OR,(TMIN,GT,45.))GOTO40
IF(((PRECIP,LT,50.),AND,(PRECIP,GE,0.0)),OR,(PRECIP,GT,5000.,))
*      GOT060
```

PSWG 202
 PSGI 203
 PSGI 204
 PSGI 205
 PSGI 206

Check data just read and see if they are reasonable.

```
040 WRITE(6,50)PMJDAT,TMAX,TMIN,PRECIP
050 FORMAT(' ',I5,3F12.5)
      STOP
```

PSWG 210
 PSGI 211
 PSGI 212

We reach here only if a datum was judged unreasonable. Write offending card and stop execution.

```
060 CONTINUE
$MAX=$MAX+TMAX
$MIN=$MIN+THIN
$PREC=$PREC+PRECIP
TRAIN(I)=PRECIP
GOTO 2
```

```
PSG1 215
PSG1 216
PSG1 217
PSG1 218
PSG1 220
PSG1 221
```

Keep running sums over PMDT of temperature and precipitation information. Also load appropriate place in TRAIN array for rain intensity calculation. Go on to wind speed section.

```
100 CONTINUE
TMAX = XMAX(1) + XMAX(2)*SIN(.017214*MOD((PMJDAT+344,),365,))
C = 1.570796)
001 TMAX = TMAX + XMAX(3)*RNDR(ISEED)
TMIN=XMIN(1)+XMIN(2)*TMAX
TMIN=TMIN+XMIN(3)*RNDR(ISEED)
IF (TMIN .GT. TMAX) GO TO 1
$MAX=$MAX+TMAX
$MIN=$MIN+TMIN
```

```
PSG1 225
PSG1 234
PSG1 235
PSG1 237
PSG1 238
PSG1 239
PSG1 240
PSG1 241
PSG1 242
```

Control reaches here if we wish to stochastically generate the current day's temperatures. First, calculate the mean maximum temperature for the day. Next, generate the day's minimum temperature from the maximum. Next, make sure the minimum is less than or equal to the maximum. Finally, add these temperatures to the sums of temperatures for previous days of the time-step.

```
IYEST=IPROB(RAIN(IYEST,MTIME),1)
IF(IYEST .NE. 2) TRAIN(I)=0.0
IF (IYEST .NE. 2) GO TO 2
J=IPROB(PREC(1,MTIME),5)
SPREC=$PREC+AMT(J)
TRAIN(I)=AMT(J)
```

```
PSG1 246
PSG1 247
PSG1 248
PSG1 249
PSG1 250
PSG1 251
```

Stochastically generate the day's precipitation. First determine IYEST for current day which depends on previous day's value. (If previous value was 2 rather than 1, then probability of IYEST = 2 today is considerably increased.) If IYEST = 1, then there is no precipitation today and control goes to wind speed section. If IYEST = 2, then there is precipitation today and so the amount is then determined. Calculate J, the size class of the event, an integer from 1 to 6 which depends on time of year. Once size class is determined, the amount corresponding to this class is added to SPREC, and loaded in TRAIN(I).

```
002 J=IPROB(WIND(1,MTIME),7)
SWIND=$WIND+(J-1)*8.05
```

```
PSG1 254
PSG1 255
```

Generate today's wind speed. First find J, the size class. Today's wind speed is then $(J-1) \cdot 8.05$ km/hr (8.05 km/hr = 5.00 mi/hr). Add this value to the time-step running total of wind speeds.

```
J=IPROB(SUN(1,MTIME),10)
SSUN=$SUN+(J-1)*0.1
J=IPROB(HUM(1,MTIME),10)
SHUM=$HUM+(J-1)*0.1
```

```
PSG1 258
PSG1 259
PSG1 262
PSG1 263
```

Determine fraction of possible sunlight and relative humidity similarly to wind speed. Possible values taken on will be 0, 0.1, 0.2, . . . , 1.0.

```
003 MDAY=MDAY+1
```

PSG1 264

The main loop of PSWG is ended by incrementing the Julian date.

```
X=1./PMOT
ZTMAX=SMAX*X
ZTMIN=SMIN*X
ZWIND=SWIND*X
```

PSG1 269
PSG1 270
PSG1 271
PSG1 272

Determine time-step averages for maximum and minimum air temperatures and for wind speed.

```
ZWIND = ZWIND * PWFAC
```

PSG1 276

If site is known to have different average wind speed than measuring station, multiply wind speed just determined by this factor.

```
ZSUN=SSUN*X
ZRH=SHUM*X
ZRAIN=SPREC
ZAIRT=(ZTMAX+ZTMIN)/2.
```

PSG1 279
PSG1 280
PSG1 281
PSG1 282

ZSUN, ZRH and ZAIRT are averages for the time-step. ZRAIN is the total time-step precipitation.

```
DECL=ARCSIN(SIN(6,2831853*23,45/360,)*
C COS(MOD((PMJDAT+193,),365,)*6,2831853/365,))*
X=(SIN(LAT*6,2831853/360,)*TAN(DECL)+8IN(.875*6,2831853/360,))/
C COS(LAT*6,2831853/360,)
IF (X ,GT, 1,) X=1,
IF (X ,LT, -1,) X=-1,
ZPHPD#12, + .1333333*ARCSIN(X)*360,/6,2831853
```

PSG1 285
PSG1 286
PSG1 287
PSG1 288
PSG1 289
PSG1 290
PSG1 291

Calculate ZPHPD, photoperiod, in hours, of first day of time-step.

```
CALL RINT(ZRINT, TRAIN, ZRAIN, PMOT, PMJDAT, 18EED)
CALL EVAP
```

PSG1 295
PSG1 300

Determine rain intensity and potential evaporation.

```
ZRAIN=FACTOR*ZRAIN
```

PSG1 306

Change time-step precipitation if FACTOR is not equal to 1. By changing FACTOR from one run to another, keeping all else the same, we determine the response of the entire model to changes in precipitation, a primary objective of the Water Response Model, as its name implies.

```
ENTRY ZINIT
```

PSG1 333

Entry point for initialization purposes. Called from MAIN once. Variables peculiar to PSWG are then read and written, with comment cards at the beginning, middle and end.

```
CALL EVINIT
CALL RIINIT
```

PSG1 418
PSG1 419

Call initialization sections of subroutines EVAP and RINT.

```
DO 3 I=1,PMDT
```

PSG2 120

Begin main loop. Go through loop once for each day of time-step.

```
READ(8,30,END=500)THAX,TMIN,PRECIP,WIND,PPS,RH
30 FORMAT(10X,2F5.0,F5.2,F5.1,2F5.2)
```

PSG2 122
PSG2 123

Read today's weather data.

```
THMAX=(THMAX+32.)*0.555555
TMIN=(TMIN+32.)*0.555555
PRECIP=PRECIP*25.4
WIND=WIND*1.60934
```

PSG2 133
PSG2 134
PSG2 137
PSG2 140

Convert temperature, precipitation and wind speed to metric units.

```
IF(TMIN.GT.TMAX)GOTO40
IF((TMAX.GT.42.))OR,(TMIN.LT.-43.))GOTO40
IF((PRECIP.GT.40.))OR,(PRECIP.LT.0.0))GOTO40
IF((WIND.GT.60.))OR,(WIND.LT.0.0))GOTO40
IF((PPS.GT.1.0).OR.(PPS.LT.0.0))GOTO40
IF((RH.GT.1.00).AND.(RH.GE.0.0))GOTO60
40 WRITE(6,50)TMAX,TMIN,PRECIP,WIND,PPS,RH,PMJDAT
50 FORMAT(1',7F10.3)
STOP
```

PSG2 144
PSG2 145
PSG2 146
PSG2 147
PSG2 148
PSG2 149
PSG2 152
PSG2 153
PSG2 154

Check if values just read are reasonable. If not, print offending card and stop. If reasonable, go on to summing section.

```
SMAX=SMAX+TMAX
SMIN=SMIN+TMIN
SPREC=SPREC+PRECIP
SWIND=SWIND+WIND
SSUN=SSUN+PPS
SHUM=SHUM+RH
```

PSG2 158
PSG2 159
PSG2 160
PSG2 161
PSG2 162
PSG2 163

Keep running sums of values for appropriate averages to be calculated below.

```
TRAIN(I)=PRECIP
```

PSG2 166

Load TRAIN(I) for use in rain intensity subroutine.

3 CONTINUE

PSEG2 168

End of main loop.

From here on, Version II is the same as Version I, with one exception: the entry point of Version II is much simpler than that of Version I because all the parameters for stochastically generating variables are not read in.

SUBROUTINE EVAP

EVAP calculates potential evaporation from soil surface in millimeters, during a time-step. The Blaney-Criddle method is used and closely follows the approach of Griffin et al. 1974.

Refer to Table A-2 for definitions of variables used in this program. This table is also found in the complete program listing at the end of this section.

ZEVAP=F1(ZAIRT, ARRAY1, NPTS)

EVAP 056

Here, ZEVAP is multiplying factor ($\lesssim 1$) depending on air temperature, which has been empirically determined.

Table A-2. Variable dictionary for EVAP

A, B, C, Z	TEMPORARY VARIABLES USED IN DAYLIGHT CALCULATION.
ARRAY(5,2)	PAIRS OF DATA POINTS FOR INTERPOLATION BY F1 IN CALCULATING BLANEY CRIDDLE FACTOR.
CVVCDV	FRACTION OF SOIL SURFACE COVERED BY ANNUAL AND PERENNIAL VEGETATION.
DALITE(365)	ARRAY INDEXED BY JULIAN DATE . GIVES NUMBER OF MINUTES OF DAYLIGHT ON THAT JULIAN DATE.
DLTFR(365)	ARRAY INDEXED BY JULIAN DATE AND IS FRACTION OF YEAR'S DAYLIGHT WHICH FALLS ON THAT JULIAN DATE.
F1	FUNCTION WHICH LINEARLY INTERPOLATES BETWEEN PAIRS OF DATA POINTS TO DETERMINE DEPENDENT VARIABLE.
LAT	LATITUDE OF SITE, DEGREES.
MM	FLAG USED ONLY IN CASE PHJDAT IS EVER ZERO.
NPTS	NUMBER OF PAIRS OF DATA POINTS ACTUALLY USED IN ARRAY.
PMDT	LENGTH OF TIMESTEP, DAYS.
PMJDAT	JULIAN DATE OF FIRST DAY OF TIMESTEP.
RCHECK(20)	ARRAY USED TO READ AND WRITE COMMENTS IN WITH INITIAL DATA.
TOTMIN	MINUTES OF DAYLIGHT IN YEAR.
ZAIRT	AVERAGE TIMESTEP AIR TEMPERATURE, DEGREES CELCIUS.
ZEVAP	POTENTIAL EVAPORATION FOR TIMESTEP, MM, DRIVING VARIABLE USED BY OTHER SUBMODELS.

```
IF(PMJDAT .GT. 0) GO TO 670
PMJDAT=1
MM=1
670 CONTINUE
```

```
EVAP 057
EVAP 058
EVAP 059
EVAP 060
```

PMJDAT is used as a subscript in the next line. These lines simply set it equal to 1 in case it should ever be 0.

```
ZEVAP=ZEVAP*(1.8*ZAIRT + 32.)*DLTFR(PMJDAT)*(1.-CVVCOV)*25.4*PMDT EVAP 063
```

This, in essence, is subroutine EVAP. The potential evaporation equals the empirical factor times the temperature in degrees Fahrenheit, times the fraction of the year's daylight occurring today, times the fraction of uncovered soil surface, times 25.4 to change from inches to millimeters, times PMDT to change from one day to the value for the entire time-step.

```
CVVCOV=0.0
```

```
EVAP 064
```

Reset CVVCOV. It is calculated each time-step by one or both vegetation submodels.

```
IF(MM .EQ. 0) GO TO 680
PMJDAT=0
MM=0
680 CONTINUE
```

```
EVAP 065
EVAP 066
EVAP 067
EVAP 068
```

Set PMJDAT back to 0 if it was changed to 1 in lines 57-60 above.

```
ENTRY EVINIT
```

```
EVAP 073
```

Entry point called once from PSWG to read initial data and do daylight calculations which need to be done only once.

```
DO 650 I=1, 365
A=730.,-.274*LAT+.00793*(LAT**2)
B=.342, -.78*LAT+.1*(LAT**2)
C=1
Z=2.*3.1416*((C+285.)/365.)
DALITE(I)=A+B*SIN(Z)
TOTMIN=DALITE(I)+TOTMIN
650 CONTINUE
```

```
EVAP 108
EVAP 109
EVAP 110
EVAP 111
EVAP 112
EVAP 114
EVAP 115
EVAP 116
```

In this loop calculate the length of daylight in minutes for each day of the year at latitude LAT. Also calculate TOTMIN, the total minutes of daylight in a year.

```
DO 660 I=1, 365
DLTFR(I)=DALITE(I)/TOTMIN
660 CONTINUE
```

```
EVAP 119
EVAP 120
EVAP 121
```

Calculate DLTFR, the fraction of daylight which occurs each day of the year.

SUBROUTINE RINT

This program calculates ZRINT, precipitation intensity in mm/hr. ZRINT is used by WATER in determining rate of infiltration into soil. Intensity is important mainly if the rate of water arriving at the soil surface is greater than the infiltration rate. Under these conditions, runoff or runoff could occur.

Refer to Table A-3 for definitions of variables used in this program. This table is also repeated in the complete program listing at the end of this section.

DO 550 I=1,PMDT

RINT 070

Make one pass through this loop for each day of time-step.

Table A-3. Variable dictionary for RINT

A, B	PARAMETERS IN HIGH INTENSITY CALCULATION.
ARRAY(10)	HOLDS UP TO 5 PAIRS OF DATA POINTS FOR INTERPOLATION BY FUNCTION F1 IN DETERMINING NORMAL INTENSITY.
BA	INTERMEDIATE VARIABLE IN HIGH INTENSITY CALCULATION.
B1	INTERMEDIATE VARIABLE IN HIGH INTENSITY CALCULATION.
F1	FUNCTION WHICH LINEARLY INTERPOLATES BETWEEN NPTB PAIRS OF DATA POINTS.
ISBEDD	INTEGER FROM WHICH RANDOM NUMBERS ARE GENERATED.
N	INDEX OF TIME OF YEAR. IN MIDDLE OF YEAR N#1. OTHER TIMES OF YEAR N#2.
NPTB	NUMBER OF PAIRS OF DATA POINTS IN NORMAL INTENSITY CALCULATION.
PDAY1,PDAY2	BEGINNING AND ENDING JULIAN DATES OF CENTRAL SEGMENT OF YEAR.
PMDT	LENGTH OF TIMESTEP, DAYS.
PMJDAT	JULIAN DATE OF BEGINNING OF TIMESTEP.
PTH	PRECIP AMOUNT ABOVE WHICH HIGH INTENSITY CAN OCCUR
PA(2)	COMPARED WITH R TO SEE IF HIGH INTENSITY ACTUALLY OCCURRED.
R	TEMPORARY VARIABLE, SET EQUAL TO RANDOM NUMBER
RCHECK(20)	ARRAY USED FOR READING AND WRITING COMMENTS IN WITH INITIALIZATION DATA.
TR	TEMPORARY VARIABLE.
TRAIN(20)	DAILY PRECIPITATION AMOUNTS, MM. ARRAY INDEXED BY DAY OF TIMESTEP
X	TODAY'S RAIN
Y	TODAY'S PRECIPITATION INTENSITY, MM/HR.
YSUM	SUM OVER TIMESTEP OF DAILY PRECIP INTENSITY TIMES PRECIP AMOUNT.
ZRAIN	TIMESTEP PRECIPITATION,MM. DRIVING VARIABLE USED BY WATER SUBMODEL.
ZRINT	RAIN INTENSITY, MM/HR. DRIVING VARIABLE USED BY WATER SUBMODEL.

X=TRAIN(I)

RINT 074

Get today's precipitation amount, x, from appropriate location in TRAIN, which was loaded in PSWG.

```
IF(X .GT. 1.E-5) GO TO 100
GO TO 590
```

RINT 077
RINT 079

If $x \geq 1.0 \times 10^{-5}$, this is considered precipitation so an intensity must be determined. Otherwise, go to end of loop.

100 IF(X .LT. PTH) GO TO 500

RINT 082

If there is precipitation today but the amount is less than threshold value PTH, go to statement 500 and calculate normal intensity for this time of year.

R=RANDOM(18EED)

RINT 085

If we reach here, a high intensity is possible. Choose a random number uniformly distributed in interval 0 to 1.

```
N#2
IF((PMJDAT .GE. PDAY1) ,AND, (PMJDAT .LE. PDAY2)) N#1
```

RINT 091
RINT 092

Determine which of two segments of year we're in. In central segment (summer, roughly) N = 1.

IF(R .GT. PA(N)) GO TO 500

RINT 095

If random number chosen above is greater than a threshold PA, which varies with segment of year, then go to section calculating normal intensity for this time of year.

R=R/PA(N)

RINT 097

If we reach here, a high intensity will result for today's precipitation. Generate a new random number.

```
150 TR=BA*(1.-R)
IF(TR .LE. 1.E-10) TR=1.E-10
Y=B1*ALOG(TR)
IF(Y .GT. 25.) Y=25.
GO TO 520
```

RINT 099
RINT 100
RINT 102
RINT 105
RINT 106

Calculate intensity from exponential distribution. TR is not allowed to be smaller than 10^{-10} in order to keep ALOG function manageable. Also, intensity is kept less than 25 mm/hr (a value it would almost never reach anyway). Go on to YSUM calculation.

Lines 99 and 102 require several lines of algebra to derive. From "Local Climatological Data" sheets obtained from

the U.S. Weather Bureau for the station of interest (Pocatello, Idaho, for Curlew Valley runs), a histogram was constructed of

(frequency of precipitation events per .01 in/hr interval
where intensity ≥ 0.1 in/hr)

vs.

(intensity, in/hr).

Data over a period of several years were used. This histogram was fit with the expression:

$$\text{frequency} = ae^{-bx}, \quad (\text{A-1})$$

where x is the intensity, in/hr.

Then, if intensity > 0.1 in/hr, probability for intensity to be between x and $x+dx$ is

$$P(x)dx = (ae^{-bx})(dx/.01). \quad (\text{A-2})$$

If intensity > 0.1 in/hr, the probability for it to be between .1 and ∞ is 1, i.e.:

$$1 = \int_{0.1}^{\infty} (ae^{-bx})(dx/.01) = [a/(.01b)]e^{-1b}. \quad (\text{A-3})$$

If we let S be the probability that 0.1 in/hr $<$ intensity $\leq x^*$, then

$$S = \int_{0.1}^{x^*} (ae^{-bx})(dx/.01). \quad (\text{A-4})$$

If the integral is carried out,

$$S = 1 - [a/(0.01b)]e^{-bx^*}. \quad (\text{A-5})$$

Now, if we let $S = R$, where R is a random number chosen uniformly over the range from 0 to 1, and solve Equation A-5 for x , we get

$$x^* = -(1/b) \ln [(0.01b/a)(1-R)]. \quad (\text{A-6})$$

The values of x^* will then have a distribution given by ae^{-bx} , as required.

The transformation of Equation A-5 into FORTRAN code is straightforward. Parameters a and b become A and B . The factor $0.01b/a$ becomes $0.01 * B/A = BA$; $1/b$ becomes $1/B \Rightarrow 25.4/B = B1$, so that intensities come out in mm/hr, not in/hr. Thus, $(0.01b/a)(1-R)$ becomes $BA * (1-R) = TR$; x^* becomes Y ; and $Y = -B1 * ALOG(TR)$.

```
500 Y=F1(PMJDAT, ARRAY, NPT8)
```

```
RINT 110
```

This is the normal intensity calculation. This line is missed only if intensity is high (i.e., this line is seldom missed). Function F1 interpolates between values found in ARRAY, dependent on time of year.

520 Y8UHDXeY + Y8UM

RINT 113

Continue running sum over time-step of daily intensity times amount.

```
IF(ZRAIN .LE. 1.E-6) GO TO 570
ZINT = YSUM/ZRAIN
GO TO 580
570 ZRAIN=0.0
ZINT=0.0
580 IF((ZINT*24.*PMDT) .LT. ZRAIN) ZINT=ZRAIN/(24.*PMDT)
```

RINT 118
RINT 119
RINT 120
RINT 121
RINT 122
RINT 123

Determine average rain intensity, making sure of two things first: 1) that we don't divide by zero, and 2) that the precipitation amount we'd get if precipitation fell at rate ZINT for the entire time-step is at least as large as the total time-step precipitation already determined in PSWG.

ENTRY RIINIT

RINT 129

Entry point for reading and writing initial data and comments, and for calculations which need to be done only once.

```
BA=0,0!+B/A
B1=25.4/B
```

RINT 176
RINT 177

Calculate BA and B1 which are used in high intensity calculation (lines 99 and 102).

FUNCTION IPROB (A,N)

IPROB (A,N) determines an index from 1 to N+1 given an integrated probability distribution A and a uniformly chosen random number X, $0 \leq X \leq 1$. A is an array with N values such that $A(1) < A(2) < A(3) < \dots < A(N) \leq 1$. If $A(1) > X$, then IPROB = 1. If $A(2) > X > A(1)$, then IPROB = 2, etc. If $X > A(N)$, then IPROB = N+1. Array A can be set up in many ways. The index determined can be for precipitation size class, wind speed class, relative humidity (RH) class, etc. For example, we have RH classes set up so that if IPROB = 1, RH = 0, if IPROB = 2, RH = 0.1, ..., if IPROB = 11, RH = 1.0.

X=RANDOM(ISEED)

IPROB 04

Choose random number between 0 and 1.

```
DO 1 I=1,N
IF (A(I) ,GT, X) GO TO 2
001 CONTINUE
```

IPROB 05
IPROB 06
IPROB 07

This DO loop takes each value of A, starting with the smallest, and checks it against the value of X, until a value is found greater than X. The loop is then exited.

002 IPROB=I

IPROB 08

Set value of function equal to current value of I. Usually this means $A(I-1) < X < A(I)$. If DO loop was exited normally, i.e., $X >$ all values of A, then $I = N + 1$.

COMPLETE PROGRAM LISTING

SUBROUTINE PSWG, VERSION I

	BETWEEN -1 AND +1).	C PSG1 087
SHUM	RUNNING SUM OF UP TO PMDT DAYS' RELATIVE HUMIDITY.	C PSG1 088
SMAX	RUNNING SUM OF UP TO PMDT DAYS' MAXIMUM TEMPERATURES, DEGREES CELCIUS.	C PSG1 089
SMIN	RUNNING SUM OF UP TO PMDT DAYS' MINIMUM TEMPERATURES, DEGREES CELCIUS.	C PSG1 090
SPREC	RUNNING SUM OF UP TO PMDT DAYS' PRECIPITATION EVENTS, MM.	C PSG1 091
SSUN	RUNNING SUM OF UP TO PMDT DAYS' PER CENT POSSIBLE SUNLIGHT	C PSG1 092
SUN(10,13)	INTEGRATED PROBABILITY DISTRIBUTION OF PER CENT POSSIBLE SUNLIGHT CLASS BY PERIOD OF YEAR.	C PSG1 093
SWIND	RUNNING SUM OF UP TO PMDT DAYS' AVERAGE WIND SPEEDS, KM/HR.	C PSG1 094
TMAX	MAXIMUM TEMPERATURE FOR CURRENT DAY, DEGREES CELCIUS.	C PSG1 095
TMIN	MINIMUM TEMPERATURE FOR CURRENT DAY, DEGREES CELCIUS.	C PSG1 096
TRAIN(20)	ARRAY WHICH HOLDS DAILY PRECIP VALUES FOR TIMESTEP (USED BY RAIN INTENBITY ROUTINE).	C PSG1 097
WIND(7,13)	INTEGRATED PROBABILITY DISTRIBUTION OF WIND SPEED CLASS BY PERIOD OF YEAR,	C PSG1 098
XMAX(1),XMAX(2)	PARAMETERS FOR SINE WAVE FIT TO SEVERAL YEARS' DAILY MAXIMUM TEMPERATURES, TAKEN AT NEAREST WEATHER BUREAU SITE.	C PSG1 099
XMAX(3)	STANDARD DEVIATION OF DATA ABOUT SINE WAVE FIT USING XMAX(1) AND XMAX(2).	C PSG1 100
XMIN(1),XMIN(2)	PARAMETERS FOR LINEAR REGRESSION BETWEEN TMAX AND TMIN.	C PSG1 101
XMIN(3)	STANDARD DEVIATION OF TMIN.	C PSG1 102
ZAIRT	AVERAGE DAILY AIR TEMPERATURE FOR TIMESTEP, DEGREES CELCIUS, DRIVING VARIABLE USED BY OTHER SUBMODELS.	C PSG1 103
ZESUM	SUM FROM OCTOBER 1 OF ZEVAP, MM.	C PSG1 104
ZEVAP	POTENTIAL EVAPORATION, MM/TIMESTEP, DRIVING VARIABLE USED BY OTHER SUBMODELS.	C PSG1 105
ZPHPD	PHOTOPERIOD OF FIRST DAY IN TIMESTEP, HOURS, DRIVING VARIABLE USED BY OTHER SUBMODELS.	C PSG1 106
ZRAIN	TOTAL PRECIPITATION FOR TIMESTEP, MM, DRIVING VARIABLE USED BY OTHER SUBMODELS.	C PSG1 107
ZRH	AVERAGE DAILY RELATIVE HUMIDITY, DECIMAL FRACTION FROM 0-1, DRIVING VARIABLE USED BY OTHER SUBMODELS.	C PSG1 108
ZRINT	PRECIPITATION INTENSITY, MM/HR, DRIVING VARIABLE USED BY OTHER SUBMODELS.	C PSG1 109
ZRSUM	SUM FROM OCTOBER 1 OF ZRAIN, MM.	C PSG1 110
ZSUN	AVERAGE DAILY PER CENT POSSIBLE SUNLIGHT FOR TIMESTEP, DECIMAL FRACTION FROM 0-1, DRIVING VARIABLE USED BY OTHER SUBMODELS.	C PSG1 111
ZTMAX	AVERAGE DAILY MAXIMUM TEMPERATURE FOR TIMESTEP, DEGREES CELCIUS, DRIVING VARIABLE USED BY OTHER SUBMODELS.	C PSG1 112
ZTMIN	AVERAGE DAILY MINIMUM TEMPERATURE FOR TIMESTEP, DEGREES CELCIUS, DRIVING VARIABLE USED BY OTHER SUBMODELS.	C PSG1 113
ZWIND	AVERAGE DAILY WIND SPEED FOR TIMESTEP, DRIVING VARIABLE USED BY OTHER SUBMODELS.	C PSG1 114
SHUM=0, SMIN=0, SPREC=0, SSUN=0, SWIND=0, SHUM=0,		C PSG1 115 C PSG1 116 C PSG1 117 C PSG1 118 C PSG1 119 C PSG1 120 C PSG1 121 C PSG1 122 C PSG1 123 C PSG1 124 C PSG1 125 C PSG1 126 C PSG1 127 C PSG1 128 C PSG1 129 C PSG1 130 C PSG1 131 C PSG1 132 C PSG1 133 C PSG1 134 C PSG1 135 C PSG1 136 C PSG1 137 C PSG1 138 C PSG1 139 C PSG1 140 C PSG1 141 C PSG1 142 C PSG1 143 C PSG1 144 C PSG1 145 C PSG1 146 C PSG1 147 C PSG1 148 C PSG1 149 C PSG1 150 C PSG1 151 C PSG1 152 C PSG1 153 C PSG1 154 C PSG1 155 C PSG1 156 C PSG1 157 C PSG1 158 C PSG1 159 C PSG1 160 C PSG1 161 C PSG1 162 C PSG1 163 C PSG1 164 C PSG1 165 C PSG1 166 C PSG1 167 C PSG1 168 C PSG1 169 C PSG1 170 C PSG1 171 C PSG1 172 C PSG1 173 C PSG1 174 C PSG1 175 C PSG1 176

```

      JDAY=PHJDAT          PSG1 177
      MOAY=MDAY             PSG1 178
C
C
C   MAIN LOOP           PSG1 179
      DO 3 I=1,PMDT        PSG1 180
      MTIME=MDAY/28+1       PSG1 181
      IF (MTIME .GT. 13) MTIME=13
C
C   READ IN TEMP AND PRECIP DATA IF FLAG SET    PSG1 182
      IF(.NOT.READ)GOTO100  PSG1 183
  020 READ(8,25,END=500)TMAX,TMIN,PRECIP        PSG1 184
  025 FORMAT(7X,2F6.1,3F6.1)                      PSG1 185
      GOTO30
C
C   500 READ=.FALSE.                                PSG1 186
C   IF WE REACH HERE THEN ADDITIONAL TEMPS AND PRECIP WILL BE
C   SUPPLIED BY THE STOCHASTIC WEATHER GENERATOR.        PSG1 187
      GOTO100
C
C   030 CONTINUE                                     PSG1 188
C
C   NOW CHECK DATA FOR BEING REASONABLE            PSG1 189
      IF(TMAX.LT.TMIN)GOTO40  PSG1 190
      IF((TMAX,LT.=30.),OR,(TMAX,GT.45.))GOTO40  PSG1 191
      IF((TMIN,LT.=30.),OR,(TMIN,GT.45.))GOTO40  PSG1 192
      IF((PRECIP,LT.50.),AND,(PRECIP,GE.0.0)),OR,(PRECIP,GT.5000.))  PSG1 193
      * GOTO60
C   SOMETIMES ZERO PRECIP IN D8CODE8 IS LISTED AS A RIDICULOUSLY LARGE NO  PSG1 194
C
C   SOMETHING WRONG = WRITE OFFENDING CARD AND STOP      PSG1 195
  040 WRITE(6,50)PMJDAT,TMAX,TMIN,PRECIP            PSG1 196
  050 FORMAT(1',1S,3F12.3)                          PSG1 197
      STOP
C
C   060 CONTINUE                                     PSG1 198
      TMAX=8MAX+TMAX          PSG1 199
      TMIN=8MIN+TMIN          PSG1 200
      SPREC=8PREC+PRECIP      PSG1 201
C   LOAD PRECIP INFORMATION FOR ZPRINT CALCULATION    PSG1 202
      TRAIN(I)=PRECIP         PSG1 203
      GOTO2
C
C
C   100 CONTINUE                                     PSG1 204
C   TEMPERATURE SECTION                           PSG1 205
C   TMAX IS A QUADRATIC FIT TO THE YEAR'S TEMPERATURES  PSG1 206
C   RNDR IS 'RANDOM NORMAL' NUMBER GENERATOR ( ,68 OF VALUES BETWEEN  PSG1 207
C   =1 AND +1)                                         PSG1 208
C   XMAX(3) IS THE STANDARD DEVIATION ABOUT THIS FIT.  PSG1 209
C   THE FIRST TMAX BELOW IS A SINE WAVE FIT TO THE YEAR'S MEAN MAX TEMP  PSG1 210
C   .017214 = 2 * PI / 365.                         PSG1 211
C   1.570796 = PI / 2.                            PSG1 212
      TMAX = XMAX(1) + XMAX(2)*SIN(.017214*MOD((PHJDAT+344.),365.))
      C =1,570796)                         PSG1 213
C   THE FOLLOWING TMAX IS THE DAY'S MAXIMUM TEMPERATURE.  PSG1 214
  001 TMAX = TMAX + XMAX(3)*RNDR(ISEED)            PSG1 215
      TMIN=XMIN(1)+XMIN(2)*TMAX                     PSG1 216
      TMIN=TMIN+XMIN(3)*RNDR(ISEED)                  PSG1 217
      IF (TMIN .GT. TMAX) GO TO 1                   PSG1 218
      TMAX=8MAX+TMAX          PSG1 219
      TMIN=8MIN+TMIN          PSG1 220
      SPREC=8PREC+PRECIP      PSG1 221
      TRAIN(I)=AMT(J)
      GOTO2
C
C
C   PRECIPITATION SECTION                         PSG1 222
C   IYESY HAS SOMETHING TO DO WITH WHETHER OR NOT WE HAD RAIN YESTERDAY.  PSG1 223
      IYESY=IPROB(RAIN(IYESY,MTIME),1)              PSG1 224
      IF(IYESY .NE. 2) TRAIN(I)=0.0                 PSG1 225
      IF (IYESY .NE. 2) GO TO 2                   PSG1 226
      J=IPROB(PREC(1,MTIME),5)                      PSG1 227
      SPREC=8PREC+AMT(J)
      TRAIN(I)=AMT(J)
C
C   WIND SECTION                                 PSG1 228
  002 J=IPROB(WIND(1,MTIME),7)                    PSG1 229
      SWIND=8WIND+(J=1)*8.05                       PSG1 230
C
C   PERCENT POSSIBLE SUNLIGHT SECTION          PSG1 231
      J=IPROB(BUN(1,MTIME),10)                      PSG1 232
      SSUN=8SUN+(J=1)*0.1                          PSG1 233
C
C   RELATIVE HUMIDITY SECTION                  PSG1 234
      J=IPROB(HUM(1,MTIME),10)                      PSG1 235
      SHUM=8HUM+(J=1)*0.1                          PSG1 236
  003 MOAY=MDAY+1                               PSG1 237
C   END MAIN LOOP                                PSG1 238
C

```

```

C          X#1./PMDT          P8G1 267
C          ZTMAX=SMAX*X      P8G1 268
C          ZTMIN=SMIN*X      P8G1 269
C          ZWIND=SWINDEX     P8G1 270
C          ZWIND=ZWIND*X      P8G1 271
C          ZWIND IS IN KM/HR  P8G1 272
C          ZSUN=8SUN*X       P8G1 273
C          ZRH=SHUM*X        P8G1 274
C          ZRAIN=SPREC        P8G1 275
C          ZAIRT=(ZTMAX+ZTMIN)/2, P8G1 276
C          ZSUN=8SUN*X       P8G1 277
C          ZRH=SHUM*X        P8G1 278
C          ZRAIN=SPREC        P8G1 279
C          ZAIRT=(ZTMAX+ZTMIN)/2, P8G1 280
C          THIS IS WILKINSON PHOTOPERIOD CALCULATION P8G1 281
C          DECL=ARSIN(SIN(6,2831853*23,45/360.))*
C          COS(MOD((PMJDAT+93.,)365.)#6,2831853/365.)) P8G1 282
C          X=(8IN(LAT#6,2831853/360.)*TAN(DECL)+8IN(.875*6,2831853/360.))/ P8G1 283
C          COS(LAT#6,2831853/360.) P8G1 284
C          IF (X .GT. 1.) X#1., P8G1 285
C          IF (X .LT. -1.) X#1., P8G1 286
C          ZPHPD=12. + .1333333*ARSIN(X)*360./6,2831853 P8G1 287
C          ZPHPD=12. + .1333333*ARSIN(X)*360./6,2831853 P8G1 288
C          DETERMINE RAIN INTENSITY P8G1 289
C          CALL RINT(ZRINT, TRAIN, ZRAIN, PMDT, PMJDAT, ISEED) P8G1 290
C          ZRINT IS RETURNED IN MM/HR P8G1 291
C          DETERMINE ZEVAP P8G1 292
C          CALL EVAP P8G1 293
C          ZEVAP IS IN MM/TIMESTEP P8G1 294
C          THIS IS THE WEATHER MODIFICATION P8G1 295
C          ZRAIN=FACTOR*ZRAIN P8G1 296
C          SUM SOME VARIABLES FROM OCT 1 = = WATER YEAR P8G1 297
C          IF(PMJDAT.LT.270)GOTO900 P8G1 298
C          IF(ABS(PMJDAT-270) .GE. PMDT) GO TO 900 P8G1 299
C          ZRSUM=0.0 P8G1 300
C          ZESUM=0.0 P8G1 301
C          900 ZRSUM=ZRSUM+ZRAIN P8G1 302
C          ZESUM=ZESUM+ZEVAP P8G1 303
C          IF(NNN .LT. 58) GO TO 910 P8G1 304
C          WRITE(4,930) P8G1 305
C          NNN=0 P8G1 306
C          910 ARITE(4,940)PMJDAT,ZTMAX,ZTHIN,ZRH,ZPHPD,ZRAIN,ZRINT,ZRSUM,ZSUN P8G1 307
C          *,ZEVAP,ZESUM,ZWIND P8G1 308
C          NNN=NNN+1, P8G1 309
C          930 FORMAT('1', 1PMJDAT ZTMAX ZTMIN ZRH ZPHPD ZRAIRP8G1 310
C          *N ZRINT ZRSUM ZSUN ZEVAP ZESUM ZWINDP8G1 311
C          *D1, /) P8G1 312
C          940 FORMAT('1', 4X, 13, 2(4X,F6.2),5X, F4.2, 3(5X, F5.2), P8G1 313
C          * 2(5X, F7.2), 5X, F5.2, 5X, F7.2, 5X, F5.2) P8G1 314
C          RETURN P8G1 315
C          ENTRY ZINIT P8G1 316
C          COMMON TIME,TSTART,TEND,DT,DTPR,DTPL, P8G1 317
C          1CAAR(6,8),CADEBT(6,8),CADETH,CAUWST,CDDL(12,4),CHD(10),CHDX(10), P8G1 318
C          2CHDOXX(10),CNFFIX,CNSDF,CNSDS,CNSOMF,CNSOMS,CNSUP,CVDETH(12,4), P8G1 319
C          3CVLTFR(11,4),CPHEN(6,8),CPH8(6),CVRDBT(6,10),CVT8PR(6,8),CVVCOV,P8G1 320
C          4CWINF,CWPSI(10),PMDT,PMDTPL,PMDTPL,PMFGP8,PMJDAT,PMN,PMNCOH,PMNCP,PMNCP,P8G1 321
C          5PK(10),XAAC(4),XAAWT(4,8),XAAT(4),XAFT8(4),XAFT8(4),XANUMB(4,6),P8G1 322
C          6XABA(4),XABAWT(4),XAYNG(4),XAYWT(4),XH80LT(10),XNMN,XN80MF,XN80MS,P8G1 323
C          7XVFG(6,5),XVLITR(12,4),XVPLNT(6,8),XVTOTL,XWHTHA(10),XW8TND,ZAIRT,P8G1 324
C          8ZEVAP,ZESUM,ZPHPD,ZRAIN,ZRINT,ZRSUM,ZRH,ZRINT,ZRISUM,ZSUN,ZTHMAX,ZTMIN, P8G1 325
C          9ZWIND P8G1 326
C          LOGICAL READ P8G1 327
C          REAL LAT P8G1 328
C          INTEGER PMJDAT P8G1 329
C          COMMON /SUNNY/ IYEST,ISEED P8G1 330
C          DIMENSION XMAX(3),XMIN(3),RAIN(2,13),PREC(6,13),AMT(6), P8G1 331
C          * WIND(7,13), SUN(10,13), HUM(10,13) P8G1 332
C          DIMENSION TRAIN(20) P8G1 333
C          DIMENSION RCHECK(20) P8G1 334

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```

C      WRITE(4,930)                               PSG1 358
C      NNNB0                                     PSG1 359
C      READ(5,710) RCHECK                      PSG1 360
C      WRITE(6,720) RCHECK                      PSG1 361
C      READ(5,710) RCHECK                      PSG1 362
C      WRITE(6,720) RCHECK                      PSG1 363
C      READ(5,710) RCHECK                      PSG1 364
C      WRITE(6,720) RCHECK                      PSG1 365
C      READ(5,/) ISEED                         PSG1 366
C      WRITE(6,/) ISEED                         PSG1 367
C      READ(5,/) LAT                           PSG1 368
C      WRITE(6,/) LAT                           PSG1 369
C      READ(5,/) XMAX,XMIN                     PSG1 370
C      WRITE(6,/) XMAX                         PSG1 371
C      READ(5,/) XMAX,XMIN                     PSG1 372
C      WRITE(6,/) XMIN                         PSG1 373
C      READ(5,/) XMIN                         PSG1 374
C      READ(5,/) XMIN                         PSG1 375
C      READ(5,/) RAIN                          PSG1 376
C      WRITE(6,/) RAIN                         PSG1 377
C      READ(5,/) PREC                         PSG1 378
C      WRITE(6,/) PREC                         PSG1 379
C      READ(5,/) AMT                           PSG1 380
C      WRITE(6,/) AMT                           PSG1 381
C      READ(5,/) AMT                           PSG1 382
C      READ(5,/) WIND                          PSG1 383
C      WRITE(6,/) WIND                         PSG1 384
C      READ(5,/) WIND                          PSG1 385
C      READ(5,/) WIND                          PSG1 386
C      READ(5,710) RCHECK                      PSG1 387
C      WRITE(6,720) RCHECK                      PSG1 388
C      READ(5,710) RCHECK                      PSG1 389
C      WRITE(6,720) RCHECK                      PSG1 390
C      READ(5,710) RCHECK                      PSG1 391
C      WRITE(6,720) RCHECK                      PSG1 392
C      READ(5,710) SUN                         PSG1 393
C      WRITE(6,720) SUN                         PSG1 394
C      READ(5,710) HUM                         PSG1 395
C      WRITE(6,720) HUM                         PSG1 396
C      READ(5,710) PHFAC                        PSG1 397
C      WRITE(6,720) PHFAC                        PSG1 398
C      READ(5,710) READ                         PSG1 399
C      WRITE(6,720) READ                         PSG1 400
C      READ(5,710) READ                         PSG1 401
C      WRITE(6,720) READ                         PSG1 402
C      READ(5,710) READ                         PSG1 403
C      WRITE(6,720) READ                         PSG1 404
C      READ(5,710) FACTOR                      PSG1 405
C      WRITE(6,720) FACTOR                      PSG1 406
C      READ(5,710) FACTOR                      PSG1 407
C      WRITE(6,720) FACTOR                      PSG1 408
C      READ(5,710) FACTOR                      PSG1 409
C      WRITE(6,720) FACTOR                      PSG1 410
C      710 FORMAT(20A4)                         PSG1 411
C      720 FORMAT(' ', 20A4)                      PSG1 412
C
C      IYESTM1                                  PSG1 413
C
C      CALL INITIALIZATION SECTION OF SUBROUTINES EVAP AND RINT
C      CALL EVINIT                                PSG1 414
C      CALL RIINIT                                PSG1 415
C
C      RETURN                                    PSG1 416
C      END                                       PSG1 417
C
C      PSG1 418
C      PSG1 419
C      PSG1 420
C      PSG1 421
C      PSG1 422
C      PSG1 423

```

SUBROUTINE PSWG, VERSION II

```

SUBROUTINE PSWG                               PSG2 001
C
C      THIS VERSION OF PSWG USED IN 5-YEAR RUNS.
C      WEATHER VARIABLES ARE READ FROM WEATHER DATA FILE.    PSG2 002
C
C      VARIABLE DICTIONARY                           PSG2 003
C
C      DECL          ANGLE CALCULATED IN PHOTOPERIOD CALCULATION.    PSG2 004
C
C      PSG2 005
C      PSG2 006
C      PSG2 007
C      PSG2 008
C      PSG2 009
C      PSG2 010
C      PSG2 011
C      PSG2 012
C      PSG2 013
C      PSG2 014
C      PSG2 015

```

EVAP	SUBROUTINE WHICH CALCULATES POTENTIAL EVAPORATION.	C P8G2 016
FACTOR	PRECIPITATION FACTOR BY WHICH EACH EVENT IS MULTIPLIED.	C P8G2 017
ISEED	SEED FROM WHICH RNDR GENERATES NEXT RANDOM NUMBER.	C P8G2 018
JDAY	JULIAN DATE AT BEGINNING OF TIMESTEP.	C P8G2 019
LAT	LATITUDE OF SITE.	C P8G2 020
NNN	COUNTER TO DETERMINE WHEN TO START PRINTING ON NEXT PAGE.	C P8G2 021
PMDT	TIMESTEP LENGTH, DAYS.	C P8G2 022
PRECIP	PRECIPITATION FOR CURRENT DAY, MM.	C P8G2 023
PHJDAT	JULIAN DATE AT BEGINNING OF TIMESTEP, VALUE DETERMINED IN MAIN PROGRAM.	C P8G2 024
PWFAC	FACTOR FOR ADJUSTING AVERAGE WIND SPEED IF SITE IS KNOWN TO HAVE DIFFERENT AVERAGE WIND SPEED.	C P8G2 025
RCHECK(20)	VARIABLE USED TO READ AND WRITE COMMENTS IN WITH INITIAL DATA.	C P8G2 026
RINT	SUBROUTINE WHICH CALCULATES PRECIPITATION INTENSITY.	C P8G2 027
SHUM	RUNNING SUM OF UP TO PMDT DAYS! RELATIVE HUMIDITY.	C P8G2 028
SMAX	RUNNING SUM OF UP TO PMDT DAYS! MAXIMUM TEMPERATURES, DEGREES CELCIUS.	C P8G2 029
SMIN	RUNNING SUM OF UP TO PMDT DAYS! MINIMUM TEMPERATURES, DEGREES CELCIUS.	C P8G2 030
SPREC	RUNNING SUM OF UP TO PMDT DAYS! PRECIPITATION EVENTS, MM.	C P8G2 031
SBUN	RUNNING SUM OF UP TO PMDT DAYS! PER CENT POSSIBLE SUNLIGHT	C P8G2 032
SWIND	RUNNING SUM OF UP TO PMDT DAYS! AVERAGE WIND SPEEDS: KM/HR.	C P8G2 033
TMAX	MAXIMUM TEMPERATURE FOR CURRENT DAY, DEGREES CELCIUS.	C P8G2 034
TMIN	MINIMUM TEMPERATURE FOR CURRENT DAY, DEGREES CELCIUS.	C P8G2 035
TRAIN(20)	ARRAY WHICH HOLDS DAILY PRECIP VALUES FOR TIMESTEP (USED BY RAIN INTENSITY ROUTINE).	C P8G2 036
ZAIRT	AVERAGE DAILY AIR TEMPERATURE FOR TIMESTEP, DEGREES CELCIUS. DRIVING VARIABLE USED BY OTHER SUBMODELS.	C P8G2 037
ZEBUM	SUM FROM OCTOBER 1 OF ZEVAP, MM.	C P8G2 038
ZEVAP	POTENTIAL EVAPORATION, MM/TIMESTEP. DRIVING VARIABLE USED BY OTHER SUBMODELS.	C P8G2 039
ZPHPD	PHOTOPERIOD OF FIRST DAY IN TIMESTEP, HOURS. DRIVING VARIABLE USED BY OTHER SUBMODELS.	C P8G2 040
ZRAIN	TOTAL PRECIPITATION FOR TIMESTEP, MM. DRIVING VARIABLE USED BY OTHER SUBMODELS.	C P8G2 041
ZRH	AVERAGE DAILY RELATIVE HUMIDITY, DECIMAL FRACTION FROM 0-1. DRIVING VARIABLE USED BY OTHER SUBMODELS.	C P8G2 042
ZRINT	PRECIPITATION INTENSITY, MM/HR. DRIVING VARIABLE USED BY OTHER SUBMODELS.	C P8G2 043
ZRSUM	SUM FROM OCTOBER 1 OF ZRAIN, MM.	C P8G2 044
ZBUN	AVERAGE DAILY PER CENT POSSIBLE SUNLIGHT FOR TIMESTEP, DECIMAL FRACTION FROM 0-1. DRIVING VARIABLE USED BY OTHER SUBMODELS.	C P8G2 045
ZTHAX	AVERAGE DAILY MAXIMUM TEMPERATURE FOR TIMESTEP, DEGREES CELCIUS. DRIVING VARIABLE USED BY OTHER SUBMODELS.	C P8G2 046
ZTMIN	AVERAGE DAILY MINIMUM TEMPERATURE FOR TIMESTEP, DEGREES CELCIUS. DRIVING VARIABLE USED BY OTHER SUBMODELS.	C P8G2 047
ZWIND	AVERAGE DAILY WIND SPEED FOR TIMESTEP. DRIVING VARIABLE USED BY OTHER SUBMODELS.	C P8G2 048

```

C
C
      SMAX=0;
      SMIN=0;
      SPREC=0;
      SWIND=0;
      SSUN=0;
      SHUM=0;
      JDAY=PMJDAT
      MDAY=JDAY
C
C
C   MAIN LOOP
      DO 3 I=1,PMDT
C   READ TODAY'S DATA
      READ(6,30,END=500)TMAX,TMIN,PRECIP,WIND,PPS,RH
      30 FORMAT(10X,2F5.0,F5.2,F5.1,2F5.2)
C
      GOT0501
      500 CONTINUE
      STOP
      501 CONTINUE
C   CONVERT TO METRIC UNITS
C
C   TEMPS FROM F TO C
      TMAX=(TMAX-32.)*0.555555
      TMIN=(TMIN-32.)*0.555555
C
C   PRECIP FROM INCHES TO MM
      PRECIP=PRECIP*25.4
C
C   AVERAGE WIND SPEED FROM MILES / HR  TO KM/HR
      WIND=WIND*1.60934
C
C
C   CHECK IF VALUES ARE SENSIBLE
      IF(TMIN.GT.TMAX)GOT040
      IF((TMAX.GT.42.),OR,(TMIN.LT.-43.))GOT040
      IF((PRECIP.GT.40.),OR,(PRECIP.LT.0.0))GOT040
      IF((WIND.GT.60.),OR,(WIND.LT.0.0))GOT040
      IF((PPS.GT.1.0),OR,(PPS.LT.0.0))GOT040
      IF((RH.LT.1.00),AND,(RH.GE.0.0))GOT060
C
C   IF WE REACH HERE SOMETHING IS WRONG.  WRITE OFFENDING CARD AND STOP.
      40 WRITE(6,50)TMAX,TMIN,PRECIP,WIND,PPS,RH,PMJDAT
      50 FORMAT(11,7F10.3)
      STOP
C
C
      60 CONTINUE
      SMAX=SMAX+TMAX
      SMIN=SMIN+TMIN
      SPREC=SPREC+PRECIP
      SWIND=SWIND+WIND
      SSUN=SSUN+PPS
      SHUM=SHUM+RH
C
C   LOAD TRIM FOR USE IN SUBROUTINE RINT
      TRIM(T1)PRECIP
C
      3 CONTINUE
C   END MAIN LOOP
C
C
C
      XX1./PMDT
C
      ZTMAX=SMAX*X
      ZTMIN=SMIN*X
      ZWIND=SWIND*X
C   HERE IS A FACTOR FOR ADJUSTING AVERAGE WIND SPEED IF SITE IS KNOWN TO BE DIFFERENT FROM MEASURING STATION
      ZWIND=ZWIND * PWFACT
      ZSUN=SSUN*X
      ZRH=SHUM*X
      ZRAIN=SPREC
      ZAIRTY=(ZTMAX+ZTMIN)/2.
C
C   THIS IS WILKINSON'S PHOTOPERIOD CALCULATION
      DECL=ARCSIN(SIN(6.2831853*23.45/360.)*
      C COS(MOD((PMJDAT+193.),365.)*6.2831853/365.))
      X=(SIN(LAT+6.2831853/360.)*TAN(DFCL)+8IN(.875*6.2831853/360.))/
      C COS(LAT+6.2831853/360.)
      IF (X .GT. 1.) X=1.
      IF (X .LT. -1.) X=-1.
      ZPHPD=12. + .1333333*ARCSIN(X)*360./6.2831853
C
      PSG2 106
      PSG2 107
      PSG2 108
      PSG2 109
      PSG2 110
      PSG2 111
      PSG2 112
      PSG2 113
      PSG2 114
      PSG2 115
      PSG2 116
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      PSG2 190
      PSG2 191
      PSG2 192
      PSG2 193
      PSG2 194
      PSG2 195

```

```

C DETERMINE ZRINT
    CALL RINT(ZRINT, TRAIN, ZRAIN, PMDT, PMJDAT, ISEED)          PSG2 196
C DETERMINE ZEVAP
    CALL EVAP              PSG2 197
C HERE IS THE RAINFALL MODIFICATION
    ZRAIN=FACTOR*SPREC          PSG2 198
C
C SUMMING SECTION
C DO FOLLOWING SUMS FROM OCTOBER 1 + = WATER YEAR
    IF(PMJDAT.LT.270)GOTO900          PSG2 199
    IF(ABS(PMJDAT-270).GE. PMDT) GO TO 900          PSG2 200
    ZRSUM=0.0          PSG2 201
    ZESUM=0.0          PSG2 202
    900 ZRSUM=ZRSUM+ZRAIN          PSG2 203
    ZESUM=ZESUM+ZEVAP          PSG2 204
    IF(NNN .LT. 50) GO TO 910          PSG2 205
    WRITE(4,930)          PSG2 206
    NNN=0          PSG2 207
    910 WRITE(4,940)PMJDAT,ZTHAX,ZTHIN,ZRH,ZPHPD,ZRAIN,ZRINT,ZRSUM,ZSUN
        *,ZEVAP,ZESUM,ZWIND          PSG2 208
        NNNNNN+1          PSG2 209
    930 FORMAT(1I, 1PMJDAT ZTHAX ZTHIN ZRH ZPHPD ZRAI          PSG2 210
        *N ZRINT ZRSUM ZSUN ZEVAP ZESUM ZWINPSG2 211
        *D, /)          PSG2 212
    940 FORMAT(1I, 4X, I3, 2(4X,F6.2),5X, F4.2, 3(5X, F5.2),
        * 2(5X, F7.2), 5X, F5.2, 5X, F7.2, 5X, F5.2)          PSG2 213
C
C RETURN
C ENTRY ZINIT
C
COMMON TIME,TSTART,TEND,DT,DTPR,DTPL,
1CAARC(6,8),CADEST(6,8),CADETH,CAUWST,CDDL(12,4),CHD(10),CHDX(10),          PSG2 214
2CHDX(10),CNFIX,CNSDF,CNSDS,CNBOMF,CNSOMS,CNSUP,CVDET(12,4),          PSG2 215
3CVLTFR(11,4),CVPHEN(6,8),CVPHS(6),CVROST(6,10),CVTSPR(6,8),CVVCOV,          PSG2 216
4CWINF,CWPST(10),PMDT,PMDTPL,PMDTTR,PMGPS,PMJDAT,PMN,PMNCOH,PMNBP,          PSG2 217
5PWK(10),XA(4),XAAVHT(4,8),XAAWT(4),XAFTS(4),XAFTT(4),XANUMB(4,8),          PSG2 218
6XA8A(4),XA8ANT(4),XAYNG(4),XAYHT(4),XHSOLT(10),XNMN,XNADMF,XN8OMS,          PSG2 219
7XVFG(6,5),XVLITR(12,4),XVLPLNT(6,6),XVTOTL,XVHTA(10),XWSTND,ZATRT,          PSG2 220
8ZEVAP,ZE8UM,ZPHPD,ZRAIN,ZRSUM,ZRH,ZRINT,ZRISUM,ZSUN,ZTMAX,ZTHIN,          PSG2 221
9ZWIND          PSG2 222
C
REAL LAT
C COMMON /BUNNY/ IYEST,ISEED          PSG2 223
C
DIMENSION TRAIN(20)
DIMENSION RCHECK(20)          PSG2 224
C
WRITE(4,930)          PSG2 225
NNN=0          PSG2 226
C
READ(5,710) RCHECK          PSG2 227
WRITE(6,720) RCHECK          PSG2 228
C
READ(5,/) TSEED          PSG2 229
WRITE(6,/) ISEED          PSG2 230
C
READ(5,/) LAT          PSG2 231
WRITE(6,/) LAT          PSG2 232
C
READ(5,/) PWFAC          PSG2 233
WRITE(6,/) PWFAC          PSG2 234
C
READ(5,/) FACTOR          PSG2 235
WRITE(6,/) FACTOR          PSG2 236
C
READ(5,710) RCHECK          PSG2 237
WRITE(6,720) RCHECK          PSG2 238
C
710 FORMAT(20AH)
720 FORMAT(' ', 20A4)
C
CALL INITIALIZATION SECTIONS OF EVAP AND RINT
    CALL EVINIT          PSG2 239
    CALL RTINIT          PSG2 240
C
RETURN          PSG2 241
END          PSG2 242

```

SUBROUTINE EVAP

```

C INTEGER PMJDAT
C REAL LAT
C
C READ(5,710) RCHECK
C WRITE(6,720) RCHECK
C
C READ(5,/) LAT
C WRITE(6,/) LAT
C READ(5,/) ARRAY1
C WRITE(6,/) ARRAY1
C READ(5,/) NPTS
C WRITE(6,/) NPTS
C
C 710 FORMAT(20A4)
C 720 FORMAT(' ', 20A4)
C
C FROM GRIFFIN, HANKS BIOME REPORT
DO 650 I=1, 365
A=730.,=.274*LAT+.00793*(LAT**2)
B=34,2=,78*LAT+,1*(LAT**2)
C#1
Z=2,*3,1416*((C+285.)/365.)
C LENGTH OF DAY IN MINUTES
DALITE(I)=A+B*SIN(Z)
TOTMIN=DALITE(I)+TOTMIN
650 CONTINUE
C
C FRACTION OF DAYLIGHT FOR EACH DAY
DO 660 I=1, 365
DLTFR(I)=DALITE(I)/TOTMIN
660 CONTINUE
C
        WRITE(6,681) DALITE
        WRITE(6,681) TOTMIN
681 FORMAT(' ', 10F12.5)
C
        READ(5,710) RCHECK
        WRITE(6,720) RCHECK
C
        RETURN
END

```

SUBROUTINE RINT

```

C PA(2)      COMPARED WITH R TO SEE IF HIGH INTENSITY ACTUALLY          C RINT 038
C OCCURRED.                                              C RINT 039
C R      TEMPORARY VARIABLE. SET EQUAL TO RANDOM NUMBER                  C RINT 040
C RCHECK(20) ARRAY USED FOR READING AND WRITING COMMENTS IN WITH        C RINT 041
C INITIALIZATION DATA.                                              C RINT 042
C TR      TEMPORARY VARIABLE.                                              C RINT 043
C TRAIN(20) DAILY PRECIPITATION AMOUNTS, MM. ARRAY INDEXED BY           C RINT 044
C DAY OF TIMESTEP.                                              C RINT 045
C X       TODAY'S RAIN.                                              C RINT 046
C Y       TODAY'S PRECIPITATION INTENSITY , MM/HR.                      C RINT 047
C YSUM     SUM OVER TIMESTEP OF DAILY PRECIP INTENSITY TIMES            C RINT 048
C PRECIP AMOUNT.                                              C RINT 049
C ZRAIN    TIMESTEP PRECIPITATION/MM. DRIVING VARIABLE USED BY          C RINT 050
C WATER SUBMODEL.                                              C RINT 051
C ZINT     RAIN INTENSITY, MM/HR. DRIVING VARIABLE USED BY              C RINT 052
C WATER SUBMODEL.                                              C RINT 053
C YSUM=0.0
C
C DO 550 I=1,PMDT
C X IS TODAY'S PRECIP
C Y IS TODAY'S PRECIP INTENSITY
C X=TRAIN(I)
C
C DO WE HAVE ANY RAIN TODAY?
C IF(X .GT. 1.E-5) GO TO 100
C
C GO TO 550
C
C IF X LARGE ENOUGH ALLOW FOR HIGH INTENSITIES
C 100 IF(X .LT. PTH) GO TO 500
C
C WILL NEED A RANDOM NUMBER TO DETERMINE IF WE HAVE HIGH INTENSITY
C R=RANDOM(1SEED)
C
C DIVIDE YEAR INTO TWO SEGMENTS, ALLOWING DIFFERENT HIGH INTENSITY
C PROBABILITIES IN EACH
C
C IN CENTRAL SEGMENT N=1
C   N#2
C   IF((PMJDAT .GE. PDAY1) .AND. (PMJDAT .LE. PDAY2)) N#1
C N NOW TELLS US WHICH SEGMENT OF YEAR WE'RE IN
C
C IF(R .GT. PA(N)) GO TO 500
C GENERATE NEW (8EMI) RANDOM NUMBER
C   R=R/PA(N)
C
C 150 TR=BA*(1.-R)
C   IF(TR .LE. 1.E-10) TR=1.E-10
C
C   Y=B1*ALOG(TR)
C
C LIMIT Y TO AN INCH AN HOUR
C   IF(Y .GT. 25.) Y=25.
C   GO TO 520
C
C
C NORMAL INTENSITY CALCULATION
C 500 Y=F1(PMJDAT, ARRAY, NPTB)
C
C
C 520 YSUM=X*Y + YSUM
C
C 550 CONTINUE
C
C   IF(ZRAIN .LE. 1.E-6) GO TO 570
C   ZINT = YSUM/ZRAIN
C   GO TO 580
C 570 ZRAIN=0.0
C   ZINT=0.0
C 580 IF((ZINT*24.*PMDT) .LT. ZRAIN) ZINT=ZRAIN/(24.*PMDT)
C
C
C RETURN
C

```

```

C      ENTRY RIINIT                           RINT 128
C      DIMENSION PA(2), ARRAY(10), RCHECK(20)   RINT 129
C      DIMENSION TRAIN(20)                      RINT 130
C      INTEGER PMDT                            RINT 131
C      READ(5,600) RCHECK                      RINT 132
C      WRITE(6,610) RCHECK                      RINT 133
C      WRITE(6,630)                           RINT 134
C      READ(5,600) RCHECK                      RINT 135
C      WRITE(6,610) RCHECK                      RINT 136
C      READ(5,/) PTH                         RINT 137
C      WRITE(6,620) PTH                         RINT 138
C      WRITE(6,630)                           RINT 139
C      READ(5,600) RCHECK                      RINT 140
C      WRITE(6,610) RCHECK                      RINT 141
C      READ(5,/) PDAY1, PDAY2                 RINT 142
C      WRITE(6,620) PDAY1, PDAY2                 RINT 143
C      WRITE(6,630)                           RINT 144
C      READ(5,600) RCHECK                      RINT 145
C      WRITE(6,610) RCHECK                      RINT 146
C      READ(5,/) PDAY1, PDAY2                 RINT 147
C      WRITE(6,620) PDAY1, PDAY2                 RINT 148
C      WRITE(6,630)                           RINT 149
C      READ(5,600) RCHECK                      RINT 150
C      WRITE(6,610) RCHECK                      RINT 151
C      READ(5,/) ARRAY                         RINT 152
C      WRITE(6,620) ARRAY                         RINT 153
C      WRITE(6,630)                           RINT 154
C      READ(5,600) RCHECK                      RINT 155
C      WRITE(6,610) RCHECK                      RINT 156
C      READ(5,/) ARRAY                         RINT 157
C      WRITE(6,620) ARRAY                         RINT 158
C      WRITE(6,630)                           RINT 159
C      READ(5,/) NPT8                         RINT 160
C      WRITE(6,620) NPT8                         RINT 161
C      WRITE(6,630)                           RINT 162
C      READ(5,600) RCHECK                      RINT 163
C      WRITE(6,610) RCHECK                      RINT 164
C      READ(5,/) PA                           RINT 165
C      WRITE(6,620) PA                           RINT 166
C      WRITE(6,630)                           RINT 167
C      READ(5,600) RCHECK                      RINT 168
C      WRITE(6,610) RCHECK                      RINT 169
C      READ(5,/) A, B                         RINT 170
C      WRITE(6,620) A, B                         RINT 171
C      WRITE(6,630)                           RINT 172
C      READ(5,600) RCHECK                      RINT 173
C      WRITE(6,610) RCHECK                      RINT 174
C      BA=0.01*B/A                          RINT 175
C      B1=25.4/B                           RINT 176
C      WRITE(6,*) BA, B1                      RINT 177
C      READ(5,600) RCHECK                      RINT 178
C      WRITE(6,610) RCHECK                      RINT 179
C      READ(5,/) A, B                         RINT 180
C      WRITE(6,620) A, B                         RINT 181
C      WRITE(6,630)                           RINT 182
C      READ(5,600) RCHECK                      RINT 183
C      WRITE(6,610) RCHECK                      RINT 184
C      READ(5,600) RCHECK                      RINT 185
C      WRITE(6,610) RCHECK                      RINT 186
C      READ(5,600) RCHECK                      RINT 187
C      WRITE(6,610) RCHECK                      RINT 188
C      READ(5,600) RCHECK                      RINT 189
C      WRITE(6,610) RCHECK                      RINT 190
C      READ(5,600) RCHECK                      RINT 191
C      WRITE(6,610) RCHECK                      RINT 192
C      READ(5,600) RCHECK                      RINT 193
C      WRITE(6,610) RCHECK                      RINT 194
C
C
C      600 FORMAT(20A4)
C      610 FORMAT(' ', 20A4)
C      620 FORMAT(10F12.5)
C      630 FORMAT(' ')
C
C      RETURN
C      END

```

FUNCTION IPROB

```

FUNCTION IPROB(A,N)
DIMENSION A(1)
COMMON /SUNNY/ IYEST,ISEED
X=RANDOM(ISEED)
DO 1 I=1,N
  IF (A(I) .GT. X) GO TO 2
 001 CONTINUE
 002 IPROB*I
  RETURN
END

```

IPROB	01
IPROB	02
IPROB	03
IPROB	04
IPROB	05
IPROB	06
IPROB	07
IPROB	08
IPROB	09
IPROB	10

FUNCTION RNOR

```

FUNCTION RNOR(IR)
C THIS FUNCTION COURTESY DR. REX HURST, DEPT. COMPUTER SCIENCE AND
C APPLIED STATISTICS, UTAH STATE UNIVERSITY, LOGAN, UTAH 84322
$SET OWN
  DATA I/O/
$RESET OWN
  IF (I ,GT, 0) GO TO 30
  010 X=2,*RANDOM(IR)=1,
  Y=2,*RANDOM(IR)=1,
  S=X*X+Y*Y
  IF (S ,GE, 1,) GO TO 10
  S=SQRT(-2,* ALOG(S)/S)
  RNOR=X*S
$SET OWN
  GO2=Y*8
$RESET OWN
  I=1
  GO TO 40
  030 RNOR=GO2
  I=0
  040 RETURN
  END

```

RNOR	01
RNOR	02
RNOR	03
RNOR	04
RNOR	05
RNOR	06
RNOR	07
RNOR	08
RNOR	09
RNOR	10
RNOR	11
RNOR	12
RNOR	13
RNOR	14
RNOR	15
RNOR	16
RNOR	17
RNOR	18
RNOR	19
RNOR	20
RNOR	21
RNOR	22

LITERATURE CITED

- GRiffin, R. A., R. J. HANKS, and S. CHILDS. 1974. Model for estimating water, salt, and temperature distribution in the soil profile. US/IBP Desert Biome Res. Memo. 74-61. Utah State Univ., Logan. 12 pp.

B. HEAT

P. W. Lommen

GENERAL DESCRIPTION OF THE HEAT SUBMODEL

This submodel determines average temperature during a time-step for each soil layer. Soil temperature information is needed by VEG in determining root respiration rates, by DCMP in determining decomposition rates and by WATER in checking if the soil is frozen. Temperature determinations more frequent than once each time-step (generally 4 days) would be more accurate but, given the overall model objectives, not likely to be more useful.

The approach used is very similar to that of Hanks et al. (1971). The soil surface temperature is taken to be the mean daily air temperature at 2 m for the time-step (determined in the weather submodel). The temperature at the bottom of the profile (60-cm depth was used for the Curlew Valley simulation) is set equal to the mean air temperature for the previous 30 days (adapted from the approach of Beckman et al. 1973). Once these boundary conditions are established the temperature profile is determined by the solution of Equation B-1:

$$\frac{\partial T}{\partial t} = \frac{\partial}{\partial z} (\sigma \frac{\partial T}{\partial z}) , \quad (B-1)$$

where

- T = the soil temperature at a given point at a given instant of time, $^{\circ}\text{C}$;
- t = time, day;
- z = depth in soil, cm;
- σ = soil thermal diffusivity (the ratio of thermal conductivity, $\text{cal}\cdot\text{cm}^{-1}\cdot\text{day}^{-1}\cdot{}^{\circ}\text{C}^{-1}$, to specific heat, $\text{cal}\cdot\text{cm}^{-3}\cdot{}^{\circ}\text{C}^{-1}$), cm^2/day .

This differential equation is converted to a difference equation for computation. A set of nodes is introduced in the soil profile (at Curlew Valley the depths of these eight nodes are 0, 3, 10, 20, 30, 40, 50 and 60 cm) and the Crank-Nicholson iteration scheme (Richtmyer 1957) used to generate $N-2$ equations with $N-2$ unknowns. N is the number of soil nodes and the $N-2$ unknowns are the temperatures at all except top and bottom nodes. A tri-diagonal matrix method of solution (Richtmyer 1957) is then applied to the $N-2$ equations.

DISCUSSION

Thermal diffusivity is assumed to be independent of soil water content. Because of the boundary conditions and the relatively long time-step used (4 days for Curlew Valley), soil temperatures turn out to be fairly insensitive to the values used for thermal diffusivity. Values for thermal conductivity and specific heat were taken from Hanks et al. (1971).

CURLEW VALLEY IMPLEMENTATION

Thermal conductivity is equal to $86.4 \text{ cal}\cdot\text{cm}^{-1}\cdot\text{day}^{-1}\cdot{}^{\circ}\text{C}^{-1}$ throughout profile (Griffin et al. 1974). Specific heat, taken from the same source, is $0.3 \text{ cal}\cdot\text{cm}^{-3}\cdot{}^{\circ}\text{C}^{-1}$ throughout profile. The set of eight soil nodes at depths of 0, 3, 10, 20, 30, 40, 50 and 60 cm was chosen with a number of factors in mind: 1) almost all roots occur in the first 60 cm; 2) variations occur very slowly at 60 cm; 3) caliche layer depth is about 60 cm (the water submodel uses these same nodes; 4) 10-cm increments are convenient to work with.

PROGRAM DESCRIPTION

Only the important segments of the code in the program listing are shown and described. Sequence numbers are shown to aid in reference to full code listing which follows the program description. All comment cards, specification statements and bookkeeping sections have been left out. Almost all initialization has been deleted also. Definitions of variable names may be found in Table B-1, which also appears at the beginning of the program listing.

Table B-1. Variable dictionary for HEAT

CHD(10)	DEPTH TO SOIL NODE, CM.
CHDX(10)	THICKNESS OF LAYER AROUND NODE, COUNTING FROM 2ND NODE, CM.
CHDXX(10)	DISTANCE BETWEEN ADJACENT NODES, CHDXX(I) = CHD(I+1) - CHD(I), CM.
DBGFLG	IF=.TRUE. WRITE DEBUGGING INFORMATION THIS TIME STEP
DEBUG1	NUMBER OF TIME STEPS BETWEEN DEBUGGING OUTPUTS
DT	=PMDT, LENGTH OF TIME STEP, DAY.
FTAVE(PMDT,N)	FUNCTION TO AVERAGE PREVIOUS N DAYS' AIR TEMPERATURES BY AVERAGING APPROPRIATE NUMBER OF PREVIOUS TIME STEP AVERAGE TEMPERATURES.
PHCVC(10)	SPECIFIC HEAT OF SOIL LAYER. (REMEMBER, 1ST LAYER IS CENTERED ON 2ND NODE.) CAL CM=3 C=1
PHK(10)	THERMAL CONDUCTIVITY OF SOIL BETWEEN NODES. (1ST VALUE IS FOR REGION BETWEEN NODES 1 AND 2). CAL CM=1 DAY=1 C=1.
PMDT	LENGTH OF TIME STEP, DAY.
PHJDAT	JULIAN DATE OF BEGINNING OF TIMESTEP.
PMN	NUMBER OF SOIL NODES.
THA(10)	THA(I) IS THE NEGATIVE OF THE COEFFICIENT OF THU(I+1) IN THE ITH EQUATION IN THE SET OF EQUATIONS TO SOLVE FOR THE THU ARRAY.
THB(10)	THB(I) IS THE COEFFICIENT OF THU(I) IN THE ITH EQUATION IN THE SET OF EQUATIONS TO SOLVE FOR THE THU ARRAY.
THC(10)	THC(I) IS THE NEGATIVE OF THE COEFFICIENT OF THU(I-1) IN THE ITH EQUATION IN THE SET OF EQUATIONS TO SOLVE FOR THE THU ARRAY.
THCCC(20)	AN ARRAY USED TO READ AND WRITE COMMENTS.
THD(10)	THD(I) IS THE CONSTANT, RIGHT HAND SIDE OF THE ITH EQUATION IN THE SET OF EQUATIONS TO SOLVE FOR THE THU ARRAY.
THM	AN INTEGER EQUAL TO THE LARGEST WHOLE NUMBER OF TIMESTEPS IN 30 DAYS.
THMR	A REAL VARIABLE EQUAL TO THM.
HTA(10)	TEMPERATURE OF SOIL NODES AT BEGINNING OF TIMESTEP, DEGREES C.
HTB(10)	TEMPERATURE OF SOIL NODES AT END OF TIMESTEP, DEGREES C.
HTHAC(10)	TEMPORARY ARRAY USED IN CALCULATING MATRIX ELEMENTS IN CALL TO TRI-DIAGONAL MATRIX SUBROUTINE.
HTHB(10)	ANOTHER TEMPORARILY USED ARRAY FOR CALCULATING MATRIX ELEMENTS IN CALL TO TRI-DIAGONAL MATRIX SUBROUTINE.
THUC(10)	THIS ARRAY CONTAINS THE TEMPERATURES OF THE INNER NODES (2 THROUGH PMN-1) AT THE END OF PMDT. THESE TEMPERATURES ARE THE SOLUTIONS OBTAINED BY THE TRI-DIAGONAL MATRIX SUBROUTINE.
TIME	TIME AT START OF TIMESTEP. EQUALS TSTART PLUS (NUMBER OF TIMESTEPS) * PMDT
TSTART	JULIAN DATE OF BEGINNING OF SIMULATION
XHSOLYT(10)	AVERAGE TEMPERATURE OF SOIL NODE DURING PMDT, DEGREES C.
ZAIRT	AVERAGE AIR TEMPERATURE FOR PRESENT TIMESTEP, DETERMINED BY PSHG, DEGREES C.
ZHAIRT(31)	HOLDS THM PRESENT AND PAST TIME STEP AVERAGE AIR TEMPERATURES. ZHAIRT(1) HOLDS PRESENT TIME STEP TEMP. ZHAIRT(2) HOLDS PREVIOUS TIME STEP TEMP, ETC.

17 THTB(1) = ZAIRT

HEAT 195

Assume surface temperature equals average air temperature for time-step.

```
NTHM=THM+1
18 ZHAIRT(NTHM)=ZHAIRT(NTHM-1)
NTHM=NTHM-1
IF(NTHM .GE. 2) GO TO 18
ZHAIRT(1)=ZAIRT
```

HEAT 200
HEAT 201
HEAT 202
HEAT 203
HEAT 204

Variable NTHM is essentially a DO loop index which decreases by one each time (Burroughs FORTRAN doesn't accept negative DO loop increments). This loop shifts temperature in ZHAIRT, dropping the oldest time-step temperature from ZHAIRT (THM + 1) and loading present temperature in ZHAIRT (1).

THTB(PMN)=FTAVE(PMDT,30)

HEAT 208

Set the temperature of the bottom node equal to the average temperature of the previous 30 days. Accomplish this using function FTAVE.

```
28 DO 30 I= 1, PMN-2
30 THD(I) = THA(I) * THTHAC(I) + THA(I+1) *
   * (THTHAC(I) - THA(I) - THA(I+1)) + THA(I+2) * THTHAC(I+1)
   THD(1) = THD(1) + THTB(1) * THTHAC(1)
   THD(PMN-2) = THD(PMN-2) + THTB(PMN) * THTHAC(PMN-1)
```

HEAT 223
HEAT 224
HEAT 225
HEAT 228
HEAT 229

Calculate the right-hand sides of the PMN-2 difference equations. For details see "Derivation of Difference Equations."

CALL TDM(THA, THB, THC, THD, THU, PMN-2)

HEAT 239

TDM is the subroutine which solves PMN-2 equations for PMN-2 unknowns (temperatures at nodes 2 through PMN-1). The equations are of the form:

$$- C_i U_{i-1} + B_i U_i - A_i U_{i+1} = D.$$

The U 's (or THU's) are the temperatures determined by TDM and returned to HEAT. For more information see the detailed program description of subroutine TDM.

```
DO 32 I=1,PMN-2
32 THTB(I+1) = THU(I)
```

HEAT 246
HEAT 247

Load THU array, just determined by TDM, into the appropriate places in the THTB array.

```
DO 34 I=1,PMN
34 XHSOLT(I) = (THA(I) + THTB(I)) / 2.
```

HEAT 250
HEAT 251

Make XHSOLT the average temperature at the soil nodes during PMDT.

ENTRY HINIT

HEAT 274

HEAT INITIALIZATION SECTION

Initial data are read in and written here. Also, calculations which need to be done only once each run are done here.

```
READ(5,80)THCCC
WRITE(6,81)
WRITE(6,82)THCCC
```

```
HEAT 281
HEAT 282
HEAT 283
```

First, a comment card is read (THCC is used only to read and write comments). This card is intended to be a general comment about HEAT, e.g., INITIALIZATION DATA FOR HEAT. Then come four spaces and this comment is written.

```
READ(5,80)THCCC
WRITE(6,82)THCCC
READ(5,1)CHD
WRITE(6,84)CHD
```

```
HEAT 285
HEAT 286
HEAT 287
HEAT 288
```

Another comment card is read and written, saying something about CHD (the depths of the nodes). The last characters on the card are the dimensions of the variable. Then values of the variable CHD, dimensioned 10, are read in and written.

An analogous procedure is then followed for reading in CHDX, PHCV, PHK, XHSOLT and ZHAIRT.

```
READ(5,80)THCCC
WRITE(6,82)THCCC
```

```
HEAT 317
HEAT 318
```

Finally, a comment is read and written, which says END READING INITIAL VALUES FOR HEAT.

```
DO 110 I=1,PMN-1
110 CHDXX(I)=CHD(I+1)-CHD(I)
```

```
HEAT 328
HEAT 329
```

This array is simply the distances between adjacent soil nodes.

```
THM=30. / PMDT
```

```
HEAT 338
```

THM is an integer equal to the largest whole number of time-steps in 30 days.

```
DO 140 I=1,PMN-1
THTHAC(I)=PHK(I) / CHDXX(I)
140 THTHB(I)=2.*PHCV(I)*CHDX(I) / PMDT
DO 160 I=1,PMN-2
THA(I) = THTHAC(I+1)
THB(I) = THTHB(I) + THTHAC(I) + THTHAC(I+1)
160 THC(I)=THTHAC(I)
THA(PMN-2)=0.
THC(I) = 0.
```

```
HEAT 342
HEAT 343
HEAT 344
HEAT 347
HEAT 348
HEAT 349
HEAT 350
HEAT 351
HEAT 352
```

These calculations load arrays THA, THB and THC for use when the tridiagonal matrix subroutine (TDM) is called. Since there is no water dependence on specific heat or thermal conductivity, these arrays do not change during the run and can be calculated just once. For details see "Derivation of Difference Equations."

COMPLETE PROGRAM LISTING

```

SSET SEPARATE          HEAT 001
SSET DWN              HEAT 002
C
C   SUBROUTINE HEAT
C
C   SOIL HEAT PROFILE SUBMODEL OF DESERT BIOME WATER RESPONSE MODEL    HEAT 003
C   MARCH 1976.  WRITTEN BY: PAUL H. LORREN                                HEAT 004
C                                         ECOLOGY CENTER, UMC 52                         HEAT 005
C                                         UTAH STATE UNIVERSITY                           HEAT 006
C                                         LOGAN, UTAH 84322                            HEAT 007
C
C   VARIABLE DICTIONARY FOR HEAT
C
C   CHD(10)      DEPTH TO SOIL NODE, CM.                                     HEAT 008
C   CHDX(10)      THICKNESS OF LAYER AROUND NODE, COUNTING FROM 2ND      HEAT 009
C                   NODE, CM.                                              HEAT 010
C
C   CHDXX(10)     DISTANCE BETWEEN ADJACENT NODES, CHDXX(I) = CHD(I+1) - HEAT 011
C                   CHD(I), CM.                                         HEAT 012
C
C   DBGFLG       TF=.TRUE. WRITE DEBUGGING INFORMATION THIS TIME STEP HEAT 013
C
C   DEBUG1       NUMBER OF TIME STEPS BETWEEN DEBUGGING OUTPUTS           HEAT 014
C
C   DT           =PHDT, LENGTH OF TIME STEP, DAY.                          HEAT 015
C
C   FTAVE(PHDT,N) FUNCTION TO AVERAGE PREVIOUS N DAYS' AIR TEMPERATURESHEAT 016
C   BY AVERAGING APPROPRIATE NUMBER OF PREVIOUS TIME STEP AVERAGE TEMPERATURES. HEAT 017
C
C   PHCV(10)      SPECIFIC HEAT OF SOIL LAYER, (REMEMBER, 1ST LAYER IS CENTERED ON 2ND NODE.) CAL CR=3 C=1 HEAT 018
C
C   PHK(10)       THERMAL CONDUCTIVITY OF SOIL BETWEEN NODES, (1ST VALUE IS FOR REGION BETWEEN NODES 1 AND 2), CAL CM=1 DAY=1 C=1 HEAT 019
C
C   PHDT         LENGTH OF TIME STEP, DAY.                               HEAT 020
C
C   PHJDAT       JULIAN DATE OF BEGINNING OF TIMESTEP.                  HEAT 021
C
C   PHN          NUMBER OF SOIL NODES.                                    HEAT 022
C
C   THA(10)       THA(I) IS THE NEGATIVE OF THE COEFFICIENT OF THU(I+1) IN THE ITH EQUATION IN THE SET OF EQUATIONS TO SOLVE FOR THE THU ARRAY. HEAT 023
C
C   THB(10)       THB(I) IS THE COEFFICIENT OF THU(I) IN THE ITH EQUATION IN THE SET OF EQUATIONS TO SOLVE FOR THE THU ARRAY.          HEAT 024
C
C   THC(10)       THC(I) IS THE NEGATIVE OF THE COEFFICIENT OF THU(I-1) IN THE ITH EQUATION IN THE SET OF EQUATIONS TO SOLVE FOR THE THU ARRAY.          HEAT 025
C
C   THCCC(20)     AN ARRAY USED TO READ AND WRITE COMMENTS.             HEAT 026
C
C   THD(10)       THD(I) IS THE CONSTANT, RIGHT HAND SIDE OF THE ITH EQUATION IN THE SET OF EQUATIONS TO SOLVE FOR THE THU ARRAY.          HEAT 027
C
C   THM          AN INTEGER EQUAL TO THE LARGEST WHOLE NUMBER OF TIMESTEPS IN 30 DAYS.          HEAT 028
C
C   THMR         A REAL VARIABLE EQUAL TO THM.                           HEAT 029
C
C   THTAC(10)     TEMPERATURE OF SOIL NODES AT BEGINNING OF TIMESTEP, DEGREES C.          HEAT 030
C
C   THTB(10)     TEMPERATURE OF SOIL NODES AT END OF TIMESTEP, DEGREES C.          HEAT 031
C
C   THTHAC(10)    TEMPORARY ARRAY USED IN CALCULATING MATRIX ELEMENTS IN CALL TO TRI-DIAGONAL MATRIX SUBROUTINE.          HEAT 032
C
C   THTHB(10)    ANOTHER TEMPORARILY USED ARRAY FOR CALCULATING MATRIX ELEMENTS IN CALL TO TRI-DIAGONAL MATRIX SUBROUTINE.          HEAT 033
C
C   THU(10)       THIS ARRAY CONTAINS THE TEMPERATURES OF THE INNER NODES (2 THROUGH PHN-1) AT THE END OF PHDT. THESE TEMPERATURES ARE THE SOLUTIONS OBTAINED BY THE TRI-DIAGONAL MATRIX SUBROUTINE.          HEAT 034
C

```

```

C TIME TIME AT START OF TIMESTEP. EQUALS TSTART PLUS HEAT 091
C (NUMBER OF TIMESTEPS) * PHOT HEAT 092
C
C TSTART JULIAN DATE OF BEGINNING OF SIMULATION HEAT 093
C
C XHSOLT(10) AVERAGE TEMPERATURE OF SOIL NODE DURING PHOT, HEAT 094
C DEGREES C. HEAT 095
C
C ZAIRT AVERAGE AIR TEMPERATURE FOR PRESENT TIMESTEP. HEAT 096
C DETERMINED BY PSHGP, DEGREES C. HEAT 097
C
C ZHAIRT(31) HOLDS THM PRESENT AND PAST TIME STEP AVERAGE AIR HEAT 098
C TEMPERATURES. ZHAIRT(1) HOLDS PRESENT TIME STEP HEAT 099
C TEMP. ZHAIRT(2) HOLDS PREVIOUS TIME STEP TEMP, ETC. HEAT 100
C
C
C
C BRIEF DESCRIPTION AND MAIN ASSUMPTIONS HEAT 101
C
C ONE. FOR SOIL SURFACE TEMPERATURE I'LL USE THE MEAN DAILY TEMPERATURE HEAT 102
C OR HAVE A MEASURED OR SIMULATED TEMPERATURE READ IN. IF DESIRED AN HEAT 103
C ENERGY BALANCE APPROACH MIGHT BE BETTER, ALTHOUGH R. J. HANKS HEAT 104
C THOUGHT THAT WOULD BE PRETTY HAIRY AND HENCE PROBABLY NOT WORTHWHILE HEAT 105
C FOR US (REF. H.A. BECKMAN, J.W. MITCHELL, AND W.P. PORTER, 1973). HEAT 106
C THERMAL MODEL FOR PREDICTION OF A DESERT IGUANA'S DAILY AND SEASONAL HEAT 107
C BEHAVIOR, TRANS. ASME, SERIES C 95, 257-262.) HEAT 108
C
C TWO. FOR THERMAL DIFFUSIVITY I'LL ASSUME IT'S INDEPENDENT OF WATER HEAT 109
C CONTENT. BOTH HEAT CONDUCTIVITY AND HEAT CAPACITY HAVE A DEPENDENCE HEAT 110
C ON WATER CONTENT BUT DIFFUSIVITY, THEIR RATIO HAS ONLY A WEAK WATER HEAT 111
C DEPENDENCE (R. J. HANKS, PERSONAL COMMUNICATIONS 5-24-74). HEAT 112
C IF DESIRED WE CAN INCLUDE WATER AS IN R.J. HANKS, D.D. AUSTIN, HEAT 113
C AND H.T. ONDRECHEN, 1971, SOIL TEMPERATURE ESTIMATION BY A NUMERICAL HEAT 114
C METHOD. SOIL SCI. SOC. AM. PROC. 35, 665. THEY GIVE A HEAT 115
C SIMPLE RELATIONSHIP BETWEEN HEAT CAPACITY AND WATER CONTENT. HEAT 116
C FOR HEAT CONDUCTIVITY THEY USE METHOD OF DE VRIES, D.A., 1963, HEAT 117
C THERMAL PROPERTIES OF SOILS, CHAPTER 7 IN PHYSICS OF PLANT HEAT 118
C ENVIRONMENT, ED. BY VAN WIJK, JOHN WILEY AND SONS, INC., NEW YORK. HEAT 119
C
C THREE. FOR THE BOTTOM BOUNDARY CONDITION, I'LL SAY FOR NOW THAT THE HEAT 120
C SOIL TEMPERATURE AT 60 CM EQUALS THE MEAN MONTHLY AIR TEMPERATURE AT HEAT 121
C 2M (MITCHELL ET AL., OP. CIT., AND DE VRIES, OP. CIT.). HEAT 122
C
C THE PROGRAM IS TAKEN PRETTY MUCH FROM R.J. HANKS, D.D. AUSTIN, HEAT 123
C AND H.T. ONDRECHEN, 1971, SOIL TEMPERATURE ESTIMATION BY A NUMERICAL HEAT 124
C METHOD. SOIL SCI. SOC. AM. PROC. 35, 665. HEAT 125
C OCCASIONAL INSPIRATION IS TAKEN FROM HANKS, R.J., AND S.A. HEAT 126
C BOWERS, 1962, NUMERICAL SOLUTION OF THE MOISTURE FLOW EQUATION FOR HEAT 127
C INFILTRATION IN LAYERED SOILS. SOIL SCI. SOC. AMER. PROC. 26, 530-534 HEAT 128
C THE FINAL PRODUCT IS CONCEPTUALLY ALMOST THE SAME AS THE TEMPERATURE HEAT 129
C SECTION OF R.A. GRIFFIN, R.J. HANKS, AND S. CHILDS, 1973, MODEL HEAT 130
C FOR ESTIMATING WATER, SALT, AND TEMPERATURE DISTRIBUTION IN THE SOIL HEAT 131
C PROFILE, US/IBP DESERT BIOME PROGRAM PUBLICATION USU, LOGAN, UTAH. HEAT 132
C
C THIS ROUTINE MUST BE CALLED AFTER THE WATER SUBROUTINE IF A THETA HEAT 133
C DEPENDENCE ON DIFFUSIVITY IS TO BE INCLUDED. HEAT 134
C THIS DEPENDENCE IS NOT NOW INCLUDED. HEAT 135
C
C FOR NOW THE TEMPERATURE OF THE WATER MOVING BETWEEN LAYERS HEAT 136
C IS NOT CONSIDERED IN THE TEMPERATURE OF THE LAYER. NO VAPORIZATION HEAT 137
C OR CONDENSATION EFFECTS ARE INCLUDED EITHER. HEAT 138
C
C
C COMMON TIME,TSTART,TEND,DT,DTPR,DTPL, HEAT 139
C 1CAARC(6,8),CADEFST(6,8),CADETH,CAUNST,CHDX(10),CHDXX(10), HEAT 140
C 2CNFIX,CNSDF,CNSDF,CNSDF,CNSOHS,CNSUP,CVDETH(12,4),CVLTFR(11,4), HEAT 141
C 3CPHEM(6,8),CPHSE(6),CVRDST(6,10),CVTSPRC(6,8),CHINF,CHPSI(10), HEAT 142
C 4PHOT,PHOTPL,P4DTPR,PMFGPS,PMJDAT,PHN,PNNCOR,PHNSP, HEAT 143
C 5XA(4,3),XAHT(4,8),XAHT(4),XAFTS(4),XAFT(4),XANUMB(4,8), HEAT 144
C 6XASAC(4),XASANT(4),XAYHG(4),XAYHT(4),XHSOLTE(10),XMMN,XNSOMF,XNSOHS,HEAT 145
C 7XPAB5,XPLBP,XPPD4,XVFG(6,5),XVLITR(12,4),XVPLNT(6,6),XVTOTL, HEAT 146
C 8XHTHT(10),XNSTND,ZAIRT,ZEVAP,ZESUN,ZPHPD,ZRAIN,ZRSUM,ZRH,ZRINT, HEAT 147
C 9ZRISUM,ZSUN,ZTHMAX,ZTHIN,ZWIND,COOL(12,4) HEAT 148
C
C COMMON/DB/DEBUG1,DEBUG2,DEBUG3 HEAT 149
C
C FT IS IN COMMON WITH FTAVE HEAT 150
C COMMON/FT/ZHATRT(31) HEAT 151
C
C INTEGER PMN, THM HEAT 152
C
C LOGICAL DBGFLG HEAT 153
C
C DIMENSION PHCV(10), PHK(10), THTAC(10), THTB(10), THA(10), HEAT 154
C

```



```

C ENTRY HINIT
C
C IN THIS SECTION ARE THE READING AND WRITING OF INPUT TO THIS
C SUBROUTINE AND CALCULATIONS WHICH ARE TO BE DONE ONLY ONCE.
C
C READ AND WRITE INPUT DATA
C VARIABLE THCCC IS FOR READING AND WRITING COMMENTS
  READ(5,80)THCCC
  WRITE(6,81)
  WRITE(6,82)THCCC

C
  READ(5,80)THCCC
  WRITE(6,82)THCCC
  READ(5,/)CHD0
  WRITE(6,84)CHD0

C
  READ(5,80)THCCC
  WRITE(6,82)THCCC
  READ(5,/)CHDX
  WRITE(6,84)CHDX

C
  READ(5,80)THCCC
  WRITE(6,82)THCCC
  READ(5,/)PHCV
  WRITE(6,84)PHCV

C
  READ(5,80)THCCC
  WRITE(6,82)THCCC
  READ(5,/)PHK
  WRITE(6,84)PHK

C
  READ(5,80)THCCC
  WRITE(6,82)THCCC
  READ(5,/)XHSOLT
  WRITE(6,84)XHSOLT

C READ IN ZHAIRT FOR PREVIOUS 30 DAYS OF AIR TEMPERATURES
C THESE TEMPS ARE TIME STEP AVERAGES NOT NECESSARILY DAILY TEMPS
  READ(5,80)THDTC
  WRITE(6,82)THCCC
  READ(5,/)ZHAIRT
  WRITE(6,84)ZHAIRT

C
  READ(5,80)THCCC
  WRITE(6,82)THCCC
  WRITE(6,81)

C
  80 FORMAT(20A4)
  81 FORMAT(//++)
  82 FORMAT('0',20E16)
  84 FORMAT(' ', 10E12.4,+/)

C NOW DO THE DELTA-X CALCULATIONS
  DO 110 I=1,PMN-1
  110 CHOXX(I)=CHOC(I+1)-CHOC(I)
C END DELTA-X CALCULATIONS
C
  DO 120 I=1,PMN
  THTA(I)=XHSOLT(I)
  120 THTB(I)=XHSOLT(I)

C THM IS THE CLOSEST INTEGER TO THE NO. OF TIME STEPS IN 30 DAYS
  THM=30. / PMT
C SINCE NO THETA DEPENDENCE ON CV OR K INCLUDED, THESE
C CALCULATIONS HAVE TO BE MADE ONLY ONCE
  DO 140 I=1,PMN-1
    THTHAC(I)=PHCK(I) / CHOXX(I)
  140 THTHBC(I)=2.*PHCV(I)+CHODX(I) / PMOT

C PHCV(PMN-1) AND CHODX(PMN-1) ARE NOT USED SO CAN JUST LOAD ZEROES IN
  DO 160 I=1,PMN-2
    THAC(I) = THTHAC(I+1)
    THOC(I) = THTHBC(I) + THTHAC(I) + THTHAC(I+1)
  160 THOC(I)=THTHAC(I)
    THAC(PMN-2)=0.
    THOC(1) = 0.

C END OF EQUATIONS WHICH CAN BE CALCULATED ONLY ONCE IF NO THETA
C DEPENDENCE IS INCLUDED IN CV OR K
C
C
C RETURN
END

```

DERIVATION OF DIFFERENCE EQUATIONS

As mentioned in the general description of HEAT, the temperature profile is determined by the solution of Equation B-1:

$$\frac{\partial T}{\partial t} = \frac{\partial}{\partial z} (\sigma \frac{\partial T}{\partial z}). \quad (B-1)$$

where

- T = the soil temperature at a given point at a given instant of time, $^{\circ}\text{C}$;
- t = time, day;
- z = depth in soil, cm;
- σ = soil thermal diffusivity (the ratio of thermal conductivity, $\text{cal}\cdot\text{cm}^{-1}\cdot\text{day}^{-1}\cdot{}^{\circ}\text{C}^{-1}$, to specific heat, $\text{cal}\cdot\text{cm}^{-3}\cdot{}^{\circ}\text{C}^{-1}$), cm^2/day .

The difference equations are derived as follows:

for a thin layer of soil during a time interval Δt ,

$$(\text{heat in}) - (\text{heat out}) = (\text{heat stored}). \quad (B-2)$$

In particular, for layer i during Δt ,

$$(\text{heat in})_i = - (K \frac{\partial T}{\partial z}) \text{ at top of layer } i, \quad (B-3)$$

where

counting of layers starts at the soil surface and goes down; heat flowing down is positive:

$(\text{heat in})_i$ in Equation B-3 has units of $\text{cal}\cdot\text{cm}^{-2}\cdot\text{day}^{-1}$;

- K = soil thermal conductivity, $\text{cal}\cdot\text{cm}^{-1}\cdot\text{day}^{-1}\cdot{}^{\circ}\text{C}^{-1}$;
- T = temperature of layer i , $^{\circ}\text{C}$;
- z = depth in soil, cm.

Flesh out Equation B-3,

$$(\text{heat in})_i = (-K_{i-1/2}) \left\{ \left[\frac{T_i - T_{i-1}}{\Delta z_{i-1/2}} + \frac{T_i^* - T_{i-1}^*}{\Delta z_{i-1/2}} \right] \left(\frac{1}{2} \right) \right\}, \quad (B-4)$$

where

- T_i = temperature of layer i at beginning of Δt , assumed located at the center of a layer, called a node. The first node is at the soil surface at 0-cm depth. The second is at 3-cm depth (at Curlew Valley) and is at the center of layer 1, which extends from 1- to 5-cm depth. Node 3 at Curlew is at 10-cm depth and is at the center of layer 2, which extends from 5- to 15-cm depth, etc. The bottom layer is centered on the next to the bottom node. There are PMN nodes

and, hence, PMN—2 layers. These distinctions between nodes, layers, regions between nodes, etc., appear confusing but must be made in using the difference equations;

- T_{i-1} = temperature of layer $i-1$ at beginning of Δt ;
- T_i^* = temperature of layer i at end of Δt ;
- T_{i-1}^* = temperature of layer $i-1$ at end of Δt ;
- $K_{i-1/2}$ = conductivity in region between centers of layers $i-1$ and i (i.e., between nodes i and $i+1$);
- $\Delta z_{i-1/2}$ = distance from center of layer $i-1$ to center of layer i (i.e., from node i to $i+1$).

The quantity in braces is the temperature gradient determined by the Crank-Nicholson scheme (Richtmyer 1957) and is the average of the temperature gradients at the beginning and end of Δt .

By similar reasoning:

$$\begin{aligned} (\text{heat out})_i &= - (K \frac{\partial T}{\partial z}) \text{ at bottom of layer } i, \\ &= - (K_{i+1/2}) \left\{ \left[\frac{T_{i+1} - T_i}{\Delta z_{i+1/2}} + \frac{T_{i+1}^* - T_i^*}{\Delta z_{i+1/2}} \right] \left(\frac{1}{2} \right) \right\}. \end{aligned} \quad (B-5)$$

The heat stored in $\text{cal}\cdot\text{cm}^{-2}\cdot\text{day}^{-1}$

$$= \frac{(Cv_i)(\Delta x_i)}{\Delta t} (T_i^* - T_i), \quad (B-6)$$

where

- Cv_i = specific heat of layer i , $\text{cal}\cdot\text{cm}^{-3}\cdot{}^{\circ}\text{C}^{-1}$;
- Δx_i = thickness of layer i , cm;
- Δt = length of time-step, day.

By substituting Equations B-4, B-5 and B-6 in Equation B-2 we get:

$$\begin{aligned} &- K_{i-1/2} \left[\frac{T_i - T_{i-1} + T_i^* - T_{i-1}^*}{\Delta z_{i-1/2}} \right] \\ &+ \frac{K_{i+1/2}}{2} \left[\frac{T_{i+1} - T_i + T_{i+1}^* - T_i^*}{\Delta z_{i+1/2}} \right] \\ &= \frac{Cv_i \Delta x_i}{\Delta t} (T_i^* - T_i). \end{aligned} \quad (B-7)$$

Multiply through by two and collect T^* terms on the left. After two lines of algebra we get:

$$-C_i T_{i-1}^* + B_i T_i^* - A_i T_{i+1}^* = D_i , \quad (B-8)$$

where

$$C_i = \frac{K_{i-1/2}}{\Delta z_{i-1/2}} , \quad (B-9)$$

$$B_i = \frac{K_{i-1/2}}{\Delta t_{i-1/2}} + \frac{K_{i+1/2}}{\Delta z_{i+1/2}} + \frac{2Cv_i \Delta x_i}{\Delta t} , \quad (B-10)$$

$$A_i = \frac{K_{i+1/2}}{\Delta z_{i+1/2}} , \quad (B-11)$$

$$D_i = T_{i-1} \left(\frac{K_{i-1/2}}{\Delta z_{i-1/2}} \right) + T_i \left[\frac{2Cv_i \Delta x_i}{\Delta t} - \frac{K_{i-1/2}}{\Delta z_{i-1/2}} - \frac{K_{i+1/2}}{\Delta z_{i+1/2}} \right] + T_{i+1} \left(\frac{K_{i+1/2}}{\Delta z_{i+1/2}} \right) . \quad (B-12)$$

For top and bottom layers we must make small changes in Equations B-8 to 12 because boundary condition must be included. The temperature at the surface at the end of the time-step is set equal to the average air temperature during Δt :

$$T_s^* = \text{ZAIRT} . \quad (B-13)$$

The temperature at the bottom node T_B^* (there are PMN nodes) at the end of Δt is set equal to the average air temperature during the previous 30 days.

For the top layer then, $(\text{heat in})_1$ contains only one unknown temperature, not two as shown in Equation B-4.

That is

$$(\text{heat in})_1 = -\langle K_{1/2} \rangle \left[\frac{T_1 - T_s}{\Delta z_{1/2}} - \frac{T_1^* - T_s^*}{\Delta z_{1/2}} \right] \left(\frac{1}{2} \right) . \quad (B-14)$$

In Equation B-14, only T_1^* , the temperature of layer 1 (i.e., node 2) is unknown. Equations B-5 and 6 for the top layer with $i=1$ are unchanged. Substituting Equations B-14, 5 and 6 in Equation B-2 now yields by the same procedure as before:

$$B_1 T_1^* - A_1 T_2^* = D_1 \quad (B-15)$$

where

$$B_1 = \frac{K_{1/2}}{\Delta z_{1/2}} + \frac{K_{3/2}}{\Delta z_{3/2}} + \frac{2Cv_1 \Delta x_1}{\Delta t} , \quad (B-16)$$

$$A_1 = \frac{K_{3/2}}{\Delta z_{3/2}} , \quad (B-17)$$

$$D_1 = T_s \frac{K_{1/2}}{\Delta z_{1/2}} + T_1 \left[\frac{2Cv_1 \Delta x_1}{\Delta t} - \frac{K_{1/2}}{\Delta z_{1/2}} - \frac{K_{3/2}}{\Delta z_{3/2}} \right] + T_2 \frac{K_{3/2}}{\Delta z_{3/2}} + T_s^* \frac{K_{1/2}}{\Delta z_{1/2}} . \quad (B-18)$$

For the bottom layer, $(\text{heat out})_{\text{bottom}}$ contains only one unknown temperature. After several lines of algebra we then get (say the bottom layer is layer number M):

$$-C_m T_{m-1}^* + B_m T_m^* = D_m , \quad (B-19)$$

where

$$C_m = \frac{K_{m-1/2}}{\Delta z_{m-1/2}} , \quad (B-20)$$

$$B_m = \frac{K_{m-1/2}}{\Delta z_{m-1/2}} + \frac{K_{m+1/2}}{\Delta z_{m+1/2}} + \frac{2Cv_m \Delta x_m}{\Delta t} , \quad (B-21)$$

$$D_m = T_{m-1} \left(\frac{K_{m-1/2}}{\Delta z_{m-1/2}} \right) + T_m \left[\frac{2Cv_m \Delta x_m}{\Delta t} - \frac{K_{m-1/2}}{\Delta z_{m-1/2}} - \frac{K_{m+1/2}}{\Delta z_{m+1/2}} \right] + T_B \left(\frac{K_{m+1/2}}{\Delta z_{m+1/2}} \right) + T_B^* \left(\frac{K_{m+1/2}}{\Delta z_{m+1/2}} \right) . \quad (B-22)$$

Now summarize these equations for A , B , C and D .

$$A_i = \frac{K_{i+1/2}}{\Delta z_{i+1/2}} \quad \text{for } i = 1 \text{ to PMN} - 3 , \quad (B-23)$$

$$B_i = \frac{K_{i-1/2}}{\Delta z_{i-1/2}} + \frac{K_{i+1/2}}{\Delta z_{i+1/2}} + \frac{2Cv_i \Delta x_i}{\Delta t} \quad \text{for } i = 1 \text{ to PMN} - 2 , \quad (B-24)$$

$$C_i = 0 \quad \text{for } i = 1 ,$$

$$= \frac{K_{i-1/2}}{\Delta z_{i-1/2}} \quad \text{for } i = 2 \text{ to PMN} - 2 , \quad (B-25)$$

$$\begin{aligned}
 D_i &= T_s \frac{K_{1/2}}{\Delta z_{1/2}} + T_1 \left[\frac{2C_{v1} \Delta x_1}{\Delta t} - \frac{K_{1/2}}{\Delta z_{1/2}} - \frac{K_{3/2}}{\Delta z_{3/2}} \right] \\
 &\quad + T_2 \frac{K_{3/2}}{\Delta z_{3/2}} + T_s^* \frac{K_{1/2}}{\Delta z_{1/2}} \\
 &\quad \text{for } i = 1, \\
 &= T_{i-1} \frac{K_{i-1/2}}{\Delta z_{i-1/2}} + T_i \left[\frac{2C_{vi} \Delta x_i}{\Delta t} - \frac{K_{i-1/2}}{\Delta z_{i-1/2}} \right. \\
 &\quad \left. - \frac{K_{i+1/2}}{\Delta z_{i+1/2}} \right] + T_{i+1} \frac{K_{i+1/2}}{\Delta z_{i+1/2}} \\
 &\quad \text{for } i = 2 \text{ to } PMN - 3, \\
 &= T_{i-1} \frac{K_{i-1/2}}{\Delta z_{i-1/2}} + T_i \left[\frac{2C_{vi} \Delta x_i}{\Delta t} - \frac{K_{i-1/2}}{\Delta z_{i-1/2}} \right. \\
 &\quad \left. - \frac{K_{i+1/2}}{\Delta z_{i+1/2}} \right] + T_B \frac{K_{i+1/2}}{\Delta z_{i+1/2}} + T_B^* \frac{K_{i+1/2}}{\Delta z_{i+1/2}} \\
 &\quad \text{for } i = PMN - 2. \tag{B-26}
 \end{aligned}$$

It can easily be seen in Equations B-23, 24 and 25 that there are no temperatures involved. Also, the conductivity, K , and specific heat, C_v , are not dependent on water content or temperature. (A water content dependence can be included if it is felt such detail is warranted. See Hanks et al. 1971). Thus, the A 's, B 's and C 's need to be calculated only once. The D 's must be calculated each time-step.

Transform Equations B-23, 24, 25 and 26 into computer code:

- a. Thermal conductivity $K_{1/2}$ becomes $PHK(1)$
 $K_{3/2}$ becomes $PHK(2)$
 \vdots
 $K_{PMN-2+1/2}$ becomes
 $PHK(PMN-1)$
- b. Specific heat Cv_i becomes $PHCV(I)$ for $I = 1$ to $PMN-2$
- c. Distance from node to node $\Delta z_{1/2}$ becomes $CHDXX(1)$
 \vdots
 $\Delta z_{PMN-2+1/2}$ becomes
 $CHDXX(PMN-1)$
- d. Thickness of layer Δx_i becomes $CHDX(I)$ for $I = 1$ to $PMN-2$

e. Temperatures at beginning of time-step
 T_i becomes $THTA(I+1)$ for $I = 1$ to $PMN-2$
 T_s becomes $THTA(1)$
 T_B becomes $THTA(PMN)$

f. Temperatures at end of time-step
 T_s^* becomes $THTB(1)$
 T_B^* becomes $THTB(PMN)$

g. Time-step length Δt becomes $PMDT$

h. Tridiagonal matrix elements
 A_i, B_i, C_i, D_i become
 $THA(I), THB(I), THC(I),$
 $THD(I)$ for $I = 1, PMN-2$.

Now, if we define temporary variables $THTHA(I) = PHK(I)/CHDXX(I)$ and $THTHB(I) = 2 * PHCV(I) * CHDX(I)/PMDT$, then Equation B-23 becomes

$$\begin{aligned}
 THA(I) &= THTHA(I+1) && \text{for } I = 1 \text{ to } PMN - 3, \\
 &= 0 && \text{for } I = PMN - 2,
 \end{aligned}$$

Equation B-24 becomes

$$\begin{aligned}
 THC(I) &= 0 && \text{for } I = 1, \\
 &= THTHA(I) && \text{for } I = 2 \text{ to } PMN - 2,
 \end{aligned}$$

Equation B-25 becomes

$$\begin{aligned}
 THB(I) &= THTHA(I)+THTHA(I+1)+THTHB(I) \\
 &\quad \text{for } I = 1 \text{ to } PMN - 2,
 \end{aligned}$$

Equation B-26 becomes

$$\begin{aligned}
 THD(I) &= THTA(1)*THTHA(1)+THTA(2)*(THTHB(1)-THTHA(1) \\
 &\quad -THTHA(2))+THTA(3)*THTHA(2)+THTB(1)*THTHA(1) \\
 &\quad \text{for } I = 1, \\
 &= THTA(I)*THTHA(I)+THTA(I+1)*(THTHB(I)-THTHA(I) \\
 &\quad -THTHA(I+1))+THTA(I+2)*THTHA(I+1) \\
 &\quad \text{for } I = 2 \text{ to } PMN - 3, \\
 &= THTA(PMN-2)*THTHA(PMN-2)+THTA(PMN-1) \\
 &\quad *(THTHB(PMN-2)-THTHA(PMN-2)-THTHA(PMN-1)) \\
 &\quad +THTA(PMN)*THTHA(PMN-1)+THTB(PMN)*THTHA(PMN-1) \\
 &\quad \text{for } I = PMN - 2.
 \end{aligned}$$

As mentioned earlier, THA , THB and THC have no water content or temperature dependence and hence are calculated only once, in the initialization section. THD is dependent on temperature and hence is calculated each time-step.

LITERATURE CITED

- BECKMAN, W. A., J. W. MITCHELL, and W. P. PORTER. 1973. Thermal model for prediction of a desert iguana's daily and seasonal behavior. *Trans. ASME, Series C* 95: 257-262.
- GRIFFIN, R. A., R. J. HANKS, and S. CHILDS. 1974. Model for estimating water, salt and temperature distribution in the soil profile. *US/IBP Desert Biome Res. Memo.* 74-61. Utah State Univ., Logan. 12 pp.
- HANKS, R. J., D. D. AUSTIN, and W. T. ONDRECHEN. 1971. Soil temperature estimation by a numerical method. *Soil Sci. Soc. Amer. Proc.* 35:665-667.
- RICHTMYER, R. D. 1957. Difference methods for initial value problems. Interscience Publ., New York.

C. WATER
(including WBAL and WTIME)
P. W. Lommen

**GENERAL DESCRIPTION OF THE
WATER SUBMODEL**

In the Water Response Model, soil water potential is needed by the plant submodels in order to predict growth. This is provided by submodel WATER. Soil water potential also helps determine rates in nitrogen and decomposition submodels. Inputs required each time-step are precipitation, evaporation and transpiration. Soil parameters needed once are: 1) relation between soil water potential and soil water content (θ); 2) relation between hydraulic conductivity and θ ; 3) wet and dry limits to soil water potential; 4) conductivity of caliche layer; 5) soil layer thicknesses and locations; 6) average runoff:runoff ratio per day; 7) largest permissible value of change in θ during water time-step (which is generally much smaller than overall model time-step); 8) initial values of θ and depth of water standing on surface.

Various papers (Hanks and Bowers 1962; Hanks et al. 1969; Nimah and Hanks 1973; Griffin et al. 1974) have provided ideas which have contributed to this effort.

A set of nodes is introduced in the soil profile (the same nodes as for submodel HEAT) as reference points for soil layers. Figure C-1 is a schematic diagram of submodel WATER. The soil water potential in soil layer i is the solution of Equation C-1:

$$\epsilon_i \left[\frac{\partial H}{\partial t} \right] = \left[\frac{\partial}{\partial z} \left(K \frac{\partial H}{\partial z} \right) \right] + A_i. \quad (\text{C-1})$$

A_i is the removal of water by roots in layer i (transpiration) and is proportional to water available in layer i and relative root amount in layer i .

The remainder of the equation is a standard diffusion equation: H is the soil water potential in layer i , bars; K is the soil hydraulic conductivity at layer i , $\text{cm}^2 \cdot \text{bar}^{-1} \cdot \text{day}^{-1}$; ϵ_i is the specific water capacity of layer i , bar^{-1} ; Z is soil depth, centimeters; t is time, days.

The upper boundary condition on Equation C-1 is determined by the surface flux of water which depends on evaporation, precipitation and precipitation intensity, and standing water. The bottom boundary condition is determined by the caliche layer conductivity and water content, both of which are read in with initial parameters.

A set of difference equations is then generated. It is solved by a tridiagonal matrix method of Richtmyer (1957). For more details, see "Derivation of Difference Equations" below, and Detailed Program Description of subroutine TDM in section D of this research memorandum.

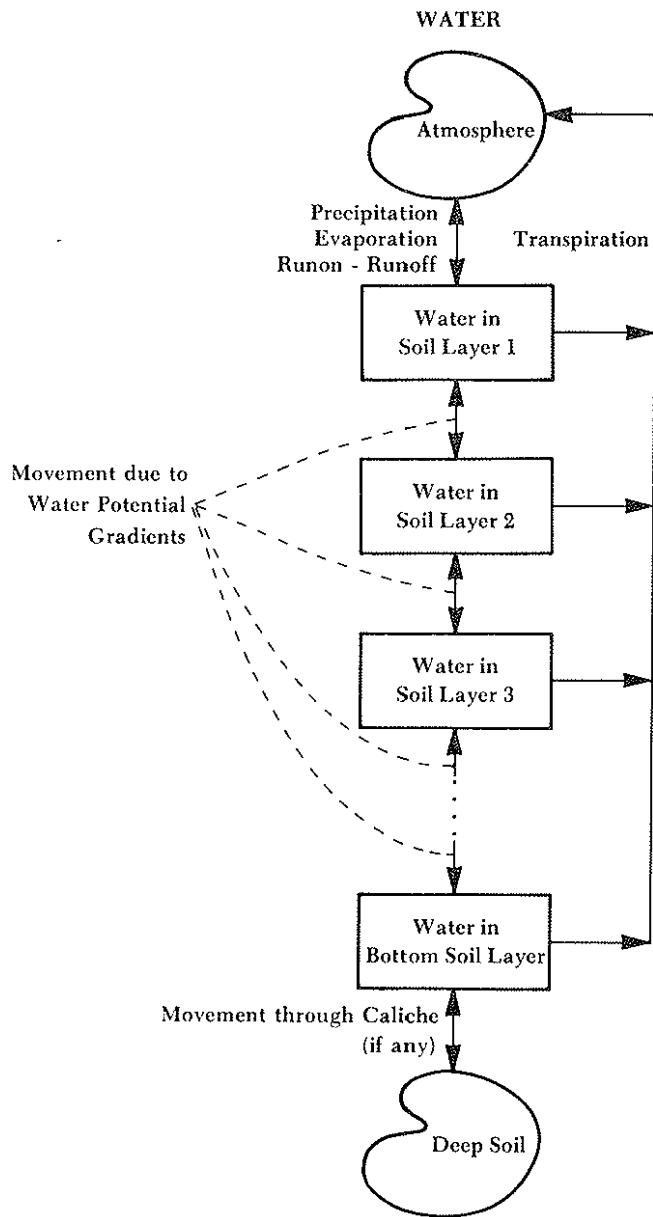


Figure C-1. Schematic diagram of submodel WATER.

PROGRAM DESCRIPTION

Only the important segments of the FORTRAN code are shown and described. Sequence numbers are shown to aid in reference to the full code listing that follows the program description. All comment cards, specification statements and bookkeeping sections have been deleted also. Definitions of variable names may be found in Table C-1, which also appears at the beginning of the program listing.

Before proceeding to the code, several additional comments should be made. First, volumetric water content of the soil, a dimensionless quantity (cm of water per cm of soil), is a very important and much-used variable throughout the program and will be called *theta* in the description. Similarly, soil water potential, measured in bars pressure, will be abbreviated SWP.

Second, water subdivides PMDT, the overall model

time-step (typically 4 days), as needed. If water is moving rapidly into the soil profile during a precipitation event, e.g., the WATER time-step, TWDT will be cut down to 30 min (the minimum allowed). WATER tries to find the largest TWDT consistent with the requirement that theta does not change more than PWTLIM (typically .015) during TWDT. We want TWDT large enough to be efficient but small enough to be accurate. There is a fair amount of code concerned with determining the best value of TWDT.

Third, in making difference equations from the main differential equation, it has been necessary to define nodes, layers and regions between nodes for the soil profile. This can be confusing. Figure C-2 shows how this was done for Curlew Valley. There are PMN nodes or reference points, PMN-1 regions between nodes and PMN-2 layers. Also shown in Figure C-2 are the variables which are indexed by layers, nodes and regions.

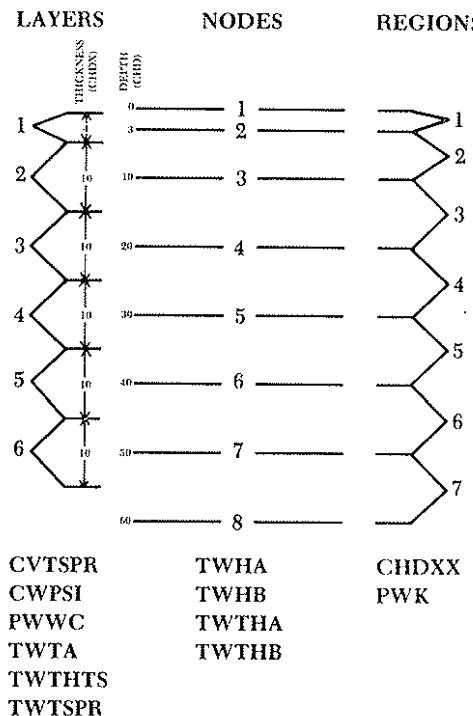


Figure C-2. Relations between layers, nodes and regions between nodes for the soil profile as used in Curlew Valley runs. The first layer is centered on the second node, etc. Also shown are layer width (CHDX) and node depth (CHD), both in centimeters. Finally, arrays indexed by layer are listed under column LAYERS, etc.

Table C-1. Variable dictionary for WATER

LIST OF VARIABLES FOR WATER	
CHD(10)	DEPTHS, CM, OF NODES BELOW SURFACE (A NODE IS A POINT WHERE A WATER POTENTIAL IS CALCULATED) STARTING AT SURFACE
CHDX(10)	THICKNESS OF REGION CENTERED ON NODE WHERE COUNTING STARTS AT FIRST NODE BELOW SURFACE AND GOES DOWN
CHDXX(10)	CHDXX(I)=CHD(I+1) - CHD(I)
FTVTPR(10)	MM OF WATER TAKEN FROM EACH LAYER DURING PMDT
FWINF	NET TOP SURFACE FLUX FOR PMDT, CM, DOES NOT INCLUDE TRANSPERSION.
FWPSI(10)	SOIL WATER POTENTIAL, BARS, VALUE AT END OF PMDT
PBGFLG	IF=.TRUE., WRITE DEBUGGING INFORMATION THIS TIME STEP
PBUG1	NUMBER OF TIME STEPS BETWEEN DEBUGGING OUTPUTS
FLGFLG	IF=.TRUE., WRITE DEBUGGING INFORMATION THIS TWDT
PMDT	TIME STEP DETERMINED IN MAIN, DAYS
PMN	NUMBER OF NODES, SAME AS NUMBER OF NODES IN HEAT, COUNTING STARTS AT SURFACE
PWDELW	INCREMENT IN VHC, TYPICALLY 0.01-0.02
PWH(60)	TABLE OF HYDRAULIC PRESSURE HEAD VERSUS THETA, BARS, USING SAME THETA SCALE AND SPACING AS PWKIN
PWHCRY	ALLOWABLE LOW PRESSURE LIMIT FOR ANY LAYER
PWHHET	ALLOWABLE HIGH PRESSURE LIMIT FOR ANY LAYER
PWK(10)	HYDRAULIC CONDUCTIVITY, CM2 BAR-1 DAY-1, PWK(I) IS CONDUCTIVITY AVERAGED OVER TWDT, IN REGION BETWEEN NODES I AND I+1, WHERE COUNTING STARTS AT SURFACE.
PWKCAL	CONDUCTIVITY OF CALCHE LAYER
PWKIN(60)	TABLE OF CONDUCTIVITY VERSUS THETA, CM2 BAR-1 DAY-1, STARTING WITH VALUE AT THETA = 0.0, READ IN IN WINIT.
PWKSUM(60)	ARRAY USED TO CALCULATE AVERAGE K, (CM-BARS)/DAY
PWLLIM	LOWER LIMIT OF THETA, DIMENSIONLESS CALCULATED IN WINIT AND = SUM OF CONDUCTIVITY X DELTA H
PWM	NUMBER OF ENTRIES IN CONDUCTIVITY AND PRESURE TABLES
PWRNRF	RUNON TO RUNOFF RATIO PER DAY
PWT(60)	ARRAY CONTAINING UNIFORMLY DISTRIBUTED VALUES OF THETA
PWTLEM	LARGEST CHANGE IN THETA ALLOWED FOR NODES 2 TO PMN-1 DURING ANY TIME STEP TWDT. TYPICAL VALUE .01 TO .02
PWHC(10)	WATER CAPACITY, BAR-1, OF REGIONS SURROUNDING NODES, COUNTING STARTS AT FIRST NODE BELOW SURFACE
R	A VERY TEMPORARY VARIABLE - USED IN REFINED TWDT ESTIMATE, TRANSPERSION SECTION, REDUCTION OF TWDT IF DELTA THETA TOO LARGE, AND AS RATIO OF WATER IN TO WATER STORED AS CALCULATED IN WBAL.
S	A VERY TEMPORARY VARIABLE - USED IN REFINED TWDT ESTIMATE, TRANSPERSION SECTION, CONDUCTIVITY SECTION, AND REDUCTION OF TWDT IF DELTA THETA TOO LARGE.
T	A VERY TEMPORARY VARIABLE - USED IN REFINED TWDT ESTIMATE.
TDH	A SUBROUTINE USED BY WATER AND HEAT TO SOLVE A SET OF SIMULTANEOUS DIFFERENCE EQUATIONS, THE LEFT HAND SIDES OF WHICH FORM A TRI-DIAGONAL MATRIX.
TIME	CURRENT JULIAN DATE - BOOKKEEPING DONE IN MAIN PROGRAM.
TSTART	JULIAN DATE OF START OF RUN - INITIALIZED IN MAIN PROGRAM
TWA	FRACTION OF PWDELW INTERVAL, USED IN INTERPOLATING
TWA(10)	PARAMETER A FOR TRI-DIAGONAL MATRIX ROUTINE (TDH ROUTINE)
TWAAA(10)	ARRAY CONTAINING VALUES OF TWTHA(I) FOR I=2,PMN-1

Table C-1, continued

TW8(10)	PARAMETER B FOR TDM ROUTINE
TWBEC(10)	CONTAINS ORDERED VALUES OF TWAA.
TH	A VERY TEMPORARY VARIABLE - USED IN SURFACE FLUX CALCULATION, TRANSPERSION SECTION, AND CONDUCTIVITY SECTION.
TWC(10)	PARAMETER C FOR TDM ROUTINE
TWCCC	USED TO READ AND WRITE COMMENTS IN INPUT DATA
THD(10)	PARAMETER D FOR TDM ROUTINE
TWDT	ACTUAL TIME STEP WATER IS USING
TWDTHP(10)	CHANGE IN THETA DURING LAST TWDT
TWDTP	LENGTH OF PREVIOUS WATER TIME STEP
TWDTO	HOLDS CURRENT VALUE OF TWDT AS IT IS BEING REDUCED BECAUSE DELTA THETA IS TOO LARGE.
THEVAP	EVAPORATIVE DEMAND, MM, WATER TO EVAPORATE FROM SURFACE DURING REMAINDER OF PMDT
TWFZRZ	EQUALS .TRUE. IF SOIL PROFILE FROZEN, EQUALS .FALSE. IF NOT FROZEN.
TWI	TEMPORARY VARIABLE USED TO SET UP PWT ARRAY.
TWHAC(10)	PRESSURE HEAD AT BEGINNING OF TWDT, BARS
TWHBC(10)	PRESSURE HEAD AT END OF TWDT, BARS
TWHHA	INTERPOLATED VALUES OF PHH
TWIN	EQUALS .TRUE. IF SURFACE PRESSURE IS WITHIN LIMITS
THJA	INTEGER USED IN PICKING VALUES OF K, H OFF TABLES
THJB	INTEGER USED IN PICKING VALUES OF K, H OFF TABLES
THJR	INTEGER COUNTER USED TO LIMIT NUMBER OF TWDT HALVINGS
THKSA	INTERPOLATED VALUE OF PNKSUM
THONE	EQUALS .TRUE. IF FIRST DELTA THETA APPROXIMATION HAS ALREADY BEEN DONE DURING CURRENT TWDT.
THR	RAIN, MM, WATER TO INFILTRATE, LEAVE STANDING OR RUNOFF DURING REMAINDER OF PMDT.
THRAIN	EQUALS .TRUE. IF RAIN OCCURS DURING TWDT
THRP	EQUALS .TRUE. IF THRAIN WAS TRUE LAST TWDT.
THSF	SURFACE FLUX OF WATER OR VAPOR, CM
THSF8	FLUX OF WATER MOVING INTO PROFILE DURING TWDT THROUGH CALICHE, CM.
THSFBT	FLUX OF WATER MOVING INTO PROFILE DURING PMDT THROUGH CALICHE, CM.
THSFC	CALCULATED SURFACE FLUX USING THHB(1) AND PWK(1).
TWSFD	EQUALS THSF-THSFC
TWSIND	STANDING WATER, MM, AFTER RUNON-RUNOFF ASSUMPTIONS HAVE BEEN CONSIDERED.
TWSIRD	CHANGE DURING TIME STEP IN WATER STORED IN LAYERS OF PROFILE, CM. (SHOULD EQUAL TWIN)
TWTAC(10)	WATER AVAILABLE IN LAYERS, DIMENSIONLESS
TWTHAAC(10)	VOLUMETRIC WATER CONTENT AT BEGINNING OF PMDT
TWTHAC(10)	VOLUMETRIC WATER CONTENT (VWC) AT BEGINNING OF TWDT
TWTHBC(10)	VWC AT END OF TWDT
TWTHC	THETA AVERAGED OVER TWDT FOR WHATEVER LAYER WE'RE CALCULATING AT THE MOMENT

Table C-1, continued

THTK	PROPORTIONALITY CONSTANT WHICH IS CALCULATED TO MAKE TRANSPERSION DEMAND FROM A LAYER PROPORTIONAL TO WATER AVAILABLE AND RELATIVE ROOT AMOUNTS IN A LAYER.
THTHTS(10)	RUNNING SUM OVER THOT'S OF TRANSPERSION BY LAYER, CM
THTSPRC(10)	TRANSPERSION LOSS OF WATER FROM REGION SURROUNDING NODE, CM, (TOP AND BOTTOM NODES EXCLUDED) DURING THOT
THTOT	TOTAL TIME THAT HAS ELAPSED IN PMDT. DOES NOT INCLUDE CURRENT THOT, DAYS
THTN(6)	TRANSPIRATIONAL DEMAND BY FUNCTIONAL GROUP, CM
THU(10)	WATER POTENTIALS IN BARS OF SOIL LAYERS AS RETURNED FROM SUBROUTINE TDM.
TWHAC(10)	USED IN SETTING UP CALL TO TDM
TWHB(10)	USED IN SETTING UP CALL TO TDM
TWIN	FLUX OF WATER MOVING IN TO PROFILE THIS TIME STEP, EQUALS FLUX IN AT TOP + FLUX IN FROM BOTTOM - TRANSPERSION, CM. (SHOULD EQUAL TWSTRD)
U	A VERY TEMPORARY VARIABLE-USED IN REFINED THOT ESTIMATE
WBAL	SUBROUTINE WHICH CHECKS OVERALL ACCURACY OF CALCULATIONS DONE IN WATER - DETERMINES WATER INTO OR OUT OF PROFILE AND COMPARES IT TO CHANGE IN WATER STORED IN PROFILE.
WTIME	FUNCTION WHICH RETURNS ELAPSED CPU TIME IN SECONDS FROM START OF RUN.
XHSGLT(10)	SOIL TEMPERATURE PROFILE, C. INDEXED BY NODES, SO XHSOLT(2), E.G., IS TEMPERATURE OF FIRST LAYER.
XWSIND	STATE VARIABLE CALCULATED BY WATER EQUAL TO AMOUNT OF WATER STANDING ON SOIL SURFACE, MM.
XHTHTA(10)	THETA OF LAYER AT END OF PMDT
Y	A VERY TEMPORARY VARIABLE - USED ONLY TO HOLD VALUE OF FUNCTION WTIME.
Z	A DUMMY USED AS AN ARGUMENT IN WTIME
ZEVAP	MM WATER POTENTIALLY EVAPORATED FROM SOIL SURFACE IN PMDT VALUE OBTAINED FROM SUBROUTINE PSWG
ZRAIN	RAINFALL, MM IN PMDT
ZRINT	RAINFALL INTENSITY, MM/HR

SUBROUTINE WATER

```
IF(XHSOLT(2) .LE. -1) TWFRZN=.TRUE.
```

WATR 290

If temperature of the top soil layer is less than or equal to -1°C , the entire soil profile is considered frozen.

```
DO 50 I=1,6
  DO 50 J=1,PMN-2
  50 TWTW(I)=TWTW(I)+1.E-5*CVTSPR(I,J)
```

WATR 319
WATR 320
WATR 322

Determine TWTW(I), transpiration demand in centimeters for plant functional group I, for $I = 1$ to 6.

```
IF(.NOT. TWFRZN) GO TO 70
TWRAIN=.FALSE.
TWEVAP=0.0
TWRP=.FALSE.
GOT0100
```

WATR 334
WATR 335
WATR 336
WATR 337
WATR 338

If soil is frozen, set evaporation equal to zero, set flags indicating there is no precipitation this TWDT, nor was there any last TWDT, and go to section refining TWDT estimate.

```
70 IF((TWR+TWSTND).LE.4.)GOT080
TWRAIN = .TRUE.
TWDT=0.02083
IF(TWRP)GOT090
GO TO 120
80 TWRAIN=.FALSE.
90 TWDT=TWDTP
```

WATR 339
WATR 340
WATR 341
WATR 342
WATR 343
WATR 344
WATR 345

If the amount of water remaining on the surface to be infiltrated is less than or equal to 4 mm, set TWRAIN = TRUE (not raining this TWDT), set TWDT = TWDT_P (previous value) and go on to section refining TWDT estimate. If water amount is greater than 4 mm (no rain this TWDT), set TWDT equal to .02083 (= 1/48 day = 30 min = minimum value) and check if rain during last TWDT. If yes, set TWDT = TWDT_P and go on to section refining TWDT estimate. If no, keep TWDT at minimum value and skip section refining TWDT estimate.

```
R=0.3*PWTLIM
S=0.9*PWTLIM
T=0.0
DO110I=2,PMN-1
U=ABS(TWDTHP(I))
IF(U.LT.R)GOT0110
IF(U.GT.S)GOT0120
IF(U.GT.T)T=U
110 CONTINUE
IF(T.LT.R)T=R
IF(T.LE.0.0)GOT0120
TWDT=1.9*TWDT*(PWTLIM/T)
```

WATR 352
WATR 353
WATR 354
WATR 355
WATR 356
WATR 357
WATR 358
WATR 359
WATR 360
WATR 361
WATR 362
WATR 363

The only circumstances under which we do not reach this point are if TWRAIN = .TRUE. and TWRP = .FALSE. (The most common example of this would be that the surface was dry last TWDT but rain has occurred since.) The point of this section is to increase TWDT as much as possible within the constraint that theta does not change more than PWTLIM during TWDT. R, S and T are defined as shown. Each pass through DO loop (one pass per soil layer), U is set equal to magnitude of change in theta during previous TWDT. If U is ever found to be greater than $0.9 * PWTLIM$, remainder of this section is skipped (TWDT

retains present value). At the completion of the loop plus the next statement, T is the larger of: 1) $0.3 * \text{PWTLIM}$ and 2) the largest value of U (maximum value $0.9 * \text{PWTLIM}$). After a precautionary check for zero value of T, TWDT is increased by the factor PWTLIM/T . The factor 0.9 is a precautionary measure so TWDT isn't increased too much because if TWDT is set too large here, a later check may reduce it.

```
170 IF(TWDT .GT. (PMDT-THTTOT)) TWDT=PMDT-THTTOT
```

HATR 365

Check the sum of TWDT's to be sure it isn't greater than PMDT.

```
130 CONTINUE
```

HATR 375

Control returns to this point if TWDT is reduced in the line below.

```
IF(TWFRZN) GO TO 150
```

HATR 380

If soil is frozen, skip potential surface flux calculation.

```
TW=AHEN1(THR,(ZRINT+TWDT*24.))
```

HATR 391

The contribution to the surface flux from precipitation, TW, is the minimum of the following: 1) ZRINT * TWDT * 24 (which is the amount of precipitation in TWDT at rate ZRINT); and 2) TWR, the remaining precipitation to infiltrate into the soil. At the end of each TWDT, ZRINT * TWDT * 24 is subtracted from TWR (line 801). Thus, line 391 is necessary to ensure that the sum of ZRINT * TWDT * 24 does not become larger than ZRAIN, total precipitation for the time-step.

```
TWSF=TH+THSTND-THEVAP+TWDT/PMDT
140 TWSF=TWSF*0.1
```

HATR 392
HATR 395

Potential surface flux, in centimeters, equals TW from line 391 above, plus standing water, minus that portion of evaporation for PMDT which occurs this TWDT.

```
150 TWSF=0.0
```

HATR 397

We reach here only if soil is frozen (line 380). If frozen, then set surface flux equal to zero and go on.

```
R=TWDT/PMDT
10170 I=1,PMN-2
170 THTSR(I)=0.0
DO 210 J=1,6
THTK=0.0
DO180 I=1,PMN-2
THTA(I)=THTA(I+1)-PHLLIM
180 THTK=THTK+THTA(I)*CVRDST(J,I)
IF(THTK .LE. 1.E-6) GO TO 190
THTK=R*THTK(J)/THTK
190 CONTINUE
DO200 I=1,PMN-2
200 THTSR(I)=THTSR(I)+THTK*THTA(I)*CVRDST(J,I)
210 CONTINUE
```

HATR 413
HATR 414
HATR 415
HATR 416
HATR 419
HATR 420
HATR 422
HATR 423
HATR 426
HATR 427
HATR 428
HATR 429
HATR 430
HATR 431

Determine THTSR(I), centimeters, transpiration demand by layer. It is proportional to water available in the layer THTA(I), and the fraction of roots in the layer CVRDST(J,I). Transpiration demand is assumed uniformly distributed over PMDT.

Thus, each TWDT, the demand is $R = \text{TWDT}/\text{PMDT}$ times the total demand. Line 418 begins the main DO loop

over plant functional groups (FG's). TWTK first becomes the sum over layers of water available in the layer times fraction of roots of FG J in the layer. Water available is dimensionless and equal to the value of theta at the beginning of TWDT, TWTHA(I+1), minus the lower limit of theta, PWLLIM. The indexing looks strange because TWTHA is indexed over nodes, and TWTA over layers (see Fig. C-2). Line 426 will be true if there is no FG represented by current value of J. (For Curlew Valley simulation, e.g., perennial FG's fill places 1, 2, 3 in XVPLNT, CVRDST, etc., and annual FG's fill places 5, 6, leaving place 4 vacant.) In line 427, TWTK becomes the proportionality factor needed. Lines 429, 430 are a DO loop over soil layers, where, in each pass through the loop, the transpirational demand due to roots of FG J in layer I is added to the demand from layer I. The algebra behind these lines of code is not obvious so more explanation is necessary. If one puts the equation in lines 423 and 427 into line 430 and writes it in normal algebraic form we get:

$$\Delta[\text{TWTSPR}(I)]_J = \frac{\text{TWDT}}{\text{PMDT}} [\text{TWTW}(J)] \frac{[\text{TWTA}(I)] [\text{CVRDST}(J,I)]}{\sum_I [\text{TWTA}(I)] [\text{CVRDST}(J,I)]} ,$$

where $\Delta[\text{TWTSPR}(I)]_J$ means the addition to TWTSPR(I) from FG J. If we sum both sides over I (layers), we find that the total transpirational demand from FG J for this TWDT is $(\text{TWDT}/\text{PMDT})[\text{TWTW}(J)]$, which is just what we want since TWTW(J) is the demand from FG J over PMDT.

```

TH=0.3
D0230I=1,PMN=2
S=TWTSPR(I)/CHDX(I)
IF(S.LE.(TWTA(I)*0.5))GOT0220
TWTSPR(I)=TWTA(I)+0.5*CHDX(I)
S=TWTSPR(I)
220 CONTINUE
IF(TW.LT.S)TW=S
230 CONTINUE

```

```

HATR 4 36
HATR 4 35
HATR 4 36
HATR 4 38
HATR 4 39
HATR 4 40
HATR 4 41
HATR 4 42
HATR 4 43

```

S = centimeters of transpiration from a layer \div thickness of layer = change in theta for layer from transpiration (line 436). Check all layers and set TW = largest value of S. If S ever represents more than half the water available from a layer, reduce transpiration and S to a value equal to half the water available. After this loop, TWTSPR is actual transpiration. A precaution should be noted here. It is possible for the plant submodel(s) to demand more transpiration than WATER is removing from the soil. For one or two TWDT's, this is not serious, but if it occurs over several consecutive PMDT's, the plants will be growing as if there is more soil water available than actually exists. This situation should, and can, be avoided by keying transpiration to soil water in such a manner that, as water is removed from the soil, transpiration becomes zero before theta reaches PWLLIM.

```

IF((TW.LE.PWLLIM).OR.(THJM.GE.2).OR.(TWDT.LE.0.02083))GOT0240
THJM=THJM+1
TWDT=TWDT+0.9*PWLLIM/TW
IF(TWDT.LE.0.02083)TWDT=0.02083
GO TO 130
240 CONTINUE

```

```

HATR 4 45
HATR 4 46
HATR 4 47
HATR 4 48
HATR 4 49
HATR 4 50

```

TWDT will not be reduced if: 1) TW, calculated just above, is less than or equal to the largest allowable change in theta; 2) if it has already been reduced twice before; or 3)

if it is already at the minimum value of 30 min. If it is too large, we increment the counter, reduce TWDT and ensure that its value is not below minimum.

Overview of Conductivity and Specific Water Capacity Calculation

In order to accurately simulate water content and potential, it is important to determine hydraulic conductivity, PHK, as accurately as possible. Average PHK for a region between nodes (see Fig. C-2) over TWDT can be calculated if theta is known at the beginning and end of TWDT. But to determine theta at the end of TWDT, we must use average PWK during TWDT. Thus, an iteration scheme would appear to be in order. With a large subroutine such as this, however, it appears likely that it would be easy to set something up which would eat up considerable computer time. To avoid excessive computer-time use, no iterations are performed and, whenever possible, the change in theta for the current TWDT is estimated from the change in theta during the previous TWDT. "Whenever possible" turns out to be over 90% of the time.

```
IF(TWONE) GO TO 280
TWONE=.TRUE.
```

WATR 466
WATR 467

Use the flag TWONE to ensure going through this section only once each TWDT.

```
IF((TWRP .AND. TWRAIN) .OR. ((.NOT. TWRP) .AND. (.NOT. TWRAIN))) WATR 468
 1 GO TO 250
  GO TO 280
250 CONTINUE
WATR 469
WATR 470
WATR 471
```

If there was rain last TWDT and it is raining now, or if no rain occurred last TWDT and there is no rain now, we can estimate the change in theta this TWDT from change last TWDT. Otherwise, go to the section calculating conductivity and specific water capacity.

```
DO270I=2,PNN
```

WATR 472

DO loop through nodes (all except top one).

```
S=TWDT/TWDTP
IF(S.GT.1.)S=SQRT(S)
TH=TWTHB(I)+S*TWDTHP(I)
IF(TH .GE. PWTC(PNM)) GO TO 260
IF(TH .LT. PWLLIM) TH=PWLLIM
```

WATR 474
WATR 475
WATR 476
WATR 477
WATR 478

Tentative change in theta is equal to change last TWDT times S. S is the ratio of present and past time-steps if ratio ≤ 1 . If ratio > 1 , S equals the square root of the ratio as a precaution against overestimating change in theta. Finally, perform checks to ensure that theta is within limits.

TWTHB(I)=TW

WATR 479

Set theta for current node equal to tentative value.

```
IF(I.GT.2)GOTO270
TWJA=TWTHB(I) / PWDELW + 1.
TWAA=(TWTHB(I)-PWT(TWJA))/PWDELW
TWHB(I)=PWH(TWJA)+(PWH(TWJA+1)-PWH(TWJA))*TWAA
GO TO 270
```

WATR 480
WATR 483
WATR 485
WATR 486
WATR 487

If current node is below second node, skip these lines. Otherwise, calculate TWHB, SWP at end of TWDT, for first layer (second node) by interpolating between appropriate values in PWH table. It is used below in the calculation for actual surface flux (line 574).

DO 320I=2,PMN-1

WATR 494

DO loop over PMN—2 inner nodes. In this loop, calculate specific water capacity of each of the PMN—2 layers and hydraulic conductivity of the PMN—3 regions between the inner nodes.

```
TWTHC =(TWTHA(I)+TWTHB(I)) / 2.
IF(TWTHC .GT. PWT(PWH)) TWTHC=PWT(PWH)
IF(TWTHC .LT. PWLLIH) TWTHC=PWLLIH
```

WATR 495
WATR 496
WATR 497

Calculate average water content during TWDT and ensure that values lie between limits.

```
TWJA=TWTHC/PWDELW + 1.
IF(TWJA .GE. PMN) TWJA=PMN-1
TWAA=(TWTHC-PWT(TWJA))/PWDELW
TWKSA(I)=PWKSUM(TWJA)+(PWKSUM(TWJA+1)-PWKSUM(TWJA))*TWAA
TWHHA(I)=PWH(TWJA)+(PWH(TWJA+1)-PWH(TWJA))*TWAA
```

WATR 499
WATR 500
WATR 502
WATR 504
WATR 505

Using value of average water content just found, interpolate between appropriate values in PWKSUM and PWH tables, and call these values TWKSA and TWHHA.

PWHC(I-1) = PWDELW/(PWH(TWJA+1)-PWH(TWJA))

WATR 508

The specific water capacity is simply the inverse of the slope of the SWP vs. theta relationship.

IF(I.LE.2)GOTO310

WATR 509

Need TWKSA and TWHHA for two adjacent nodes to calculate PWK, hydraulic conductivity, for region between.

IF(TWJB .EQ. TWJA) GO TO 300

WATR 510

If average water content of previous node and current node are close (between same pairs of values in PWKSUM and PWH table), calculate PWK differently. This avoids any chance of a divide-by-zero (or nearly zero) situation.

PWK(I-1)=(TWKSA(I)-TWKSA(I-1))/(TWHHA(I)-TWHHA(I-1))

WATR 511

Calculate hydraulic conductivity. Hanks and Bowers (1962) call it a "round about" method in that diffusivity is calculated from measured conductivity values, and then average conductivity is determined from diffusivity. If one goes through their algebra, PWK is seen to be average conductivity over a region of soil, weighted with respect to SWP. PWKSUM, calculated in line 1013, is

$$\text{PWKSUM}(M) = \sum_{i=1}^M K_i (\Delta \text{SWP})_i,$$

where

- i = index which goes through theta values in the conductivity and SWP tables ($i = 1 \Rightarrow \theta = \text{PWTLM}$; $i = 2 \Rightarrow \theta = 2 \cdot \text{PWTLM}$, ...; $i = m \Rightarrow \theta = M \cdot \text{PWTLM}$);
- K_i = measured conductivity (read in as PWKIN) at $\theta = i \cdot \text{PWTLM}$;
- $(\Delta \text{SWP})_i$ = change in soil water potential (from PWH array) from $\theta = i \cdot \text{PWTLM}$ to $\theta = (i + 1) \cdot \text{PWTLM}$.

If theta at the top of the region corresponds to $M \cdot \text{PWTLM}$ and theta at the bottom corresponds to $N \cdot \text{PWTLM}$, then rewrite line 511:

$$\text{average conductivity} = \frac{\sum_{i=1}^M K_i (\Delta \text{SWP})_i}{\text{SWP}_M - \text{SWP}_N}.$$

Say $M > N$, then

$$\text{average conductivity} = \frac{\sum_{i=N}^M K_i (\Delta \text{SWP})_i}{\sum_{i=N}^M (\Delta \text{SWP})_i}.$$

Thus, average conductivity for a region is an average over measured conductivity, weighted with respect to SWP, as asserted above.

To illustrate, do a numerical example with theta at the node at the top of the region = 0.25 and = 0.15 at the bottom. Use input data for Curlew Valley run.

theta	0.15	0.25
TWKSA	0.4047	0.9157
TWHHA	-8.090	-8.8800
PWKIN	0.0198	0.4630

$$\begin{aligned} \text{weighted average conductivity} &= \frac{\text{TWKSA}_{.15} - \text{TWKSA}_{.25}}{\text{TWHHA}_{.15} - \text{TWHHA}_{.25}}; \\ &= \frac{0.4047 - 0.9157}{-8.090 - (-8.8800)} = 0.0709. \end{aligned}$$

$$\text{unweighted average conductivity} = \frac{0.0198 + 0.4630}{2} = 0.2414.$$

The weighted average value, which is the one used in the program, is considerably smaller than the unweighted average. This is consistent with the findings of Hanks and Bowers (1962) that the dry soil (lower conductivity) controls the flow of water more than the wetter soil.

```
300 PWK(I-1)=(PWKSUM(THJA+1)-PWKSUM(TWJA)) / (PWH(THJA+1)-PWH(TWJA)) WATR 513
```

If theta values at nodes outlining the current region are between the same pairs of values in PWKSUM and PWH tables, use this formula which is a special case of the one in line 511 and avoids the possibility of dividing by zero or a very small number.

```
310 THJB=TWJA
```

WATR 514

We need to know previous value of TWJA on the next pass through the loop.

```
320 CONTINUE
```

WATR 517

End of loop.

Overview of Top Boundary Condition Section

Potential top surface flux was calculated in line 392. Here, we check if we can meet potential by setting soil surface conditions to wettest conditions (if potential flux > 0 , or into soil) or to driest (if potential flux < 0). If potential flux can be met, actual flux is set equal to potential flux and program goes on. Since no submodel, including WATER, uses soil surface conditions, the surface node is always either at its wettest or driest condition, and more precise values are not determined. If potential flux cannot be met, actual flux is calculated, and difference between actual and potential is determined. If this difference is positive, it ultimately becomes standing water (line 794). If negative, it eventually is lost.

```
IF(TWSF.LT.0.0)GOTO330
THB(1)=PWHWET
THTHC(1)=PWT(PWM)
GOTO340
330 CONTINUE
THB(1)=PWHDRY
THTHC(1)=PWLLIM
WATR 540
WATR 544
WATR 545
WATR 546
WATR 548
WATR 551
WATR 552
```

Check sign of surface flux and set surface conditions wettest if positive, driest if negative.

```
340 CONTINUE
C CALCULATE PWK(1)
THTHC=THTHB(1)
IF(THTHC .GT. PWT(PWM)) THTHC=PWT(PWM)
WATR 554
WATR 555
WATR 556
WATR 557
```

```

      IF(TWTHC .LT. PHLLIM) TWTHC=PHLLIM          HATR 558
C PNT(TWJA) AND PNT(TWJA+1) BRACKET TWTHC
      TWJA=TWTHC/PNDELW + 1.                      HATR 559
      IF(TWJA .GE. PMN) TWJA=PMN-1                HATR 560
C CHECK IF WATER CONTENTS OF FIRST TWO NODES ARE VERY CLOSE
      IF((TWKSA(2) .GE. PWKSUM(TWJA)) .AND. (TWKSA(2) .LE. PWKSUM(TWJA+1)) HATR 561
      1 ))> GO TO 350                                HATR 562
C THAA IS FOR INTERPOLATING
      THAA=(TWTHC-PNT(TWJA))/PNDELW               HATR 563
      TWKSA(1)=PWKSUM(TWJA)+(PWKSUM(TWJA+1)-PWKSUM(TWJA))*THAA   HATR 564
      THHHA(1)=THHBC(1)                            HATR 565
      PWK(1)=(TWKSA(2)-TWKSA(1))/(THHHA(2)-THHHA(1))           HATR 566
      GO TO 360                                     HATR 567
350    PWK(1) = (PWKSUM(TWJA+1)-PWKSUM(TWJA)) / (PHHCTWJA+1)   HATR 568
      1 -PHHCTWJA)                                    HATR 569
360 CONTINUE                                         HATR 570
                                                HATR 571
                                                HATR 572
                                                HATR 573

```

Determine PWK(1) just as PWK(I) for I = 2 to PMN—2 were determined in lines 494–517. The only difference is that water content is not averaged in line 556 as it was in line 495 (averaging surface node led to nasty oscillations).

```
TWSFC=PWK(1)*THDT+(THH8(1)-THH8(2)+9.833E-4*CHDXX(1))/CHDXX(1)    HATR 574
```

Calculated surface flux equals conductivity times time-step times SWP gradient [the term 9.833—4*CHDXX(1) is contribution due to gravity].

```

IF(TWSF.LT.0.0)GOT0370          HATR 575
IF(TWSFC.GE.TWSF)GOT0390        HATR 576
GOT0380                         HATR 577
370 IF(TWSFC.LE.TWSF)GOT0390    HATR 578

```

Check if potential surface flux condition can be met.

```

380 CONTINUE
TWIN=.FALSE.
TWSFD=TWSF-TWSFC
TWSF=TWSFC
GOT0400                         HATR 580
                                      HATR 582
                                      HATR 583
                                      HATR 584
                                      HATR 585

```

If we reach here, they can't be met. Set flag announcing this, determine difference between potential and calculated fluxes, set surface flux equal to calculated value and go on.

```

390 CONTINUE
TWIN=.TRUE.
TWSFD=0.0
400 CONTINUE                         HATR 587
                                      HATR 591
                                      HATR 592
                                      HATR 594

```

If we reach here, potential surface flux condition can be met. Set flag announcing this, set difference between potential and actual equal to zero and go on.

```

IF(.NOT. TWFRZN) GO TO 420
I0410I=1,PMN=2
410 PWK(I)=PWK(I)*1.E-6
420 CONTINUE                           HATR 600
                                      HATR 601
                                      HATR 602
                                      HATR 603

```

If soil is frozen, reduce hydraulic conductivity by a factor of a million and stop soil water movement.

```

      DO 430 I=1,PMN-1
      THWA(I) = PWK(I) / CHDX(I)
      IF(I .EQ. PMN-1) GO TO 430
      THWB(I) = (2.*PWHC(I)*CHDX(I)) / TWDT
430 CONTINUE
      DO 440 I=2, PMN-3
      THAC(I) = THWA(I+1)
      THCC(I) = THWA(I)
      THBC(I) = THWB(I)+THAC(I)+THC(I)
      THAC(I) = THAC(I+1)*(THWB(I)-THA(I)-THC(I)) + THWA(I)*THC(I)
      1 + THAC(I+2)*THAC(I) + 2.*(PWK(I) - PHK(I+1)) *9.833E-4
      2 -2.*THTSPR(I)/TWDT
      THAC(I) = THWA(2)
      THC(I) = 0.
      THBC(I) = THWB(1) + THA(1)
      THDC(I) = THWA(2)*(THWB(1)-THA(1)) + THWA(3)*THA(1)
      1 + TWSE*2./TWDT -2.*PHK(2)*9.833E-4
      2 -2.*THTSPR(1)/TWDT
      THA(PMN-2) = 0.
      THC(PMN-2) = THWA(PMN-2)
      THB(PMN-2) = THWB(PMN-2) + THCC(PMN-2) + THWA(PMN-1)
      THD(PMN-2) = THWA(PMN-1)*(THWB(PMN-2)-THC(PMN-2)-THWA(PMN-1))
      1 + THWA(PMN-2)*THC(PMN-2) + 2.*THWB(PMN)*THWA(PMN-1)
      2 +2.*(PHK(PMN-2)-PHK(PMN-1)) *9.833E-4
      3 -2.*THTSPR(PMN-2)/TWDT
      HATR 641
      HATR 642
      HATR 643
      HATR 644
      HATR 645
      HATR 647
      HATR 648
      HATR 649
      HATR 650
      HATR 651
      HATR 652
      HATR 653
      HATR 655
      HATR 656
      HATR 657
      HATR 658
      HATR 659
      HATR 660
      HATR 661
      HATR 662
      HATR 663
      HATR 664
      HATR 665
      HATR 666
      HATR 667

```

Generate matrix elements of tridiagonal matrix. These elements are coefficients of SWP in the system of difference equations (one for each layer) we need to solve to determine SWP of each layer. For more information see "Derivation of Difference Equations." These matrix elements can be determined only after we've determined: 1) hydraulic conductivity; 2) specific water capacity; 3) transpiration; 4) top surface flux.

```
CALL TDM(TWA, THB, THC, THD, THU, PMN-2)
```

```
HATR 677
```

TDM is the subroutine which solves the tridiagonal matrix, generated above, for PMN—2 values of SWP. These values are returned to WATER in array TWU. For more details, see the Detailed Program Description of TDM.

```

      DO 450 I=2,PMN-1
      TWTHB(I)=TWTHA(I)+PWHC(I-1)*(THU(I-1)-TWHA(I))
      IF(TWTHB(I) .GT. PWT(PMN)) TWTHB(I)=PWT(PMN)
      IF(TWTHB(I) .LT. PHLLIM) TWTHB(I)=PHLLIM
450 CONTINUE

```

```

      HATR 690
      HATR 691
      HATR 692
      HATR 693
      HATR 694

```

Calculate TWTHB, theta of nodes at end of TWDT, from values of TWU just returned from subroutine TDM. Equation used is

$$(\text{theta}) = (\text{specific water capacity}) \times [\Delta(\text{SWP})].$$

Ensure that values obtained are within range.

```

      DO 460 I=2,PMN-1
      THJA=TWTHB(I)/PWHDELW+1.
      IF(THJA .GE. PMN) THJA=PMN-1
      THAA=(TWTHB(I)-PWT(THJA))/PWHDELW
460 TWHB(I)=PWH(THJA)+(PWH(THJA+1) - PWH(THJA))*THAA

```

```

      HATR 697
      HATR 698
      HATR 699
      HATR 700
      HATR 701

```

Calculate TWHB, SWP of nodes at end of TWDT, from values of theta just calculated (same method as that starting in lines 495 and 556). This is roundabout in that we could have set TWHB(I) = TWU(I—1) for I = 2, PMN—1. By using the specific water capacity, we find theta much faster than by hunting backwards through array PWH, but we

run the risk of the two values not exactly coinciding because of the various averages used. By determining SWP from theta rather than directly from TWU, then, small errors might occur, but theta and SWP will be consistent with each other.

```
00470 I=2,PMN-1
S=ABS(TWTHB(I)-TWTHA(I))
IF(S.GT.PWTLIM)GOT0480
470 CONTINUE
GO TO 510
```

```
WATR 705
WATR 706
WATR 707
WATR 708
WATR 709
```

Check if any of the delta thetas just calculated are larger than the limit PWTLIM. If yes, see if TWDT can be reduced. If no, go on to check of water balance.

```
480 IF(TWJH.GE.2)GOT0510
TWDTQ=TWDT
TWDT=TWDT*0.9*PWTLIM/S
TWJH=TWJH+1
IF(TWDT.LT.0.02083)TWDT=0.02083
R=TWDT/TWDTQ
490 E0500 I=2,PMN-1
TWHB(I)=TWHA(I)+(TWHB(I)-TWTHA(I))*R
500 TWTHB(I)=TWTHA(I)+(TWTHB(I)-TWTHA(I))*R
GO TO 130
510 CONTINUE
```

```
WATR 710
WATR 711
WATR 712
WATR 713
WATR 715
WATR 716
WATR 717
WATR 718
WATR 719
WATR 720
WATR 721
```

Reduce TWDT if: 1) it hasn't been reduced two or more times already (limit the number of iterations to cut down on computer time); and 2) if it isn't already at its lower limit of 30 min (0.02083 days). In line 712, reduce TWDT; the factor 0.9 is to be on the safe side. Then increment the interation counter and make sure TWDT is not less than 30 min. Finally, reduce the estimates of SWP and theta just calculated above by making the change proportional to the ratio of new TWDT to old TWDT, and go back to statement 130 (line 375) which is the start of the loop to calculate SWP once TWDT is set.

```
TWSFB=-PKCAL*TWDT*((TWHB(PMN-1) + TWTHA(PMN-1)) * .5
1 + 9.833E-4*CHDXC(PMN-1) - THHB(PMN)) / CHDXC(PMN-1)
```

```
WATR 726
WATR 727
```

Calculate water leaving bottom of soil profile (remember that convention is: in is +). This is basically the same equation as line 574.

```
CALL WBALC THTSPR, TWSF, TWSFB, TWTHA, TWTHB, CHOX, PMN,
1      TWWIN, TWSTRD, R)
```

```
WATR 730
WATR 731
```

Call subroutine WBAL to check if the sum of the amounts of water into or out of the profile (rain, evaporation, transpiration, water through caliche layer) is equal to the change in the water stored in the profile. For more detail see "Subroutine WBAL," below.

```
IF(TWDT.LT.0.05)GOT0520
IF((R.GT.99.) .OR. (ABS(TWWIN-TWSTRD) .LT. 0.006)
1 .OR.(ABSR-1.).LT.0.01)GOT0520
TWDT=0.5*TWDT
```

```
WATR 733
WATR 736
WATR 737
WATR 738
```

```
R=0.5
GO TO 490
520 CONTINUE
```

```
WATR 739
WATR 740
WATR 741
```

If the amount of water into or out of the profile is equal to the change in water stored, TWDT remains unchanged. If they are not equal, TWDT may be halved. TWDT will not be halved if its value is currently small (less than .05). Also, it will not be halved if one of the following conditions is met: 1) if R, the ratio of water in to water stored, is greater than 99 (to avoid a divide by zero, WBAL sets R = 99.9999 if TWSTRD is less than 0.001); 2) if TWWIN is sufficiently close to TWSTRD (within 0.006); 3) if R is sufficiently close to 1.0 (within 0.01).

```
CWINF=CWINF+TWSF
TWSFBT = TWSFBT + TWSFB
```

```
WATR 778
WATR 782
```

Accumulate top and bottom surface fluxes. Neither flux includes transpiration.

```
IF(.NOT. TWFRZN) GO TO 570
TWSTND=TWSTND+TWR
TWR=0.0
GO TO 620
570 CONTINUE
```

```
WATR 785
WATR 786
WATR 787
WATR 788
WATR 789
```

If soil is frozen, add precipitation to standing water and skip the normal standing water calculation.

```
IF(TWIN) GO TO 580
TWSTND=TWSFD*10.*PWRNRF**TWDT
IF (TWSTND .LT. 0.0) TWSTND=0.0
GO TO 590
580 TWSTND=0.0
590 CONTINUE
```

```
WATR 792
WATR 794
WATR 795
WATR 796
WATR 797
WATR 798
```

If potential surface flux conditions are met there will be no standing water. If unmet, then in line 794 calculate new level of standing water using parameter PWRNRF, which provides a crude estimate of runoff or runoff and will have a value near 1. (A value of 1.25 for Curlew Valley, e.g., made water continually build up on a surface once the spring melting occurred.) TWSFD is the potential surface flux minus the actual surface flux; the factor 10 changes units to millimeters; and PWRNRF to the TWDT power is a compound interest type factor.

```
600 TWR=TWR-ZRINT*TWDT*24.
610 IF(TWR .LT. 0.0) TWR=0.0
```

```
WATR 801
WATR 802
```

Determine the amount of precipitation remaining to infiltrate this PMDT. Make sure it doesn't get negative.

```
XWSTND=TWSTND
```

```
WATR 805
```

Set state variable XWSTND equal to TWSTND.

```
DO 640 I=1,PMN-2
XWTHTA(I)=TWTHB(I+1)
640 CWPSI(I)=TWTHB(I+1)
```

```
WATR 826
WATR 827
WATR 828
```

Set state variable XWTHTA, theta of layers, equal to theta of appropriate node at end of PMDT (remember layer 1 is centered on node 2). Set communication variable CWPSI, SWP of layers, equal to SWP of appropriate node at the end of PMDT.

ENTRY WINIT

```
WATR 858
```

This entry point is called once, from MAIN. It is used only for initialization purposes: 1) to read in WATER variables; 2) to initialize miscellaneous flags and variables; 3) to perform calculations which need to be done only once.

```
READ(5,670)TWCCC
WRITE(6,680)
WRITE(6,690)TWCCC
```

```
WATR 870
WATR 871
WATR 872
```

Read and write a comment which may say, e.g.,
INITIALIZATION DATA FOR WATER.

```
READ(5,670)TWCCC
WRITE(6,690)TWCCC
READ(5,/)PWDELW
WRITE(6,710)PWDELW
```

```
WATR 875
WATR 876
WATR 877
WATR 878
```

Read and write a comment which describes variable PWDELW, which is then read and written. In similar manner, variables PWH, PWKCAL, PWKIN, PWHDRY, PWHWET, PWM, PWTLIM, PWLLIM, PWRNRNF, TWSTND and TWTHB are read and written.

```
DO 750 I=1, PWM
TWI = I-1
750 PWT(I)=TWI*PWDELW
```

```
WATR 999
WATR1000
WATR1001
```

Set up array PWT, containing PWM values of theta, each PWDELW apart. The conductivity in PWKIN(I) and the SWP in PWH(I) correspond to a theta value of PWT(I).

```
DO 760 I=1,PMN
TWJA=TWTHB(I)/PWDELW + 1.
IF(TWJA .GE. PWM) TWJA=PMH-1
TWAA=(TWTHB(I)-PWT(TWJA)) / PWDELW
760 TWHB(I)=PWH(TWJA)+(PWH(TWJA+1)-PWH(TWJA))*TWAA
```

```
WATR1004
WATR1005
WATR1006
WATR1007
WATR1008
```

Calculate initial SWP values from theta values just read in TWTHB. Approach used is same as in line 483.

```
PWKSUM(1)=(PWKIN(1)+PWKIN(2))*(PWH(2)-PWH(1))*0.5
DO 770 I=2,PWM-1
770 PWKSUM(I)=(PWKIN(I)+PWKIN(I+1))*(PWH(I+1)-PWH(I))*0.5 + PWKSUM(I-1)WATR1013
PWKSUM(PWM)=2.*PWKSUM(PWM-1)-PWKSUM(PWM-2)WATR1017
```

Calculate PWKSUM, sum of conductivity times delta SWP. This is used in line 504 in average conductivity calculations. Each element in PWKSUM equals the previous element plus an increment. Take PWKSUM(I), e.g. It equals PWKSUM(I-1) plus the increment, which is the

average conductivity for theta between values of PWT(I) and PWT(I+1), times the change in SWP for theta between values of PWT(I+1) and PWT(I). In line 1017, the last increment is taken equal to the second to last increment.

```
    WRITE(6,780)
780 FORMAT(' PWKSUM, SUM OF CONDUCTIVITY TIMES DELTA PRESSURE')      WATR1020
      WRITE(6,720) PWKSUM                                              WATR1021
                                                               WATR1022
```

The array PWKSUM, which was just calculated, is written out.

```
READ(5,670)TWCCC
WRITE(6,690)TWCCC
```

```
WATR1025
WATR1026
```

Read and write a comment which says, e.g., END INITIALIZATION FOR WATER.

SUBROUTINE WBAL

WBAL is a small, simple subroutine which acts as an overall check on the accuracy of the calculations performed in WATER. For the time period in question, either TWDT or PMDT, it calculates WIN, amount of water into or out of the soil profile by transpiration, and top and bottom surface flux. It also calculates WSTRD, change in water stored during time period, from the changes in theta of each layer and from layer thickness. WBAL then determines the ratio of these two quantities. The calling program, WATER, in this case, then determines if the ratio is close enough to 1.

```
DO100I=1,PMN=2
A=A+TSPR(I)
100 WSTRD=WSTRD+(THTAF(I+1)-THTAI(I+1))*DX(I)
```

```
WBAL 16
WBAL 17
WBAL 18
```

This is a DO loop through layers. Variable A accumulates transpiration, WSTRD accumulates changes in water held in layers.

```
WIN = SF = A + SFB
```

```
WBAL 19
```

Calculate WIN, change in water in profile from surface fluxes (top and bottom) and transpiration (convention is that water in is positive).

```
IF(ABS(WSTRD),LT,1,E=3)RATIO=99.9999
```

```
WBAL 20
```

Set RATIO equal to a strange large number if WSTRD is small (avoid divide by zero or near zero).

```
IF(ABS(WSTRD),GE,1,E=3)RATIO=WIN/WSTRD
```

```
WBAL 21
```

Actually calculate RATIO if WSTRD is large enough.

FUNCTION WTIME

The purpose of this function is to determine total elapsed CPU time since the beginning of the run. Because we use the variable name TIME for other purposes in the model, the Burroughs Intrinsic Function TIME must be put in a subprogram of some kind in order for it to be used. The Z in the argument of WTIME is a completely dummy variable -- a FORTRAN function needs an argument whether it is used or not.

```
WTIME=0.016667*TIME(2)
```

```
WTM 08
```

TIME(2) is CPU time in 60ths of a second. The factor 0.016667 = 1/60 changes the right-hand side to seconds. CPU time is useful for debugging purposes.

COMPLETE PROGRAM LISTING

SUBROUTINE WATER

SUBROUTINE WATER
 WRITTEN BY PAUL W. LOMMEN
 DESERT BIOME - ECOLOGY CENTER UMC 52
 UTAH STATE UNIVERSITY
 LOGAN, UTAH 84322
 AUGUST 1976
 THIS SUBMODEL OF THE WATER RESPONSE MODEL CALCULATES SOIL WATER
 POTENTIAL IN UP TO 8 SOIL LAYERS. INPUTS NEEDED ARE PRECIPITATION,
 POTENTIAL EVAPORATION, TRANSPERSION, SOIL HYDRAULIC CONDUCTIVITY -
 SOIL
 WATER CONTENT RELATIONSHIP, AND SOIL WATER POTENTIAL - SOIL
 WATER CONTENT RELATIONSHIP.
 LIST OF VARIABLES FOR WATER
 CHD(10) DEPTHS, CM, OF NODES BELOW SURFACE (A NODE IS A POINT
 WHERE A WATER POTENTIAL IS CALCULATED) STARTING AT SURFACE
 CHDX(10) THICKNESS OF REGION CENTERED ON NODE WHERE COUNTING
 STARTS AT FIRST NODE BELOW SURFACE AND GOES DOWN
 CHDXX(10) CHDXX(I)=CHD(I+1) - CHD(I)
 FVTSPR(10) MM OF WATER TAKEN FROM EACH LAYER DURING PHOT
 KWINF NET TOP SURFACE FLUX FOR PHOT, CM, DOES
 NOT INCLUDE TRANSPERSION.
 KWPSI(10) SOIL WATER POTENTIAL, BARS, VALUE AT END OF PHOT
 DBGFLG IF=.TRUE. WRITE DEBUGGING INFORMATION THIS TIME STEP
 DEBUG1 NUMBER OF TIME STEPS BETWEEN DEBUGGING OUTPUTS
 FLGFLG IF=.TRUE. WRITE DEBUGGING INFORMATION THIS TWOTD
 PHDT TIME STEP DETERMINED IN MAIN, DAYS
 PHN NUMBER OF NODES, SAME AS NUMBER OF NODES IN HEAT,
 COUNTING STARTS AT SURFACE
 PHDELH INCREMENT IN VMC, TYPICALLY 0.01-0.02
 PHH(60) TABLE OF HYDRAULIC PRESSURE HEAD VERSUS THETA, BARS,
 USING SAME THETA SCALE AND SPACING AS PWKIN
 PWHERY ALLOWABLE LOW PRESSURE LIMIT FOR ANY LAYER
 PHHNET ALLOWABLE HIGH PRESSURE LIMIT FOR ANY LAYER
 PWK(10) HYDRAULIC CONDUCTIVITY, CM2 BAR-1 DAY-1, PWK(I) IS
 CONDUCTIVITY AVERAGED OVER TWOTD, IN REGION BETWEEN NODES
 I AND I+1, WHERE COUNTING STARTS AT SURFACE.
 PWKCAL CONDUCTIVITY OF CALCIHE LAYER
 PWKIN(60) TABLE OF CONDUCTIVITY VERSUS THETA, CM2 BAR-1 DAY-1,
 STARTING WITH VALUE AT THETA = 0.0, READ IN IN WINIT.
 PWKSUM(60) ARRAY USED TO CALCULATE AVERAGE K, (CM-BARS)/DAY
 PHLLIM LOWER LIMIT OF THETA, DIMENSIONLESS
 CALCULATED IN WINIT AND = SUM OF CONDUCTIVITY X DELTA H
 PHM NUMBER OF ENTRIES IN CONDUCTIVITY AND PRESURE TABLES
 PWRNRF RUNON TO RUNOFF RATIO PER DAY
 PHT(60) ARRAY CONTAINING UNIFORMLY DISTRIBUTED VALUES OF THETA
 PHTLIM LARGEST CHANGE IN THETA ALLOWED FOR NODES 2 TO PHM-1
 DURING ANY TIME STEP TWOTD. TYPICAL VALUE .01 TO .02
 PHWC(10) WATER CAPACITY, BAR-1, OF REGIONS SURROUNDING NODES,
 COUNTING STARTS AT FIRST NODE BELOW SURFACE
 R A VERY TEMPORARY VARIABLE - USED IN REFINED TWOTD ESTIMATE,
 TRANSPERSION SECTION, REDUCTION OF TWOTD IF DELTA THETA
 TOO LARGE, AND AS RATIO OF WATER IN TO WATER STORED

C	AS CALCULATED IN HBAL.	WATR 085
C		WATR 086
C S	A VERY TEMPORARY VARIABLE - USED IN REFINED TWDT ESTIMATE, WATR 087 TRANSPERSION SECTION, CONDUCTIVITY SECTION, AND REDUCTION WATR 088 OF TWDT IF DELTA THETA TOO LARGE.	WATR 088
C		WATR 089
C T	A VERY TEMPORARY VARIABLE - USED IN REFINED TWDT ESTIMATE, WATR 091	WATR 090
C		WATR 092
C TDM	A SUBROUTINE USED BY WATER AND HEAT TO SOLVE A SET OF SIMULTANEOUS DIFFERENCE EQUATIONS, THE LEFT HAND SIDES OF WHICH FORM A TRI-DIAGONAL MATRIX.	WATR 093 WATR 094 WATR 095
C		WATR 096
C TIME	CURRENT JULIAN DATE - BOOKKEEPING DONE IN MAIN PROGRAM.	WATR 097 WATR 098
C		WATR 099
C TSTART	JULIAN DATE OF START OF RUN - INITIALIZED IN MAIN PROGRAM	WATR 100
C		WATR 101
C TWAA	FRACTION OF PWDELW INTERVAL, USED IN INTERPOLATING	WATR 102
C		WATR 103
C THAC(10)	PARAMETER A FOR TRI-DIAGONAL MATRIX ROUTINE (TDM ROUTINE)	WATR 104
C		WATR 105
C THAAA(10)	ARRAY CONTAINING VALUES OF THA(I) FOR I=2,PMN-1	WATR 106
C		WATR 107
C THB(10)	PARAMETER B FOR TDM ROUTINE	WATR 108
C		WATR 109
C THBE(10)	CONTAINS ORDERED VALUES OF TWAA.	WATR 110
C		WATR 111
C TW	A VERY TEMPORARY VARIABLE - USED IN SURFACE FLUX CALCULATION, TRANSPERSION SECTION, AND CONDUCTIVITY SECTION.	WATR 112 WATR 113 WATR 114
C		WATR 115
C THC(10)	PARAMETER C FOR TDM ROUTINE	WATR 116
C		WATR 117
C THCC	USED TO READ AND WRITE COMMENTS IN INPUT DATA	WATR 118
C		WATR 119
C THD(10)	PARAMETER D FOR TDM ROUTINE	WATR 120
C		WATR 121
C TWDT	ACTUAL TIME STEP WATER IS USING	WATR 122
C		WATR 123
C THDTHP(10)	CHANGE IN THETA DURING LAST TWDT	WATR 124
C		WATR 125
C THDTP	LENGTH OF PREVIOUS WATER TIME STEP	WATR 126
C		WATR 127
C THDTQ	HOLDS CURRENT VALUE OF THDT AS IT IS BEING REDUCED BECAUSE DELTA THETA IS TOO LARGE.	WATR 128
C		WATR 129
C THEVAP	EVAPORATIVE DEMAND, MM, WATER TO EVAPORATE FROM SURFACE DURING REMAINDER OF PMDT	WATR 130 WATR 131 WATR 132
C		WATR 133
C THFZEN	EQUALS .TRUE. IF SOIL PROFILE FROZEN, EQUALS .FALSE. IF NOT FROZEN.	WATR 134 WATR 135
C		WATR 136
C THF	TEMPORARY VARIABLE USED TO SET UP PWT ARRAY.	WATR 137
C		WATR 138
C THHA(10)	PRESSURE HEAD AT BEGINNING OF TWDT, BARS	WATR 139
C		WATR 140
C THHB(10)	PRESSURE HEAD AT END OF TWDT, BARS	WATR 141
C		WATR 142
C THHHA	INTERPOLATED VALUES OF PHH	WATR 143
C		WATR 144
C THIN	EQUALS .TRUE. IF SURFACE PRESSURE IS WITHIN LIMITS	WATR 145
C		WATR 146
C THJA	INTEGER USED IN PICKING VALUES OF K, H OFF TABLES	WATR 147
C		WATR 148
C THJB	INTEGER USED IN PICKING VALUES OF K, H OFF TABLES	WATR 149
C		WATR 150
C THJM	INTEGER COUNTER USED TO LIMIT NUMBER OF TWDT HALVINGS	WATR 151
C		WATR 152
C THKSA	INTERPOLATED VALUE OF PWKSUM	WATR 153
C		WATR 154
C THONE	EQUALS .TRUE. IF FIRST DELTA THETA APPROXIMATION HAS ALREADY BEEN DONE DURING CURRENT TWDT.	WATR 155
C		WATR 156
C THR	RAIN, MM, WATER TO INFILTRATE, LEAVE STANDING OR RUNOFF DURING REMAINDER OF PMDT.	WATR 157 WATR 158
C		WATR 159
C THRAIN	EQUALS .TRUE. IF RAIN OCCURS DURING TWDT	WATR 160
C		WATR 161
C THRP	EQUALS .TRUE. IF THRAIN WAS TRUE LAST TWDT.	WATR 162
C		WATR 163
C THSF	SURFACE FLUX OF WATER OR VAPOR, CM	WATR 164
C		WATR 165
C THSFB	FLUX OF WATER MOVING INTO PROFILE DURING TWDT THROUGH CALICHE, CM.	WATR 166 WATR 167
C		WATR 168
C THSFBT	FLUX OF WATER MOVING INTO PROFILE DURING PMDT THROUGH CALICHE, CM.	WATR 169 WATR 170
C		WATR 171
C THSFC	CALCULATED SURFACE FLUX USING THHB(1) AND PWK(1).	WATR 172 WATR 173


```

XWSTND=TWSTND                                WATR 805
C
C   CALCULATE SUM OF TRANSPERSION, CM          WATR 806
      DO 631 I=1,PMN-2                         WATR 807
      630 TWTHTS(I)=TWTHTS(I)+TWTSPR(I)        WATR 808
C
C   RESET TIMING                               WATR 809
      TWTTOT=TWTTOT+THDT                      WATR 810
C
      IF(ABS((TWTTOT-PMOT)/PMOT) .GT. 0.002) GO TO 60  WATR 811
C
C   FIND WRAP UP SECTION FOR THDT             WATR 812
      WATR 813
      WATR 814
      WATR 815
      WATR 816
      WATR 817
      WATR 818
      WATR 819
      WATR 820
      WATR 821
      WATR 822
      WATR 823
      WATR 824
      WATR 825
      WATR 826
      WATR 827
      WATR 828
      WATR 829
      WATR 830
      WATR 831
      WATR 832
      WATR 833
      WATR 834
      WATR 835
      WATR 836
      WATR 837
      WATR 838
      WATR 839
      WATR 840
      WATR 841
      WATR 842
      WATR 843
      WATR 844
      WATR 845
      WATR 846
      WATR 847
      WATR 848
      WATR 849
      WATR 850
      WATR 851
      WATR 852
      WATR 853
      WATR 854
      WATR 855
      WATR 856
      WATR 857
      ENTRY WINIT                                WATR 858
      WATR 859
      WATR 860
      WATR 861
      WATR 862
      WATR 863
      WATR 864
      WATR 865
      WATR 866
      WATR 867
      WATR 868
      WATR 869
      WATR 870
      WATR 871
      WATR 872
      WATR 873
      WATR 874
      WATR 875
      WATR 876
      WATR 877
      WATR 878
      WATR 879
      WATR 880
      WATR 881
      WATR 882
      WATR 883
      WATR 884
      WATR 885
      WATR 886
      WATR 887
      WATR 888
      WATR 889
      WATR 890
      WATR 891
      WATR 892
      WATR 893
      WATR 894

      READ(5,670)TWCCC
      WRITE(6,680)
      WRITE(6,690)TWCCC
      WRITE(6,700)

      C
      READ(5,670)TWCCC
      WRITE(6,690)TWCCC
      READ(5,/)PWDELW
      WRITE(6,710)PWDELW
      WRITE(6,700)

      C
      READ(5,670)TWCCC
      WRITE(6,690)TWCCC
      READ(5,/)PWH
      WRITE(6,720)PWH
      WRITE(6,700)

      C
      READ(5,670)TWCCC
      WRITE(6,690)TWCCC
      READ(5,/)PWKCAL
      WRITE(6,720)PWKCAL
      WRITE(6,700)

      C
      READ(5,670)TWCCC
      WRITE(6,690)TWCCC

```


SUBROUTINE WBAL

```

      SUBROUTINE WBAL( TSPR, SF, SFB, THTAI, THTAF, DX, PMN, WIN,
1      WSTRD, RATIO)
C
C THIS FUNCTION CHECKS WATER BALANCE OF A TIME PERIOD
C TSPR IS TRANSPERSION, CM
C SF IS TOP SURFACE FLUX (IN IS +)
C SFB IS BOTTOM SURFACE FLUX (IN IS +)
C THTAI IS THETA INITIAL, CM/CM
C THTAF IS THETA FINAL, CM/CM
C DX IS THICKNESSES OF LAYERS, CM
C PMN IS NUMBER OF SOIL NODES
C
C
      DIMENSION TSPR(PMN),THTAI(PMN),THTAF(PMN),DX(PMN)
      AM=0.0
      WSTRD=0.0
      DO1000 I=1,PMN-2
      ASA=TSPR(I)
1000 WSTRD=WSTRD+(THTAF(I+1)-THTAI(I+1))*DX(I)
      WIN = SF - A + SFB
      IF(ABS(WSTRD).LT.1,E=3)RATIO=99.9999
      IF(ABS(WSTRD).GE.1,E=3)RATIO=WIN/WSTRD
      RETURN
      END

```

FUNCTION WTIME

```
FUNCTION WTIME(Z)          PAUL LOMMEN           WTM 0100
C      MARCH 1976          THIS FUNCTION SIMPLY DETERMINES CPUTIME IN SECONDS. TIME(2) IS AN WTM 0200
C      INTRINSIC FUNCTION; TIME IS A VARIABLE NAME WE'VE WTM 0300
C      I HAD TO DO IT THIS WAY BECAUSE TIME IS A VARIABLE NAME WE'VE WTM 0400
C      ALREADY USED AND IS IN THE COMMON BLOCK, WTM 0500
C      TIME(2) IS IN 60THS OF A SECOND. 0.016667=1/60 WTM 0600
      WTIME=.016667*TIME(2)          WTM 0700
      RETURN          WTM 0800
      END          WTM 0900
                           WTM 1000
```

DERIVATION OF DIFFERENCE EQUATIONS

Soil nodes are introduced into the soil profile as reference points for the set of difference equations WATER will generate and then solve. This derivation will proceed very much as the derivation of difference equations for HEAT, since both Equations B-1 and C-1 are diffusion equations.

For a thin layer of soil we rather arbitrarily divide water movement into four components, for convenience:

$$(water \text{ in through top}) - (water \text{ out through bottom}) - (transpiration) = (water \text{ stored}). \quad (C-2)$$

For layer i :

$$(water \text{ in through top})_i = -K \frac{\partial h}{\partial z}, \quad (C-3)$$

where

the right-hand side is evaluated at the top of layer i ;

water moving down is a positive flow;

counting of layers starts at soil surface and goes down;

each side of Equation C-3 has units of $\text{cm} \cdot \text{day}^{-1}$;

K = soil hydraulic conductivity, $\text{cm}^2 \cdot \text{bar}^{-1} \cdot \text{day}^{-1}$;

H = soil hydraulic potential head, bars (includes matric potential plus gravitational potential);

z = depth in soil, cm.

Now fill out Equation C-3 as a difference equation:

$(water \text{ in through top})_i$

$$\begin{aligned} &= (-K_{i-1}) \left\{ \left[\frac{h_i - h_{i-1} + h_i^* - h_{i-1}^*}{2\Delta z_{i-1}} \right] \left(\frac{1}{2} \right) - \frac{(6)(\Delta z_{i-1})}{2} \right\}; \\ &= (-K_{i-1}) \left[\frac{h_i - h_{i-1} + h_i^* - h_{i-1}^* - 2G(\Delta z_{i-1})}{2\Delta z_{i-1}} \right], \quad (C-4) \end{aligned}$$

where

h_i = soil matric water potential (hereafter SWP) of layer i at beginning of time-step of length Δt days, located at the node in the center of layer i ;

h_{i-1} = SWP of layer $i-1$ at beginning of Δt ;

h_i^* = SWP of layer i at end of Δt ;

h_{i-1}^* = SWP of layer $i-1$ at end of Δt ;

$K_{i-1/2}$ = hydraulic conductivity of soil in region from center of layer $i-1$ to center of layer i (i.e., from node i to node $i+1$, see Fig. C-2);

G = constant to convert gravitational contribution to total soil hydraulic potential heat from cm water potential to bars, $= 9.833 \times 10^{-4} \text{ bar} \cdot \text{cm}^{-1}$;

$\Delta z_{i-1/2}$ = distance from node i to node $i+1$.

Similarly:

$(water \text{ out through bottom})_i$

$$= (-K_{i+1}) \left[\frac{h_{i+1}^* - h_i + h_{i+1} - h_i^* - 2G(\Delta z_{i+1})}{2\Delta z_{i+1}} \right]. \quad (C-5)$$

Transpiration in $\text{cm} \cdot \text{day}^{-1}$ is

$$(transpiration)_i = \frac{T_i}{\Delta t}, \quad (C-6)$$

where

T_i = transpiration removed from layer i during Δt , centimeters.

Water stored in $\text{cm} \cdot \text{day}^{-1}$ is

$$\begin{aligned} (water \text{ stored})_i &= \frac{(\Delta \theta_i)(\Delta x_i)}{\Delta t}; \\ &= \frac{(h_i - h_i^*)(S_i)(\Delta x_i)}{\Delta t}, \quad (C-7) \end{aligned}$$

where

$\Delta \theta_i$ = change in theta of layer i during Δt , dimensionless ($\theta_i = \text{cm water in layer } i / \text{cm soil in layer } i$);

Δx_i = thickness of layer i , cm;

S_i = specific water capacity of layer i during Δt , bar^{-1} , $S_i = \Delta \theta_i / \Delta h_i$.

In the same manner as in the HEAT submodel, combine Equations C-4, C-5, C-6 and C-7 with Equation C-2. After several lines of algebra we get

$$-C_i h_{i-1}^* + \theta_i h_i^* - A_i h_{i+1}^* = D_i, \quad (C-8)$$

where

$$C_i = \frac{\frac{K_{i-1}}{2}}{\frac{\Delta z_{i-1}}{2}}; \quad (C-9)$$

$$A_i = \frac{\frac{K_{i+1}}{2}}{\frac{\Delta z_{i+1}}{2}}; \quad (C-10)$$

$$B_i = A_i + C_i + \frac{2S_i \Delta x_i}{\Delta t}; \quad (C-11)$$

$$D_i = h_i \left(\frac{2S_i \Delta x_i}{\Delta t} - A_i - C_i \right) + h_{i-1} C_i + h_{i+1} A_i + 2G \left(\frac{K_{i-1}}{2} - \frac{K_{i+1}}{2} \right) - 2 \frac{T_i}{\Delta t}. \quad (C-12)$$

For top and bottom layers, adjustments must be made in Equations C-9 through C-12. The water in through the top of the top layer is the surface flux, as calculated in lines 537 through 594 of WATER, divided by Δt . Then, A_i , B_i , C_i and D_i are determined by going through the same sequence of steps which resulted in Equations C-9 through C-12. For the bottom layer the difference which must be accommodated is that the SWP below the layer is fixed.

Now summarize the equations for A , B , C , D for all layers. It is first convenient to define:

M = number of layers;

$$Y_i = K_{i-1} / \frac{\Delta z_{i-1}}{2}; \quad (C-13)$$

$$R_i = 2S_i \Delta z_i / \Delta t. \quad (C-14)$$

The result is a set of M equations of the form shown in Equation C-8, which form a tridiagonal matrix, where

$$A_i = Y_{i+1} \text{ for } i = 1, \dots, M-1; \\ = 0 \text{ for } i = M; \quad (C-15)$$

$$C_i = 0 \text{ for } i = 1; \\ = Y_i \text{ for } i = 2, \dots, M; \quad (C-16)$$

$$B_i = Y_2 + R_1 \text{ for } i = 1; \\ = Y_i + Y_{i+1} + R_i \text{ for } i = 2, \dots, M; \quad (C-17)$$

$$D_i = h_1(R_1 - Y_2) + h_2 Y_2 + \frac{2F}{\Delta t} - 2G \frac{K_3}{2} - \frac{2T_1}{\Delta t} \text{ for } i = 1; \\ = h_1(R_1 - Y_1 - Y_{i+1}) + h_{i-1} Y_i + h_{i+1} Y_{i+1} + 2G \left(\frac{K_{i-1}}{2} - \frac{K_{i+1}}{2} \right) - \frac{2T_i}{\Delta t} \text{ for } i = 2, \dots, M-1; \\ = h_M(R_M - Y_M - Y_{M+1}) + h_{M-1} Y_M + h_{M+1}^{**} (2 Y_{M+1}) + 2G \left(\frac{K_{M-1}}{2} - \frac{K_{M+1}}{2} \right) - \frac{2T_M}{\Delta t} \text{ for } i = M, \quad (C-18)$$

where

F = surface flux into top layer during Δt , cm;
 h_{M+1}^{**} = fixed potential of region below bottom layer, bars.

Finally, translate Equations C-15 through C-18 into computer code with the aid of Table C-2.

Table C-2. Transformation of algebraic to FORTRAN variables

Algebraic Variable	FORTRAN Variable (or Constant)
i	I
Δt	TWDT
F	TWSF
G	9.833E-4
M	PMN-2
K_{i-1}	PWK(I)
$\frac{\Delta z_{i-1}}{2}$	TWHA(I+2)
h_{i+1}	TWHB(I+2)
h_{i+1}^*	TWHB(PMN)
h_{M+1}	CHDX(I)
$\frac{\Delta z_{i-1}}{2}$	CHDX(I)
Δx_i	PWWC(I)
S_i	TWTSPR(I)
T_i	TWWA(I) = PWK(I)/CHDX(I)
Y_i	TWWB(I) = 2.*PWWC(I)*CHDX(I)/TWDT
R_i	TWA(I)
A_i	TWB(I)
B_i	TWC(I)
C_i	TWD(I)

Equation C-15 becomes

$$TWA(I) = TWHA(I+1) \text{ for } I = 1, \dots, PMN-3; \\ = 0 \text{ for } I = PMN-2. \quad (C-19)$$

Equation C-16 becomes

$$TWC(I) = 0 \text{ for } I = 1; \\ = TWWA(I) \text{ for } I = 2, \dots, PMN-2. \quad (C-20)$$

Equation C-17 becomes

$$TWB(I) = TWWA(2) + TWWB(I) \text{ for } I = 1; \\ = TWWA(1) + TWHA(I+1) + TWWB(I) \\ \text{for } I = 2, \dots, PMN-2. \quad (C-21)$$

And finally, Equation C-18 becomes

$$TWD(I) = TWHA(2)*(TWWB(I) - TWHA(2)) \\ + TWHA(3)*TWWA(2) + 2.*TWTSPR(I)/TWDT \\ - 2.*9.833E-4*PWK(2) - 2.*TWTSPR(I)/TWDT \\ \text{for } I = 1;$$

```

= TWHA(I+1)*(TWWB(I) - TWWA(I) - TWWA(I+1))
+TWHA(I)*TWWA(I) + TWHA(I+2)*TWWA(I+1)
+2.*9.833E-4*(PWK(I) - PWK(I+1))
-2.*TWTSPR(I)/TWDT
for I = 2, . . . , PMN-3;

= TWHA(PMN-1)*(TWWB(PMN-2) - TWWA(PMN-2) - TWWA(PMN-1))
+TWHA(PMN-2)*TWWA(PMN-2) + 2.*TWHB(PMN)*TWWA(PMN-1)
+2.*9.833E-4*(PWK(PMN-2) - PWK(PMN-1)) -2.TWTSPR(PMN-2)/TWDT
for I = PMN-2.                               (C-22)

```

Equations C-19 through C-22 are the FORTRAN versions of the difference equations used to solve for SWP of the soil layers. They are found in the program in lines 647 through 667 and immediately precede the call to the tridiagonal matrix subroutine which solves them.

LITERATURE CITED

- GRiffin, R. A., R. J. HANKS, and S. CHILDS. 1974. Model for estimating water, salt and temperature distribution in the soil profile. US/IBP Desert Biome Res. Memo. 74-61. Utah State Univ., Logan. 12 pp.
- HANKS, R. J., and S. A. BOWERS. 1962. Numerical solution of the moisture flow equation for infiltration into layered soils. Soil Sci. Soc. Amer. Proc. 26: 530-534.
- HANKS, R. J., A. KLUTE, and E. BRESLER. 1969. A numeric method for estimating infiltration, redistribution, drainage, and evaporation of water from soil. Water Resour. Res. 5:1064-1069.
- NIMAH, M. N., and R. J. HANKS. 1973. Model for estimating soil water, plant, and atmospheric interrelations. I. Description and sensitivity. Soil Sci. Soc. Amer. Proc. 37:522-527.
- RICHTMYER, R. D. 1957. Difference methods for initial value problems. Interscience Publ., New York.

D. SUPPORT PROGRAM TDM

P. W. Lommen

GENERAL DESCRIPTION OF SUBROUTINE TDM

This subroutine solves a set of N linear equations in N unknowns if the coefficients of the unknowns form a tridiagonal matrix. Difference equation approximations to the diffusion equation are typically of the tridiagonal type. The method used here is from Richtmyer (1957, page 103).

Briefly, this routine goes forward through the equations once, eliminating the $U(J)$ for the smallest J at each step. At the $N-1$ equation, one is left with two equations in two unknowns. Then $U(J)$ is solved for and the routine goes backwards through the equations solving for a value of U at each step.

$-A$, B , $-C$ are the coefficients of the U 's to the right of the main diagonal, on the diagonal and to the left of the diagonal, respectively; the D 's are the constant, right-hand sides of the equations. The U 's are the solutions. A , B , C , D must be evaluated in the routine which calls TDM.

PROGRAM DESCRIPTION

To illustrate the method of solution, first write out the equations:

$$B_1 U_1 - A_1 U_2 = D_1, \quad (D-1.1)$$

$$-C_2 U_1 + B_2 U_2 - A_2 U_3 = D_2, \quad (D-1.2)$$

$$-C_3 U_2 + B_3 U_3 - A_3 U_4 = D_3, \quad (D-1.3)$$

$$\dots$$

$$-C_N U_{N-1} + B_N U_N = D_N. \quad (D-1.N)$$

```
E(1) = A(1) / B(1)
F(1) = D(1) / B(1)
```

TDM 31
TDM 32

If Equation D-1.1 is divided by B_1 , we get

$$U_1 - (A_1/B_1)U_2 = D_1/B_1, \quad (D-2)$$

transposing we get

$$U_1 = (A_1/B_1)U_2 + (D_1/B_1) = E_1 U_2 + F_1. \quad (D-3)$$

```
00 10 I=2, N=1
DD = B(I) - C(I)*E(I-1)
E(I) = A(I) / DD
10 F(I) = (D(I) + C(I)*F(I-1)) / DD
```

TDM 33
TDM 34
TDM 35
TDM 36

To see how these equations came about, substitute Equation D-3 into Equation D-1.2 and solve for U_2 :

$$\begin{aligned} -C_2[E_1 U_2 + F_1] + B_2 U_2 - A_2 U_3 &= D_2, \\ (B_2 - C_2 E_1)U_2 &= D_2 + A_2 U_3 + X_2 F_1, \\ \text{or } U_2 &= E_2 U_3 + F_2, \end{aligned} \quad (D-4)$$

where

$$E_2 = A_2 / (B_2 - C_2 E_1), \quad (D-5)$$

and

$$F_2 = (D_2 + C_2 F_1) / (B_2 - C_2 E_1). \quad (D-6)$$

Continuing in this manner, we get

$$E_i = A_i / DD, \quad (D-7)$$

$$F_i = (D_i + C_i F_{i-1}) / DD, \quad (D-8)$$

where

$$DD = (B_i - C_i E_{i-1}), \quad (D-9)$$

and

$$U_i = E_i U_{i+1} + F_i. \quad (D-10)$$

The quantity DD is not subscripted because it is not needed again.

$U(N) = (C(N)*F(N-1) + D(N)) / (B(N) + C(N)*E(N-1))$

TDM 37

The last equation generated in the DO loop just discussed is

$$U_{N-1} = E_{N-1} U_N + F_{N-1}. \quad (D-11)$$

Substitute Equation D-11 into Equation D-1.N:

$$\begin{aligned} -C_N [E_{N-1} U_N + F_{N-1}] + B_N U_N &= D_N, \\ U_N = (C_N F_{N-1} + D_N) / (B_N - C_N E_{N-1}), \end{aligned} \quad (D-12)$$

which is what we have in line 37.

Since all the quantities on the right in Equation D-12 have been evaluated in the calling program or in TDM, U_N is thus determined.

```
I=N
20 I=I+1
      U(I) = U(I+1) * E(I) + F(I)
      IF ( I .GT. 1 ) GO TO 20
```

TDM 38
TDM 39
TDM 40
TDM 41

Once we know U_N from Equation D-12, then from Equation D-11 we get U_{N-1} . Proceeding backwards using Equation D-10 for $I = N-2, N-3, \dots, 2, 1$, we determine the remainder of the U 's.

COMPLETE PROGRAM LISTING

```

SUBROUTINE TDM(A, B, C, D, U, N)          TDM 01
C                                         TDM 02
C MARCH 1976 PAUL LOMMEN                 TDM 03
C                                         TDM 04
C THIS SUBROUTINE SOLVES A SET OF N LINEAR EQUATIONS IN N UNKNOWNNS   TDM 05
C IF THE COEFFICIENTS OF THE UNKNOWNNS FORM A TRI-DIAGONAL MATRIX.    TDM 06
C DIFFERENCE EQUATION APPROXIMATIONS TO THE DIFFUSION EQUATION ARE   TDM 07
C TYPICALLY OF THE TRI-DIAGONAL TYPE. THERE ARE SEVERAL MEANS OF     TDM 08
C SOLVING SUCH A SET OF EQUATIONS. THE MOST STRAIGHTFORWARD, AND THE   TDM 09
C ONE THAT I USE HERE AND HANKS USES IN SEVERAL OF HIS MODELS COMES    TDM 10
C FROM, ROBERT D. RICHTMYER, 1957, DIFFERENCE METHODS FOR            TDM 11
C INITIAL-VALUE PROBLEMS, INTERSCIENCE PUBLISHERS, INC., NEW YORK.   TDM 12
C SEE PAGE 103. NOTATION USED HERE IS RICHTMYERS'.                 TDM 13
C                                         TDM 14
C BRIEFLY, THIS ROUTINE GOES FORWARD THROUGH THE EQUATIONS ONCE,      TDM 15
C ELIMINATING THE U(J) FOR THE SMALLEST J AT EACH STEP. AT THE        TDM 16
C N=1 EQUATION ONE IS LEFT WITH 2 EQUATIONS IN 2 UNKNOWNNS, THEN     TDM 17
C U(N) IS SOLVED FOR AND THEN THE ROUTINE GOES BACKWARDS THROUGH THE   TDM 18
C EQUATIONS SOLVING FOR A VALUE OF U AT EACH STEP.                   TDM 19
C                                         TDM 20
C -A, C =C, ARE THE COEFFICIENTS OF THE U'S TO THE RIGHT OF THE MAIN   TDM 21
C DIAGONAL, ON THE DIAGONAL AND TO THE LEFT OF THE DIAGONAL           TDM 22
C RESPECTIVELY. THE D'S ARE THE CONSTANT, RIGHT HAND SIDES OF THE     TDM 23
C EQUATIONS. THE U'S ARE WHAT IS SOLVED FOR. A, B, C, D MUST         TDM 24
C BE EVALUATED IN THE ROUTINE WHICH CALLS TDM.                      TDM 25
C                                         TDM 26
C                                         TDM 27
C                                         TDM 28
C                                         TDM 29
C                                         TDM 30
C                                         TDM 31
C                                         TDM 32
C                                         TDM 33
C                                         TDM 34
C                                         TDM 35
C                                         TDM 36
C                                         TDM 37
C                                         TDM 38
C                                         TDM 39
C                                         TDM 40
C                                         TDM 41
C                                         TDM 42
C                                         TDM 43

DIMENSION A(20), B(20), C(20), D(20), E(20), F(20), U(20)
E(1) = A(1) / B(1)
F(1) = D(1) / B(1)
DO 10 I=2, N-1
  DD = B(I) + C(I)*E(I-1)
  E(I) = A(I) / DD
10 F(I) = (D(I) + C(I)*F(I-1)) / DD
  U(N) = (C(N)*F(N-1) + D(N)) / (B(N) - C(N)*E(N-1))
  I=N
20 I=I-1
  U(I) = U(I+1) * E(I) + F(I)
  IF (I .GT. 1) GO TO 20
  RETURN
END

```

LITERATURE CITED

RICHTMYER, R. D. 1957. Difference methods for initial value problems. Interscience Publ., New York.