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Code Generation: An Introduction to Typed EBNF

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CODE GENERATION: AN INTRODUCTION TO TYPED EBNF

by

Jason G. Young

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of the requirements for the degree

of

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in

Computer Science

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ABSTRACT

Code Generation: An Introduction to Typed EBNF

by

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Errors and inconsistencies between code components can be very costly in a software project. Efforts to reduce these costs can include the use of tools that limit human interaction with code by generating it from a description. This paper introduces two new works to address these issues: (1) an input specification called Typed EBNF (TEBNF), and (2) a prototype tool that demonstrates how TEBNF can be used to generate code. The tool generates code for a console application as described by a TEBNF grammar. An application built from the generated code will be able to receive input data, parse it, process it, and output it as needed.

(72 pages)
CONTENTS

<table>
<thead>
<tr>
<th>CHAPTER</th>
</tr>
</thead>
<tbody>
<tr>
<td>1 Introduction</td>
</tr>
<tr>
<td>1.1 Code Generation</td>
</tr>
<tr>
<td>1.2 TEBNF Input Specification and Code Generation Tool</td>
</tr>
<tr>
<td>2 Background and Related Works</td>
</tr>
<tr>
<td>2.1 Traditional Scanner and Parser Code Generation</td>
</tr>
<tr>
<td>2.2 Model-Based Parser Code Generation</td>
</tr>
<tr>
<td>3 Design</td>
</tr>
<tr>
<td>3.1 The TEBNF Language</td>
</tr>
<tr>
<td>3.2 Design Decisions</td>
</tr>
<tr>
<td>3.3 The TEBNF Code Generation Tool</td>
</tr>
<tr>
<td>3.4 Lexical Analysis and Parsing Code Generation</td>
</tr>
<tr>
<td>3.5 State Machine and Actions Code Generation</td>
</tr>
<tr>
<td>4 Implementing Tools with TEBNF</td>
</tr>
<tr>
<td>4.1 NITF File Parsing: A Real World Example</td>
</tr>
<tr>
<td>4.2 Test Cases</td>
</tr>
<tr>
<td>4.3 Results</td>
</tr>
<tr>
<td>4.4 Comparing C++ to TEBNF</td>
</tr>
<tr>
<td>5 Future Work</td>
</tr>
<tr>
<td>5.1 Optimizing the TEBNF Code Generation Tool</td>
</tr>
<tr>
<td>5.2 New I/O Methods</td>
</tr>
<tr>
<td>5.3 Runtime Graphical User Interface Generation</td>
</tr>
<tr>
<td>6 Conclusion</td>
</tr>
<tr>
<td>REFERENCES</td>
</tr>
<tr>
<td>APPENDICES</td>
</tr>
<tr>
<td>Appendix A TEBNF Syntax and Usage</td>
</tr>
<tr>
<td>Appendix B TEBNF Turing Completeness Proof</td>
</tr>
</tbody>
</table>
### LIST OF TABLES

<table>
<thead>
<tr>
<th>Table</th>
<th>Page</th>
</tr>
</thead>
<tbody>
<tr>
<td>4.1 Sample input and output data for the calculator.</td>
<td>27</td>
</tr>
<tr>
<td>4.2 Sizes of sample NITF 2.1 files sent to the test client.</td>
<td>30</td>
</tr>
<tr>
<td>4.3 Calculator Test Case Implementation Times</td>
<td>34</td>
</tr>
<tr>
<td>4.4 NITF File Client Test Case Implementation Times</td>
<td>35</td>
</tr>
<tr>
<td>4.5 Analysis results for the NITF file client test cases.</td>
<td>36</td>
</tr>
<tr>
<td>4.6 Analysis results for the calculator test cases.</td>
<td>36</td>
</tr>
<tr>
<td>4.7 P-values calculated from the analysis data of each test case.</td>
<td>36</td>
</tr>
<tr>
<td>A.1 TEBNF Elements.</td>
<td>51</td>
</tr>
<tr>
<td>A.2 TEBNF symbols, production rules, non-typed terminals, and typed terminals.</td>
<td>52</td>
</tr>
<tr>
<td>A.3 TEBNF production rule operators.</td>
<td>54</td>
</tr>
<tr>
<td>A.4 TEBNF arithmetic and comparison operators.</td>
<td>54</td>
</tr>
<tr>
<td>A.5 TEBNF inter-element operator.</td>
<td>55</td>
</tr>
<tr>
<td>A.6 TEBNF input/output specifiers.</td>
<td>57</td>
</tr>
<tr>
<td>B.1 List of 5-tuples describing UTM(4,6).</td>
<td>62</td>
</tr>
</tbody>
</table>
LIST OF LISTINGS

<table>
<thead>
<tr>
<th>Listing</th>
<th>Page</th>
</tr>
</thead>
<tbody>
<tr>
<td>A.1  A TEBNF Actions element.</td>
<td>56</td>
</tr>
<tr>
<td>A.2  A TEBNF Console Input element.</td>
<td>57</td>
</tr>
<tr>
<td>A.3  TEBNF grammar describing a calculator.</td>
<td>58</td>
</tr>
<tr>
<td>A.4  TEBNF grammar describing a UDP NITF 2.1 file transfer client.</td>
<td>60</td>
</tr>
<tr>
<td>B.1  Rogozhin’s UTM(4,6) implemented in TEBNF.</td>
<td>63</td>
</tr>
</tbody>
</table>
# LIST OF FIGURES

<table>
<thead>
<tr>
<th>Figure</th>
<th>Description</th>
<th>Page</th>
</tr>
</thead>
<tbody>
<tr>
<td>2.1</td>
<td>Example Yacc grammar rule matched to input.</td>
<td>5</td>
</tr>
<tr>
<td>2.2</td>
<td>Lex and Yacc Compilation Sequence</td>
<td>6</td>
</tr>
<tr>
<td>2.3</td>
<td>Traditional code generation process.</td>
<td>7</td>
</tr>
<tr>
<td>2.4</td>
<td>Model-based code generation process.</td>
<td>9</td>
</tr>
<tr>
<td>3.1</td>
<td>Architecture of the TEBNF prototype code generation tool.</td>
<td>16</td>
</tr>
<tr>
<td>3.2</td>
<td>Order of execution for code generated by the TEBNF code generation tool.</td>
<td>19</td>
</tr>
<tr>
<td>4.1</td>
<td>Concept of operations for NITF 2.1 format files.</td>
<td>22</td>
</tr>
<tr>
<td>4.2</td>
<td>TEBNF Implementation of the NITF 2.1 USE00A TRE</td>
<td>23</td>
</tr>
<tr>
<td>4.3</td>
<td>State machine representing a calculator.</td>
<td>26</td>
</tr>
<tr>
<td>4.4</td>
<td>State machine representing a NITF 2.1 UDP/IP file transfer client</td>
<td>29</td>
</tr>
<tr>
<td>4.5</td>
<td>TEBNF code generation tool output for the calculator test case.</td>
<td>31</td>
</tr>
<tr>
<td>4.6</td>
<td>TEBNF code generation tool output for the UDP NITF 2.1 file client test case.</td>
<td>31</td>
</tr>
<tr>
<td>4.7</td>
<td>Running the calculator test case.</td>
<td>32</td>
</tr>
<tr>
<td>4.8</td>
<td>Running the file server for the NITF 2.1 file client test case.</td>
<td>33</td>
</tr>
<tr>
<td>4.9</td>
<td>Running the NITF 2.1 file client test case.</td>
<td>33</td>
</tr>
<tr>
<td>4.10</td>
<td>Function token count for the file client test cases.</td>
<td>37</td>
</tr>
<tr>
<td>4.11</td>
<td>Function token count for the calculator test cases.</td>
<td>38</td>
</tr>
<tr>
<td>4.12</td>
<td>Function CCN for the file client test cases.</td>
<td>39</td>
</tr>
<tr>
<td>4.13</td>
<td>Function CCN for the calculator test cases.</td>
<td>39</td>
</tr>
</tbody>
</table>
CHAPTER 1

Introduction

Various defects in software can result from multiple developers working on the same code within a project [1]. Some errors introduced by the coding activities of developers may consist of behavioral differences within and between components and their interfaces [2–4]. Other errors stem from inadequate comprehension of project code, supported by the fact that developers spend 50% to 80% of their time understanding that code [5]. Furthermore, these kinds of misunderstandings can lead to bug fixes that inject more faults into code [3].

Comprehensive requirements analysis, design, and other good software development practices can prevent many post-delivery software problems [6], but cannot completely eliminate the possibility of human error. Even well designed projects can get mired in code implementation details that hinder or prevent developers from delivering on time and within budget.

1.1 Code Generation

Code generation tools can improve the software development process by generating well-organized code reducing implementation errors and inconsistencies [7]. Code generation has been shown to improve the productivity of developers, guarantee correctness of syntax, and decrease errors [8]. A compiler is a type of code generation tool that generates binary executables from code written in higher-level programming languages like C and C++. Some tools generate higher-level code instead of binary given a set of rules known as a grammar. This high-level generated code is then fed to a compiler to create a binary executable.

Domain specific code generation tools specialize in generating code for one part of an application’s overall implementation. Popular targets for specialized code generation include
lexical analyzers and parsers. One of the earliest code generation tools is the compiler-compiler (parser generator), a term first presented in the early 1960s [9].

1.2 TEBNF Input Specification and Code Generation Tool

The goal of this paper is to present a new input specification and code generation tool that addresses some of the issues not handled by commonly used code generators. This tool accepts a new input specification based on Extended Backus-Naur Form (EBNF) called Typed-EBNF (TEBNF) (see appendix A). The tool validates key features of TEBNF:

- Can describe input patterns that include a mixture of strings, numbers, and/or raw groupings of bytes.
- Integrates grammar rules with states and actions.
- Can specify different methods of receiving input and sending output.
- Can declare how raw input data should be unmarshaled into well-known types of specific sizes (in bytes).
- Can declare how well-known types should be marshaled back into their original format.
- Provides typed and non-typed EBNF terminals.
- Supports arithmetic and non-arithmetic operations inside grammar rules.
- Grammars match specific pieces of a given input to well-known types of varied sizes (in bits or bytes).
- Supports the use of variables.
- Is Turing complete (see appendix B).

The prototype code generation tool will demonstrate that it can generate a console application that can:

- Parse data from different kinds of inputs
• Process data to produce specific output(s)

• Direct output(s) to a network destination (UDP/IP), file, or console-based user-interface

• Support custom network protocol handling and interaction (UDP/IP)

• Provide a console-based user interface for the application
CHAPTER 2

Background and Related Works

The purpose of code generation tools is to help developers improve their productivity, ensure correctness of code syntax, and lessen the number of errors in software [8]. The input specifications of these tools introduce additional levels of indirection to solve these problems [10]. A range of tools have been created to generate code that can be complex and tedious to write by hand:

- Scanners
- Parsers
- Interpreters
- Compilers
- Graphical user interfaces

The TEBNF input specification shares some similarities to those accepted by other tools. In order to understand how TEBNF and the TEBNF code generation tool improves upon these approaches, a review of pertinent code generation tools and their input specifications is helpful.

2.1 Traditional Scanner and Parser Code Generation

Yacc (Yet Another Compiler Compiler) [11] is a popular tool first introduced in 1975 that generates LALR parsers given (1) a context-free grammar to describe input, (2) an action (code snippets) to run for each token grouping that matches a grammar rule, and (3) code to provide input tokens to the parser. This input specification is a hybrid between a declarative domain-specific language (i.e. a grammar) and an imperative programming
language like C [12–14]. Nevertheless, Yacc lacks the ability to read an input stream and convert it into tokens for parsing.

Lexical analyzer generators such as Lex and Flex must be used in conjunction with Yacc to accomplish this separate task of lexical analyzer generation [11, 15]. The practice of using separate tools to generate a lexical analyzer and parser means that input formats for each tool must be learned and used correctly to achieve the desired result. A benefit of the TEBNF input specification is that it describes how data is received and parsed (appendix A), allowing the TEBNF code generation tool to generate both lexical analysis and parsing code.

Figure 2.1 shows an example Yacc grammar rule matched to input formatted as military time. In this example, military_hour, minute, and second (all defined somewhere else in the grammar) describe specific parts of input data as military_time. When tokens match this rule, a code action is executed [11, 16].

Similar to Yacc is Bison [17,18], a Yacc-compatible parser generator that accepts any properly written Yacc grammar. Like Yacc, Bison-generated parsers read a sequence of tokens from a scanner generated by a lexical analyzer generator like Lex or flex.

To illustrate the steps of traditional parser generation using Lex and Yacc (figure 2.2) [11,15,16], a file is provided by the developer containing a set of patterns that define how to separate strings found in source data. This file is read by Lex, which uses these patterns to generate the C source code of a lexical analyzer. This newly generated lexical analyzer uses the patterns to identify specific strings in the input and split them into tokens to simplify processing.
A file containing grammar rules is provided by the developer to Yacc, which uses those rules to generate C source code for a syntax analyzer (i.e. parser). The syntax analyzer uses this grammar to transform the tokens output by the lexical analyzer into a syntax tree. The structure of this syntax tree implies the precedence and associativity of operators found within the tokens. The syntax tree is then traversed in depth-first order to generate the desired source code (figure 2.2) [16].

A predicated-LL(k) parser called ANTLR [19] was introduced by Parr and Quong in 1995. The ANTLR parser generator was advertised to be easier to use than generators like Yacc or Bison. An LL(k) parser is a top-down parser that parses from left to right, utilizing a look-ahead of k tokens. All parsing decisions are made solely from the next k tokens, which means that it does no backtracking.
The Hyacc (Hawaii Yacc) parser generator first released in 2008 supports complete LR(0), LALR(1), LR(1), and partial LR(k) [20, 21]. Hyacc is compatible with Yacc and Bison input grammars and works with Lex. The Hyacc parser generator is notable because it can resolve reduce/reduce conflicts through its implementation of the LR(1) parser generation algorithm [20]. Reduce/reduce conflicts occur when two or more rules in an input grammar apply to the same input sequence [22]. These conflicts are typically the result of a serious problem with an input grammar [22].

The traditional code generation process using a lexical analyzer generator in conjunction with a parser generator and actions code is shown in figure 2.3. This process illustrates the pattern used by many parser generation tools.

Figure 2.3: Traditional code generation process.

All of these parser generators provide an effective means to reduce human interaction with code. They have the added benefit of generating logical and syntactically correct code
as long as the grammar is correct. On the other hand, the input grammars used by these
parser generators cannot be used for lexical analysis of the parser input. Code actions
that generate output must be manually written and inserted into the generated code. The
inconvenience of editing generated code is avoidable in TEBNF because actions are defined
directly within TEBNF grammars (appendix A).

2.2 Model-Based Parser Code Generation

Model-based parser generators provide an alternative to traditional parser generators
using a model-based language specification. This kind of specification is explained by [23]
and [24] as starting with an abstract syntax model (ASM) embodying the main concepts of
a given language. One or more concrete syntax models (CSMs) are created from this ASM.
Each CSM defines specific details about the language being modelled. Elements within the
ASM can then be converted into their concrete representation using a mapping of the ASM
to its CSM(s). This mapping is created by annotating the ASM with pertinent constraint
metadata. With this mapping in place, any changes to the ASM by the user will cause the
language processor to automatically update to reflect those changes. Figure 2.4 illustrates
the model-based parser code generation process.

Since grammar specifications are not needed by model-based parser generators, they
can offer several advantages over traditional parser generators [24]:

- An easier language design process. Language design is decoupled from language pro-
  cessing because the language grammar is automatically generated.

- Non-tree structures can be modeled. This is different from traditional parser genera-
  tors that force users to model a tree structure.

- Some semantic checks like reference resolution can be automated.

- Handles references between language elements, as opposed to the traditional way of
  resolving references manually using a symbol table.
Model-based parser generators can behave in one of two ways based on the ASM used [24]: (1) as a traditional parser generator when an ASM representing a tree structure is used, or (2) as a model-based parser generator when an ASM representing a non-tree structure is used. The second possibility causes a model-based parser generator to begin the reference resolution process, resulting in an abstract syntax graph.

ModelCC is a model-based parser generator that accepts an annotated conceptual model as its input rather than a context-free grammar [23]. ModelCC uses this annotated model to generate a parser written in Java that automatically instantiates the language conceptual model [23, 25].

The process of generating a parser using ModelCC as explained by [24] begins with an ASM that is defined by classes representing language elements and the relationships between them. Metadata annotations are added to these language elements and their corresponding relationships to produce an ASM to CSM mapping. Reference resolution is performed to match referenced objects to their equivalent object instantiations. A parser is then generated that automatically instantiates the conceptual model.
ModelCC decreases human interaction with code by generating grammar code and lexical analysis code from an input model specification. Yet it is similar to other parser generators because it does not implicitly support specific input and output methods such as UDP/IP, etc. The TEBNF code generation tool differs from ModelCC (and the other tools reviewed in this chapter) because it is able to specify several input and output methods (appendix A).
CHAPTER 3

Design

The TEBNF language makes it possible to convert a software design into a specification that can be provided to the TEBNF code generation tool. The TEBNF code generation tool generates C++ code from TEBNF grammars that can be built by a C++ compiler into a functioning console application.

As mentioned previously, TEBNF abstracts some of the complexities of creating software with the aim of reducing defects in code. This chapter covers important design considerations and decisions that were critical to achieving the stated goals of TEBNF. Specifically, this chapter discusses the TEBNF language, design decisions, the TEBNF code generation tool, the architecture of the tool, and the code generation process.

3.1 The TEBNF Language

The TEBNF specification is composed of language constructs called elements. A TEBNF grammar is the combination of these elements and their contents to define an application. The primary function of each element type is to convey a specific type of functionality. Enforcing boundaries between different types of functionality (elements) results in greater scalability. There are five kinds of elements in the TEBNF specification:

- Input methods: a method of receiving data as input.
- Grammar sections: parses input data.
- Actions: action code to execute using data from other elements.
- State transition tables: defines the behavior of the program.
Subelements are language constructs that exist inside elements. Different kinds of subelements exist for each element type, and are enumerated in detail in appendix A. The glue that brings these elements together to describe an application is two-fold: 1) static variables that can be defined within grammar elements and used by other elements to get and store information, and 2) state transition table elements that use all of the other elements in a grammar to express the order of task execution.

The structure provided by elements and subelements in a TEBNF grammar are meant to help bridge the gap between design and implementation. From the perspective of a developer, a typical application might be represented as classes in an object-oriented language like C++. Frequently used input/output (I/O) functions in the program might be encapsulated within one or more classes that wrap frequently used I/O functionality. Data received and sent using these I/O functions would be parsed and processed by different classes structured according to a design modeled by a state machine. This kind of design could easily be represented in TEBNF using the appropriate I/O method elements to handle I/O, grammar elements to deal with lexical analysis and parsing of incoming and/or outgoing data, and a state transition table element to describe the state machine outlined in the design.

3.2 Design Decisions

Several important design decisions were made in order to improve function and reduce complexity in TEBNF. This section discusses why these design decisions were made, how these decisions influenced the design of TEBNF, and how these decisions affected the code generated from it.

3.2.1 Singleton Paradigm

One of the primary goals of TEBNF is to reduce the difficulty of translating high-level designs into grammars. With this goal in mind, elements have been designed to behave as singletons in TEBNF, as well as the code generated from them.
Multiple reasons and advantages exist for treating TEBNF elements and the C++
classes generated from them as singletons:

- **Lazy instantiation.** Singleton C++ classes make it possible to avoid allocating memory
  for element class objects until they are actually used in the generated code. This is
different from static initialization that allocates memory to a variable at the time of
declaration.

- **Thread synchronization.** Singletons can yield the best results in situations where
  multiple threads try to access the same resource. Thread-safe access to the singleton
object is achieved by locking a synchronization mechanism (e.g. mutex) inside it’s
getter function as it returns the static singleton object. This applies to code generated
from a TEBNF grammar because it is possible for multiple state table threads to need
access to the same subelement or static variable class members at the same time.

- **Instance control.** A singleton prevents other objects from instantiating their own
copies of the singleton object, ensuring that all objects access the same instance. This
simplifies the design process in TEBNF because grammar writers know exactly what
they are accessing in their grammar.

- **Flexibility.** Generated singleton element classes control the instantiation process.
  This control over the instantiation process gives them the flexibility to change the
process. Since TEBNF purposely abstracts these details from grammar writers, it is
advantageous for each element class to control the way it is instantiated based on how
it is used/interacts in the generated application code.

### 3.2.2 Input and Output Elements

Console applications typically get string or numerical input from users by displaying
questions and waiting for the user to type an answer. Attempting to determine the type
of input information in generated code could lead to incorrect interpretations of the input
type at run time. One technique that was considered to avoid this problem is to directly tie
grammar subelements or static variables to input subelements. This method proved to be unwieldy because grammar elements change during the natural process of writing a TEBNF grammar. Simply changing the name of a grammar subelement would require that name to be changed in every input subelement tied to it. This problem could be compounded as other input elements are created that contain subelements tied to the same grammar subelements or static variables. To resolve this problem, console input subelements tie each question string to a type (appendix A). The responsibility of knowing the expected input type falls to the grammar writer rather than a risky prediction.

Usage of console output elements in TEBNF was found to be simpler than console input. This is due to the fact that generated console output code performs a simple passing of output data to a C++ std::cout statement. Because std::cout easily handles outputting of numerical and string data, there is no need for special handling in TEBNF.

Support for sending and receiving data over UDP is achieved in TEBNF using UDP elements. The TEBNF language uses UDP I/O elements to abstract most of the details involved with setting up and using UDP sockets. Generated UDP I/O element classes prompt users for an IP address and port number before initiating UDP communication. It became apparent that a way was needed to indicate that a UDP output element should send data on the same socket instance used by an existing UDP input element to receive data. The ”AS” keyword expresses this relationship between two I/O elements of the same type. The ”AS” relationship defines an element that shares all of the same characteristics as another I/O element of the same type. Because TEBNF elements and their respective C++ element classes are singletons, all that is needed to represent this case in generated C++ code is a type definition of the I/O element in question (typedef). This reduces the number of C++ classes generated.

### 3.2.3 Actions Elements

Actions elements in TEBNF share two similarities with C++ functions. First, actions elements can have parameters, allowing arguments to be passed to them when called inside a state transition table element. Second, actions elements can contain multiple instructions.
Actions elements are essentially C++ code blocks that allow direct reference to subelements and static variables found in grammar elements. This means they have loose parsing requirements compared to other TEBNF elements so that the chosen C++ compiler can catch complex errors in actions element code. The syntax for accessing subelements defined inside other grammar elements can be found in appendix A.

Unlike C++ functions, actions elements cannot return values. This limitation serves to maintain the clear purpose of their usage in state tables and makes it clear that they are not intended to be used as the input or condition of a state.

3.3 The TEBNF Code Generation Tool

This report presents a prototype code generation tool that generates the lexical analysis, parsing, and actions code of a basic console application using a single TEBNF grammar as input. Generated applications accept user input where necessary and can provide meaningful status. The tool outputs a set of classes that:

- Accept input data through console, file, or UDP/IP.

- Provide a set of functions that unmarshal raw data into human-readable types such as numbers and strings, and can marshal it back into its original form.

- Use these unmarshal functions to match input data to pattern(s) specified in the grammar and convert them to human-readable values.

- Run one or more state machines with each on its own thread to receive data through input methods described in the grammar. As input data arrives, the state machine finds matches to grammar patterns and executes actions that produce the desired output.

- Provide a console-based user interface that prompts for input as needed and provides status.

The architecture of the TEBNF code generation tool consists of four stages, shown in figure 3.1. The TEBNF code generation tool is a console application that accepts three
arguments in order: (1) the path of the file containing a TEBNF grammar, (2) the path of directory where the tool will write generated code, and (3) the name to give to the generated application.

Figure 3.1: Architecture of the TEBNF prototype code generation tool.

Upon receiving these arguments, the tool reads the grammar file at the location provided to the tool. The grammar is lexically analyzed by the TEBNF scanner to produce a list of tokens, with some metadata attached to some tokens as needed.

The TEBNF parser syntactically analyzes these tokens using a recursive descent algorithm to verify correctness of format. A pointer to each element discovered by the parser is then added to a table for quick look up and inserted into a parse tree. Subelements discovered during this parsing stage are added to their parent elements and subelements as
they are found in the parse table and parse tree.

After all of the elements and subelements have been added to the parse table and parse tree, the TEBNF resolver traverses the subelements in the parse tree and their descendants to their furthest extent (leaves). This ensures that all subelements resolve to a terminal type or literal value.

Once all elements and their subelements have been resolved, the TEBNF code generator iterates through each element in order of declaration in the input grammar, and generates a C++ class or other appropriate C++ code. The name of each C++ source file corresponds to the element it was generated from. A CMakeLists.txt file is generated with these C++ source files so that CMake can be used to generate Microsoft Visual Studio 2013 solution and project files. For convenience, a _clang-format file is generated so that any clang-formatting (optional) follows the intended format.

3.4 Lexical Analysis and Parsing Code Generation

The TEBNF code generation tool generates a class for each I/O element (method) defined in a TEBNF grammar (see appendix A). These I/O classes perform no lexical analysis. TEBNF supports the receiving of input and/or sending of output through the console, files, or UDP/IP.

These I/O methods are a powerful feature of TEBNF and the TEBNF code generation tool because the tool automatically integrates the code to do I/O using these methods. The complexities of their usage are abstracted by the tool, which is one of the key advantages of TEBNF and the TEBNF code generation tool. Contrast this to the most common code generation tools, which do not provide this built-in I/O capability.

Lexical analysis and parsing is performed by the generated code in one step rather than separate steps. This is possible because of the way patterns are described in TEBNF grammar elements (see appendix A). A typical grammar element pattern is composed of groupings of bytes broken into sub-groupings of bytes. These sub-groupings can be translated into specific types (e.g. numbers, and strings) and literal values. The size in bits or bytes is defined in the grammar element based on its type.
Matching user-defined TEBNF grammar patterns to incoming data requires that one or more literal values be defined somewhere in the grammar. The value of a literal value makes it possible to find it in the input data. The size and type of that initial literal value is defined implicitly or explicitly in the grammar (e.g. 4-byte integer, etc.). Given the initial reference offset $\alpha_f$ of the literal $f$ and its size $z_f$, the offset of the literal or type immediately following it is defined as $\alpha_{f+1}$, where $\alpha_{f+1} = \alpha_f + z_f$. The offset of the literal or type defined immediately before $f$ can be defined as $\alpha_{f-1}$, where $\alpha_{f-1} = \alpha_f - z_{f-1}$ and $z_{f-1} \geq \alpha_f$. The data offsets of subsequent literals and/or types found before and after the initial reference offset are calculated based on the one after and before it, respectively.

When multiple patterns must be matched to incoming data, a separate grammar element must be written to describe each pattern. This design makes it possible to refer to any given pattern using its grammar element name, making it easy to distinguish from other grammar patterns in the same TEBNF grammar.

The prototype code generation tool translates each grammar element into a class that can (1) unmarshal raw input data into specific user-defined types, (2) verify matches to byte patterns in the raw input data, and (3) marshal the values stored in the grammar class back into their original form and byte ordering. Patterns in data arriving through TEBNF input methods are located by the state machine using unmarshal functions of grammar element classes. As data arrives through an input method, patterns are recognized in the data by the grammar classes and simultaneously unmarshaled into the data types of those classes. This means lexical analysis and parsing are performed in the same step, using a single TEBNF input (figure 3.2). This approach is different from traditional parser code generation methods. Traditional methods require the use of a lexical analyzer generator tool and parser generator tool; each with their own input specification formats (see figure 2.3).

### 3.5 State Machine and Actions Code Generation

Program behavior is defined in TEBNF using state machines, as shown in figure 3.2. State machines are represented in TEBNF using state transition table elements (see appendix A). A state machine in TEBNF describes the order of tasks executed by a single
Figure 3.2: Order of execution for code generated by the TEBNF code generation tool.

application thread. States are divided into a series of six steps. These six steps are given below, in the order they are expressed in TEBNF, which is the same order they are evaluated by the generated code:

1. A unique name that identifies the state and allows other states to reference it

2. A Boolean condition that can be either a grammar to match with input data or an explicit Boolean condition.

3. The method of input for receiving the input data (console, file, or UDP/IP).
4. The next state to jump to if the Boolean condition provided in the second step evaluates to true.

5. An output to send through the output method provided in the sixth step, an explicit code action to execute, or nothing.

6. The output method to send output specified in the fifth step. If an action or nothing was provided for the fifth step, then this step is empty as well.

These state steps shape the way TEBNF elements interact with each other and input data by determining (1) what input methods data is received on, (2) what parts of the received data match defined grammar patterns, (3) what method is used to output that data, and (4) what code actions are executed.
CHAPTER 4
Implementing Tools with TEBNF

This chapter focuses on the implementation of applications using TEBNF and the TEBNF code generation tool. The chapter is divided into four sections. The first section will showcase a real world example using a TEBNF grammar to parse data from a National Imagery Transmission Format (NITF) version 2.1 file. The second section will walk through the implementation of two test cases. The third section will cover the testing and verification of these test cases. The fourth section of the chapter will cover the results of testing.

4.1 NITF File Parsing: A Real World Example

Software developers are oftentimes tasked to write software that parses and processes data in different formats. A well-known example is word processing software. Word processing software must be able to open and read documents structured in its own proprietary format and others (e.g. pdf, txt, etc.). Creating software that reads specific data formats requires access to documentation detailing the exact structure of each format.

An example data format read by different applications is the NITF 2.1 file format. The NITF 2.1 file format is part of a suite of standards established by the United States (US) Government for formatting digital imagery [26]. Documentation detailing the NITF 2.1 standard is freely available for download from the Geospatial Intelligence Standards Working Groups website [27]. This file format is compatible with software used by members of the intelligence community, which includes the US Department of Defense (DoD) [26]. The VANTAGE™ software suite produced by the Space Dynamics Laboratory and the SOCET Services suite produced by BAE Systems are all capable of reading and exploiting NITF 2.1 formatted files [28,29].

As explained by [26], the stated purpose of the NITF 2.1 file format is to provide the
intelligence community an interoperable means of transmission and/or storage of electronic imagery data. The NITF 2.1 format is intended to be used in the dissemination of imagery derived intelligence data. A general concept of operations involving NITF data is shown in figure 4.1. First, imagery data in NITF 2.1 format is requested by a member of the intelligence community. Second, the NITF data is received and combined with other collateral information to create intelligence report file(s) and/or products containing the requested information of interest. Third, these report files and/or products are given to the requestor of that intelligence information.

Exploiting NITF 2.1 files requires a detailed understanding of the format. With this understanding, it is possible to create software than can parse NITF 2.1 files to find information of interest, generate report files, and/or products.

The NITF 2.1 file format is composed of a file header and one or more segments. Each segment contains a subheader with data fields. Each data field has a specific size and format (depending on the type of field) and is located at a specific byte offset within the file.

Conditional data and/or data characteristics can be added to NITF 2.1 files. This
flexibility to extend the format is done using conditional fields in the file header and sub-
headers indicating the existence of Tagged Record Extensions (TREs) and Data Extension
Segments. Tagged Record Extensions contain data fields, while extension segments can
contain data in new formats.

Figure 4.2: TEBNF Implementation of the NITF 2.1 USE00A TRE (TRE information
taken from [30]).

As stated previously, various applications such as Vantage and SOCET glean data from
NITF 2.1 formatted files for exploitation (figure 4.1). This can also be done using a TEBNF
grammar as demonstrated in figure 4.2. The figure shows a side-by-side comparison of the
NITF 2.1 USE00A (Exploitation Usability Extension Format) TRE [30] to its equivalent
implementation in TEBNF. Each data field for this TRE is compared to its equivalent
TEBNF grammar expression. This comparison highlights several important advantages of using TEBNF to implement parsers of specifications like NITF:

- Convenience. There is no need to keep track of the offset of each data field because it is determined based on the size of each type.

- Readability. TEBNF grammar syntax looks very similar to actual specifications as shown in figure 4.2, making it is easier to understand.

- Self-documenting. Since TEBNF grammar syntax ties the size of each data field to the size of the subelement type, the grammar helps to document itself.

4.2 Test Cases

In order to verify the functionality of the TEBNF language, two case studies were implemented. Both case studies showcase the strengths of TEBNF and the TEBNF code generation tool. Further case studies are possible because TEBNF is Turing complete (see appendix B).

4.2.1 Basic Calculator

The first test case was to create a basic calculator console application that supports addition, subtraction, multiplication, and division of integers. Producing this calculator required the tool to generate code that:

1. Parses numeric data received over a console input.

2. Makes calculations based on the data received from that console input.

3. Sends the results of those calculations to console output.

4. Allows the user to exit when finished.

The calculator begins with a step executed once at the beginning of the program. This initial step prompts users to enter a number, which is then saved as an initial result value because all subsequent math operations are executed against it. From this point onward,
the calculator repeats a cycle that 1) asks for a number, 2) asks for a math operator, 3) applies that math operator against the saved result and the last number entered, 4) saves the result, and 5) displays that result. This cycle then repeats until the user enters a = operator, which then displays the result and exits the program.

Input for the calculator is achieved with a single TEBNF console input element containing two prompt values. The first is used for prompting the user to enter a number, accepting a signed 64-bit integer. The second one is used for prompting the user to enter a single character (math operator). Outputting the result of math operations is accomplished with a single TEBNF console output element.

Acceptable input values for the calculator are limited to integers or one of five math operator characters (+, -, *, /, =). TEBNF grammar elements are defined for each math operator. Another grammar element was created to represent a signed 64-bit integer, providing a place to store integers as they are unmarshaled from input. The saved result value is represented as a static variable within the number grammar element, serving as a place to store the result of each math operation. An actions element was created for each of the supported math operators. Each actions element adds, subtracts, multiplies, divides, or sets the saved result using the last unmarshaled integer.

The last TEBNF element included in the grammar describes the calculator as a state machine utilizing the elements described above to define the execution path of the calculator. The TEBNF grammar that implements this calculator is provided in listing A.3.

The calculator state machine is represented with five states, as shown in figure 4.3. The first state of the machine is a special case entered only once at the beginning of execution. This initial state is a necessary special case that sets the ongoing result value for subsequent math operations. In this state the user is prompted to enter the initial number via the console input element. The number grammar element unmarshals this input value as a signed 64-bit integer and retains a copy for later use. The state table then executes an actions element. This actions element sets the result static variable equal to the unmarshaled value while the machine transitions to the next state.
After setting the result value while transitioning to the first state of the main cycle, the machine uses the console input element to prompt the user to enter a number again. This number is also unmarshaled from input and stored as before. The state machine then transitions to the next state.

This state uses the console input element to prompt the user to enter one of the supported math operators. The state machine does this by moving through a series of else-if states. Each state uses one of the math operator grammar elements to check the same console input for a match to one of the supported math operations. A match occurs when a grammar successfully unmarshals the input value. Upon matching an operator the machine transitions to the print state and executes an actions element applying that operator to the result and unmarshaled number, then assigns it to the result. As the print state transitions to the first state of the main cycle, an actions element is executed that writes the result to the console. The cycle then continues to repeat until the user enters a
’=’ to exit. Otherwise, if a ’=’ operator was matched, the result is written to the console as the state machine transitions to the done state. If the input matched nothing, the state machine transitions to the done state.

Table 4.1: Sample input and output data for the calculator.

<table>
<thead>
<tr>
<th>Operand</th>
<th>Operator</th>
<th>Result</th>
</tr>
</thead>
<tbody>
<tr>
<td>5</td>
<td></td>
<td></td>
</tr>
<tr>
<td>10</td>
<td>+</td>
<td>15</td>
</tr>
<tr>
<td>95</td>
<td>-</td>
<td>-80</td>
</tr>
<tr>
<td>110</td>
<td>+</td>
<td>30</td>
</tr>
<tr>
<td>10</td>
<td>/</td>
<td>3</td>
</tr>
<tr>
<td>111</td>
<td>*</td>
<td>333</td>
</tr>
<tr>
<td>33</td>
<td>-</td>
<td>300</td>
</tr>
<tr>
<td>20</td>
<td>/</td>
<td>15</td>
</tr>
<tr>
<td>5</td>
<td>*</td>
<td>75</td>
</tr>
<tr>
<td>0</td>
<td>=</td>
<td>75</td>
</tr>
</tbody>
</table>

Suppose this calculator is run using the sample data in table 4.1. The first line in the table is the initial value 5. The second operand entered by the user is the number 10. The ’+’ operator is entered by the user, and the result displayed is 15. Entering the next value of 95 followed by the operator ’-’ displays the number -80. This cycle continues until the user enters the ’=’ operator.

4.2.2 NITF 2.1 UDP/IP File Transfer Client

The second test case is a file transfer client that receives NITF 2.1 files over UDP/IP upon requesting them from a file server. The server tells the client when it is done sending files so the client knows when to exit. This requires the tool to generate code for a file client that:

1. Asks the server to send it a file by sending it a message over a UDP/IP output.

2. Receives the NITF 2.1 file from the server over a UDP/IP input.

3. Uses the file length data field in the NITF 2.1 file to determine that it has received the entire file from the server as it was sent over UDP/IP.
4. Writes that file to disk using a file output.

5. Quits upon receiving a message from the server that says it is done sending files.

The NITF 2.1 file transfer client starts by prompting the user to enter the IP address and port that will be used for sending and receiving data over UDP/IP. After entering this information, the client immediately sends the message "send" to the server to request that it send a file. Once the server receives the "send" message from the client, it reads a NITF 2.1 file from disk and begins sending it to the client over UDP/IP. As the client receives data from the server, it continually checks to see if it has received the entire NITF 2.1 file from the server. The client knows a file transfer is complete when it has received the amount of data specified in the NITF files file length data field. The client then prompts the user to enter a path including the file name specifying where the file will be written to disk. After writing the file to disk, the client requests the next file from the server.

Allowed input values for the client are limited to a string for the IP address, an unsigned integer for the port, and strings for file paths. All other input to the client comes from the server through a TEBNF UDP/IP input element. A UDP/IP output element is used by the client to send data to the server. One file output element is used by the client for writing files to disk received from the server.

A grammar element was created to find NITF 2.1 files in data received over UDP/IP. The beginning of each NITF 2.1 file can be found by searching for the byte sequence "NITF02.10", which is always found at the beginning of each file. The NITF 2.1 file header has a data field containing the length of the file. This is leveraged by the TEBNF grammar element to calculate the end offset of each file. A second grammar element was created for finding the "done" message in incoming data. A third grammar was created to define the send message. The TEBNF grammar that implements this file transfer client is provided in listing A.4.

The file transfer client can be represented as a state machine with three states, as shown in figure 4.4. While transitioning from the first state to the second, the send message is sent via the UDP/IP output element to the file server.
The second state looks at data received from the file server over the UDP/IP input element to determine if it contains a NITF 2.1 file or the "done" message. If the incoming data contains a NITF file, the state machine writes it to the file output element while transitioning to the back to the first state which tells the server to send the next file, which prompts the user for a path to write the file to. The state machine then transitions back to the first state which tells the server to send the next file. If the incoming data does not contain a file, an "else-if" case in this same state checks for the done message. If the done message was received, the machine writes a message to the console output telling the user that all files have been received, after which the machine transitions to the quit state and exits.
In a hypothetical case, assume there are five NITF 2.1 files to be sent to a test case file client. Each file has a specific file size, as shown in table 4.2.

Table 4.2: Sizes of sample NITF 2.1 files sent to the test client.

<table>
<thead>
<tr>
<th>NITF 2.1 File Size (bytes)</th>
</tr>
</thead>
<tbody>
<tr>
<td>828710</td>
</tr>
<tr>
<td>4021118</td>
</tr>
<tr>
<td>912294</td>
</tr>
<tr>
<td>3516054</td>
</tr>
<tr>
<td>998822</td>
</tr>
</tbody>
</table>

The NITF 2.1 file server would be started and begin listening on its UDP/IP socket for the "send" request from a client. The test case file client is then started and immediately sends a "send" request to the server, and a file transfer begins. The UDP server reports the size in bytes of each file sent. The file client writes each file to local disk. The size in bytes of each file received corresponds to the size the files sent by the server.

4.3 Results

C++ code was successfully generated by the TEBNF code generation tool for each of the test cases. The TEBNF code generation tool provides useful output when it generates code from a supplied input grammar. The tool displays information indicating when each stage of the code generation process finishes. Status for the generation stage displays the classes generated for each element. After the generation stage finishes and all of the code has been generated, the tool reports success and the number of element files generated. Console output from generating code for the calculator test case and the NITF 2.1 file client test case is shown in figures 4.5 and 4.6.

A CMakeLists.txt file was correctly generated by the TEBNF code generation tool for each test case, and CMake version 3.0.2 was run using those CMakeLists files to generate Microsoft Visual Studio 2013 solution and project files. The project files generated by CMake for both test cases were successfully opened and built in Microsoft Visual Studio 2013.
Figure 4.5: TEBNF code generation tool output for the calculator test case.

Figure 4.6: TEBNF code generation tool output for the UDP NITF 2.1 file client test case.
4.3.1 Calculator

The calculator test case executable was run using the test data from table 4.1. As expected, the input and output of the calculator (figure 4.7) matched what is defined in table 4.1. This means the behavior of the calculator test case matches the behavior defined in the TEBNF grammar it was generated from.

![Calculator Output](image)

Figure 4.7: Running the calculator test case.

4.3.2 NITF 2.1 File Client

The NITF 2.1 file client test case executable was run using the five sample NITF 2.1 files whose sizes are found in table 4.2. A NITF 2.1 file server was created that listened for client "send" requests over a UDP/IP socket on localhost port 10042. This server was
started, then the test case client was started and configured to send requests and receive file transfers on localhost port 10042. The expected outcome occurred, with the server successfully sending five files as indicated by the first five send messages output by the server in figure 4.8. This was followed by the last four byte "done" message is sent to notify the client it was done sending. The same five files were received by the client which prompted for a file name to save each file as shown in figure 4.9. After saving the files, the client exited because the server had sent the "done" message.

The sizes of the files received were an exact match to the file sizes listed in table 4.2, as the output of the server and client test case executables show in figures 4.8 and 4.9, respectively. This verifies that the behavior of the NITF 2.1 client test case matches the
behavior defined in the TEBNF grammar it was generated from.

4.4 Comparing C++ to TEBNF

A non-generated C++ implementation of each test case was also written. The state machines described in chapter 3 for both test cases served as the starting point of each implementation. Using the same design as the generated test cases, a baseline was established for more direct comparisons.

4.4.1 Test Case Experience

The non-generated C++ implementation of both test cases was verified by following the procedures outlined in subsections 4.3.1 and 4.3.2. Each was verified to have the same behavior and output as the test cases generated from TEBNF.

The TEBNF grammar for each test case was significantly shorter than its manual C++ counterpart. The non-generated C++ implementations had fewer lines of code than their counterparts generated from TEBNF. These results were expected because the TEBNF code generation tool does not yet perform optimization.

Writing code to handle I/O and input verification took longer in C++ than TEBNF, which only requires a declaration to setup any of the supported I/O methods. Though this inconvenience was observed while writing the calculator test case in C++, it was far more noticeable while writing the client. The client uses three different I/O methods whereas the calculator only uses one. It is evident that a more complicated application can be more convenient to write in TEBNF than C++. The time it took to implement both test cases in C++ and TEBNF are listed in tables 4.3 and 4.4.

Table 4.3: Calculator Test Case Implementation Times (measured in hours).

<table>
<thead>
<tr>
<th>Item to Implement</th>
<th>C++</th>
<th>TEBNF</th>
</tr>
</thead>
<tbody>
<tr>
<td>Console I/O</td>
<td>1</td>
<td>0.1</td>
</tr>
<tr>
<td>State Machine</td>
<td>1</td>
<td>0.5</td>
</tr>
<tr>
<td><strong>Total</strong></td>
<td><strong>2</strong></td>
<td><strong>0.6</strong></td>
</tr>
</tbody>
</table>
Table 4.4: NITF File Client Test Case Implementation Times (measured in hours).

<table>
<thead>
<tr>
<th>Item to Implement</th>
<th>C++</th>
<th>TEBNF</th>
</tr>
</thead>
<tbody>
<tr>
<td>Console I/O</td>
<td>1</td>
<td>0.1</td>
</tr>
<tr>
<td>File I/O</td>
<td>1</td>
<td>0.1</td>
</tr>
<tr>
<td>UDP/IP I/O</td>
<td>4</td>
<td>0.5</td>
</tr>
<tr>
<td>State Machine</td>
<td>4</td>
<td>1</td>
</tr>
<tr>
<td><strong>Total</strong></td>
<td><strong>10</strong></td>
<td><strong>1.7</strong></td>
</tr>
</tbody>
</table>

Another disparity in coding effort was observed while writing the NITF file parser in C++. Creating NITF parsing code in C++ took a lot more effort than in TEBNF. The non-generated implementation required calculation of an offset whenever it was necessary to jump to a specific location in the NITF file. Calculation of this offset requires knowledge beforehand of the size and position of each field. On top of this, fields in the NITF standard can vary in length and be of different formats, as explained in section 4.1. Compare this effort to the TEBNF implementation found in listing A.4 which made it possible to write a parser resembling the actual specification document itself.

4.4.2 Test Case Analysis

A widely accepted metric for measuring code complexity is McCabe’s Cyclomatic Complexity [31]. This metric was derived from graph theory by McCabe to measure the number of control flow paths in a code module [31]. McCabe’s Cyclomatic Complexity is \( e - n + 2 \), where \( e \) is the number edges in the control flow graph and \( n \) is the number of nodes [31]. An example of its use proposed by [32] employs McCabe’s Cyclomatic Complexity metric to effectively predict defects in code modules.

The Lizard code complexity analyzer [33] tool was used to analyze each test case. The analysis results from the tool contained several valuable metrics, including the average cyclomatic complexity number (CCN) [33] of every function in the test cases. The analysis results of each test case are provided in tables 4.5 and 4.6. Values related to the interquartile range (IQR) were calculated from the analysis data of each test case, including the...
lower (first) quartile (Q1) corresponding to the 25\(^{th}\) percentile, the higher quartile (Q3) corresponding to the 75\(^{th}\) percentile, and the median. In order to focus on the most relevant analysis data, the upper limit ($U_{CCN}$) and lower limit ($L_{CCN}$) of each data set was calculated as $Q_3 + 1.5(IQR)$ and $Q_1 - 1.5(IQR)$, respectively.

Table 4.5: Analysis results for the NITF file client test cases.

<table>
<thead>
<tr>
<th>Test Case</th>
<th>Avg. CCN</th>
<th>$U_{CCN}$</th>
<th>Avg. Token Count</th>
<th>Func. Count</th>
</tr>
</thead>
<tbody>
<tr>
<td>Generated</td>
<td>2.00</td>
<td>3</td>
<td>54.49</td>
<td>136</td>
</tr>
<tr>
<td>Non-generated</td>
<td>3.38</td>
<td>6</td>
<td>101.81</td>
<td>16</td>
</tr>
</tbody>
</table>

Table 4.6: Analysis results for the calculator test cases.

<table>
<thead>
<tr>
<th>Test Case</th>
<th>Avg. CCN</th>
<th>$U_{CCN}$</th>
<th>Avg. Token Count</th>
<th>Func. Count</th>
</tr>
</thead>
<tbody>
<tr>
<td>Generated</td>
<td>1.89</td>
<td>3</td>
<td>49.50</td>
<td>135</td>
</tr>
<tr>
<td>Non-generated</td>
<td>3.42</td>
<td>7</td>
<td>81.42</td>
<td>12</td>
</tr>
</tbody>
</table>

The data in tables 4.5 and 4.6 show differences between the generated and non-generated test cases. Compared to the non-generated C++ implementations, the test cases generated from TEBNF have (1) more functions, (2) a lower average number of tokens per function, and (3) a lower average CCN per function.

Table 4.7: P-values calculated from the analysis data of each test case.

<table>
<thead>
<tr>
<th>Test Case</th>
<th>$P_{CCN}$</th>
<th>$P_{TokenCount}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>File Client</td>
<td>0.041236</td>
<td>0.007916</td>
</tr>
<tr>
<td>Calculator</td>
<td>0.017212</td>
<td>0.043956</td>
</tr>
</tbody>
</table>

Tables 4.5 and 4.6 illustrate the similarity in CCN values measured by the analysis tool for generated and non-generated code. According to [34], CCN values $\leq 10$ fit inside the low risk category. Given that (1) the non-generated test cases were built specifically to mimic the behavior of the generated test cases, (2) the average CCN values for all of the test cases fall into the low risk category, and (3) are close to one another in value, it can be concluded that the non-generated test cases are comparable to their generated counterparts.
Analysis data for the generated and non-generated test cases also show that they are provably different despite their similarities. Table 4.7 contains the p-values calculated from the data sets of each test case. All of the p-values are significant at $p < 0.05$, supporting the conclusion that the data sets (the test cases) are different from one another.

![Figure 4.10: Function token count for the file client test cases (omits outliers).](image)

Tables 4.5 and 4.6 show that the generated code has a lower average token count per function than the non-generated code (figures 4.10 and 4.11). The first conclusion to be drawn from the data as plotted in these figures is that the generated code is splitting larger computational problems into smaller tasks. This conclusion can be drawn based on the fact that lower median values within smaller data spreads point to a greater number of functions with lower token counts.

The lower average CCN for generated code (tables 4.5 and 4.6) is the strongest indicator that larger computational problems are being broken down into smaller ones. Figures 4.12 and 4.13 show that the median CCN for the generated test cases are at or below the lowest values measured for the non-generated test cases. Given that [32] was able to use CCN values to detect the presence of defects in code, and that the generated code has shorter interquartile ranges paired with medians at or below the lowest quartiles of the non-generated
code, it can be concluded that a greater number of functions in the code generated from TEBNF have a lower number of defects than the non-generated code. This correlation of fewer defects per function in generated code means it is likely that as applications increase in size and scope, the number of defects will remain lower than application code not generated from TEBNF.

More than one participant is needed in order to conduct tests that are statistically significant. Nevertheless, the trends observed in the analysis are interesting and worthy of future investigation.
Figure 4.12: Function CCN for the file client test cases (omits outliers).

Figure 4.13: Function CCN for the calculator test cases (omits outliers).
CHAPTER 5

Future Work

Code generation using TEBNF creates several possibilities for future work. As mentioned in subsection 4.4, the TEBNF code generation tool can likely be optimized to produce better code. Another possibility is to add more I/O methods to TEBNF and the TEBNF code generation tool. There are many different ways to receive input and send output beyond what is currently supported by TEBNF and the tool. The last improvement covered in this chapter is to add support into the TEBNF code generation tool to automatically generate graphical user interfaces at runtime.

5.1 Optimizing the TEBNF Code Generation Tool

Many different compiler optimizations could be applied to the code generated by the TEBNF code generation tool. A likely side-effect of optimization is a reduction in the number of lines of code produced by the tool.

Some of the optimizations described by [35] could be applied to code generated by the tool. The C++ compiler that builds the generated code will likely apply many if not all of the optimizations to the actions code. The side-effects of poorly defined grammars is another factor to take into consideration. For non-actions code, other optimizations described by [35] could be applied including instruction combining, expression simplification, branch elimination, and dead code elimination.

Instruction combining is the process of combining two or more instructions into one. Expression simplification is the process of replacing expressions with more efficient ones. Both of these optimizations could be applied to marshaling/unmarshaling code generated from grammar elements that are poorly defined by the user.

Branch elimination is an optimization that removes unnecessary branches to other
branches. A form of branch elimination could be applied to generated state machine code when states transition to other states unnecessarily.

In some cases, the code generation tool might generate empty actions function(s). When this happens, dead code elimination could be employed to avoid generating them or calling them.

5.2 New I/O Methods

A wide range of I/O methods could be added to TEBNF. This could include adding support for interacting with relational databases. Support for commonly used database query languages like MySQL and PostgreSQL would allow TEBNF to interact with a wide range of systems that utilize databases.

The TCP/IP protocol is widely used and could be adapted into a set of I/O methods. Due to the fact that TCP/IP is connection-oriented, I/O methods would be needed that support both server and client I/O.

5.3 Runtime Graphical User Interface Generation

Support for automatic GUI generation could be integrated into the TEBNF code generation tool. Console user interfaces for generated applications would be replaced with a web-based GUI that communicates with the generated application. The code generation process would need to employ a runtime data mining technique called software mining [36,37], which is a form of data mining that focuses on the inspection of static and runtime software information characteristics. Some examples of static characteristics include source code files and database schemas, while runtime characteristics include polymorphic data-types, data values, and the reading and modification of an instantiated objects current state.

Software mining [36,37] would probably take place during all phases of the TEBNF code generation process. Static characteristics could be gleaned from tokens as they are read from the input grammar and used to identify runtime characteristics in the parse tree. These characteristics would then be used to map element and subelement objects to their appropriate GUI controls during the syntactic analysis phase. Once this mapping
is complete, the control(s) of the GUI are determined and the appropriate code can be generated.
CHAPTER 6

Conclusion

Errors and inconsistencies between code components can be very costly in a software project. It has been shown that the use of code generation tools can simplify and possibly reduce these errors and inconsistencies. Many tools generate only one of the many components found in a typical application. This report explored the benefits of using TEBNF as the sole input specification for the TEBNF code generation tool.

The TEBNF input specification integrates lexical analysis and parsing input specifications into one format. TEBNF also simplifies the implementation of applications that receive, parse, process, and output data through various I/O methods. Many complexities involved with designing and coding applications can be abstracted using TEBNF.

The prototype TEBNF code generation tool demonstrated the effectiveness of TEBNF as an input specification. The tool generates C++ classes that handles I/O over console, file, or UDP/IP, thereby abstracting the complexities of their usage through TEBNF. Parsing documented formats like the NITF 2.1 format is greatly simplified using TEBNF.
REFERENCES


APPENDICES
Appendix A

TEBNF Syntax and Usage

A.1 TEBNF Grammar Syntax

Like standard EBNF, Typed EBNF (TEBNF) is used to express a context-free grammar that consists of non-terminal production rules and terminal symbols that may or may not have a type. The typing of terminal symbols makes it possible to describe exactly how the input is recognized, yet preserves the simple syntax of EBNF. TEBNF provides a set of input and output methods, grammar rules, and actions, tied together to a set of states using a state transition table. It allows users to:

- Describe how the input data will be sent to the generated application (UDP, file, or in-memory).
- Describe when and how responses will be sent to the sender as needed by the specified protocol.
- Describe what the input data sent to the generated application will look like. This combines the traditional specification of lexical and syntactic analysis.
- Describe how the data will be processed by the generated application after the lexical and syntactic analysis stage.
- Describe the expected output of the application after it has been processed.
- Leverage existing knowledge of EBNF grammars rather than require the learning of a completely new format.

A.2 TEBNF Structure
The structure of TEBNF is composed of a set of elements. There are five kinds of elements in TEBNF: input methods, output methods, grammar sections, actions, and state transition tables. Collectively, these elements and their contents are known as a TEBNF grammar. Each TEBNF grammar requires at least one or more of each kind of element.

### A.3 TEBNF Elements and Subelements

TEBNF elements (table A.1) contain one or more subelements. Subelements within TEBNF consist of production rules, typed terminals, non-typed terminals, literal values, operators, states, and static variables.

<table>
<thead>
<tr>
<th>Element</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>INPUT @name</td>
<td>specifier Input element of a specific input specifier.</td>
</tr>
<tr>
<td>OUTPUT @name</td>
<td>specifier Output of a specific output specifier.</td>
</tr>
<tr>
<td>GRAMMAR @name</td>
<td>Start of grammar section.</td>
</tr>
<tr>
<td>ACTIONS @name</td>
<td>Contains one or more actions.</td>
</tr>
<tr>
<td>STATES @name</td>
<td>Start of state transition table section.</td>
</tr>
<tr>
<td>END</td>
<td>End of element section.</td>
</tr>
</tbody>
</table>

Subelements are declared where they are first used. TEBNF infers what a subelement is by the way it is used. Each element requires a name be given to it. Element names are case-sensitive, can only contain visible characters, and are always prefixed by the '@' character as shown in example A.1:

\[
\text{GRAMMAR @packet} \quad (A.1)
\]

### A.4 TEBNF Scoping Rules

Elements and subelements are directly accessible at the scope they are created, similar to the C++ language. Elements can be declared within the scope of other elements. Subelements exist within the scope of their respective elements. Each type of element has specific types of subelements that can be declared only within the scope of that type of element.
A.5 TEBNF Types

Association of types (table A.2) with terminal symbols offers an extra level of precision when matching specific patterns found in input data. These symbols are called typed terminals. TEBNF can infer the type of a terminal symbol because each type has two important components.

Table A.2: TEBNF symbols, production rules, non-typed terminals, and typed terminals.

<table>
<thead>
<tr>
<th>Type</th>
<th>Description</th>
<th>Example</th>
</tr>
</thead>
<tbody>
<tr>
<td>symbol</td>
<td>Production rule (non-terminal)</td>
<td>alphabet</td>
</tr>
<tr>
<td>symbol</td>
<td>Non-typed terminal (1 or more literals)</td>
<td>’a’, ‘b’, ’c’, 0xAB, &quot;String literal&quot;</td>
</tr>
<tr>
<td>#comment</td>
<td>Single-line comment</td>
<td>#This is a comment.</td>
</tr>
<tr>
<td>## comment</td>
<td>Multi-line comment</td>
<td>## This is a really, really, really long multi-line comment. ##</td>
</tr>
<tr>
<td>$var</td>
<td>Static variable</td>
<td>$myValue = 42 ;</td>
</tr>
<tr>
<td>type</td>
<td>Typed terminal</td>
<td>CHAR{0,} ;</td>
</tr>
<tr>
<td>BYTE</td>
<td>Represents a 8-bit byte</td>
<td>My_Kb = BYTE{1024} ;</td>
</tr>
<tr>
<td>INT_X</td>
<td>Represents an integer of size X bits</td>
<td>My_Int = INT_64;</td>
</tr>
<tr>
<td>INT_STR_X</td>
<td>Represents an integer as a string of size X bits</td>
<td>fileLength = UNSIGNED_INT_STR_96;</td>
</tr>
<tr>
<td>CHAR</td>
<td>Represents a 8-bit character</td>
<td>MyChar = CHAR ;</td>
</tr>
<tr>
<td></td>
<td></td>
<td>MyString = CHAR{128} ;</td>
</tr>
<tr>
<td>FLOAT_X</td>
<td>Floating-point number of size X bits</td>
<td>MyFloat = FLOAT_64 ;</td>
</tr>
<tr>
<td>UNSIGNED</td>
<td>Unsigned number terminal</td>
<td>UNSIGNED INT_16{2} ;</td>
</tr>
</tbody>
</table>

First, each type has an inherent size in bits or bytes. Whenever data is matched to a specific type the size is immediately known. Because the size of each type is known beforehand, the offset of the next symbol is immediately known. Second, each type inherently identifies how it should be used in a given context. TEBNF types are expressed by assigning a type to a terminal production symbol, as shown in example A.2:
payload = INT_64 \quad (A.2)

TEBNF also has static variables, which are a kind of subelement that can assume the type of whatever is assigned to them. They are static because they have global visibility—i.e. they can be declared anywhere and accessed from any other element, regardless of where they were declared. Static variables are always prefixed by the '$' character (example A.3):

\[
$payloads = payload
\] \quad (A.3)

A static variable can become typed when a typed terminal is assigned to it. Production rules, terminals, and literals can also be assigned to static variables. This capability makes static variables the most flexible subelement available in TEBNF.

**A.6 TEBNF Operators**

There are three categories of operators in TEBNF. First are production rule operators (table A.3), which are used to build production rules. Second are arithmetic and comparison operators (table A.4). Arithmetic and comparison operators are a key difference between TEBNF and standard EBNF, which does not have them. Third is inter-element operators that perform operations on and/or between elements (table A.5). The only operator that falls in this category is the "AS" operator.

**A.7 TEBNF Grammar Elements**

Grammar elements contain production rules. Production rules are subelements of their containing grammar element. Terminal and non-terminal symbols have no prefix character, are made up only of alpha-numeric characters, and are case-sensitive. Examples of grammar elements are found in listings A.3 and A.4.

Production rule subelements can only be declared within TEBNF grammar elements. Production rule subelements can be referred to directly using the containing elements name along with the dot operator followed by the subelement (symbol) name.
Table A.3: TEBNF production rule operators.

<table>
<thead>
<tr>
<th>Operator</th>
<th>Description</th>
<th>Example</th>
</tr>
</thead>
<tbody>
<tr>
<td>=</td>
<td>Definition i.e. is defined as</td>
<td>alphaNumericCharacter = letter</td>
</tr>
<tr>
<td>=</td>
<td>Grammar total length</td>
<td>= fileLength ;</td>
</tr>
<tr>
<td>,</td>
<td>Concatenation</td>
<td>twoLetters = letter , letter ;</td>
</tr>
<tr>
<td>;</td>
<td>Termination</td>
<td>twoVals = val1 , val2 ;</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Or</td>
</tr>
<tr>
<td></td>
<td></td>
<td>State Transition</td>
</tr>
<tr>
<td>.</td>
<td>Element member access</td>
<td>@packet.payloadSize</td>
</tr>
<tr>
<td>{min,max}</td>
<td>Occurrence range</td>
<td>letter{0,}</td>
</tr>
<tr>
<td>len</td>
<td>Exact range, where len is the min and max.</td>
<td>letter{26}</td>
</tr>
<tr>
<td>[]</td>
<td>Array subscript</td>
<td>myChar[5]</td>
</tr>
</tbody>
</table>

Table A.4: TEBNF arithmetic and comparison operators.

<table>
<thead>
<tr>
<th>Operator</th>
<th>Description</th>
<th>Example</th>
</tr>
</thead>
<tbody>
<tr>
<td>==</td>
<td>Equality</td>
<td>$X == $Y</td>
</tr>
<tr>
<td>=</td>
<td>Assign</td>
<td>$x = 45 ;</td>
</tr>
<tr>
<td>+</td>
<td>Add</td>
<td>$x = y + z</td>
</tr>
<tr>
<td>-</td>
<td>Subtract</td>
<td>$x = g - h</td>
</tr>
<tr>
<td>+=</td>
<td>Addition assignment</td>
<td>$x = $g - $h</td>
</tr>
<tr>
<td>++</td>
<td>Post-increment</td>
<td></td>
</tr>
<tr>
<td>-=</td>
<td>Subtraction assignment</td>
<td>$x = $g - $h</td>
</tr>
<tr>
<td>–</td>
<td>Post-decrement</td>
<td></td>
</tr>
<tr>
<td>*</td>
<td>Multiply</td>
<td>$x = y * 92</td>
</tr>
<tr>
<td>/</td>
<td>Divide</td>
<td>$x = y / 2</td>
</tr>
</tbody>
</table>

@packet.payloadSize
Table A.5: TEBNF inter-element operator.

<table>
<thead>
<tr>
<th>Operator</th>
<th>Description</th>
<th>Example</th>
</tr>
</thead>
<tbody>
<tr>
<td>AS</td>
<td>Defines a new element to be the same as an existing element</td>
<td>OUTPUT @UDP_Out AS @UDP_In END</td>
</tr>
</tbody>
</table>

This format is similar to the way object-oriented languages like C++ and Java provide access to object members, though it is important to note that TEBNF itself is not object-oriented. The dot operator permits other grammar elements and state transition table elements to have access to a given production rule subelement.

A.8 TEBNF State Transition Table Elements

The function of any given application can be described as a finite state machine composed of a finite set of states [38]. The machine is in one state at a time, and movement from one state to another is triggered by specific inputs [38]. Because applications can be asynchronous, i.e. performing work on multiple threads, it is possible to have a finite state machine on each thread of execution. Concurrent behavior is becoming common in today's software [39].

Representation of a finite state machine in TEBNF is done using a state transition table that can access any TEBNF input, output, grammar symbol, or static variable. This state transition table ties the various elements and subelements of a TEBNF grammar into a coherent description of a single thread of execution. This means that TEBNF makes it possible to represent multiple threads of execution using multiple state transition tables. Each state transition table consists of six columns delimited by the pipe operator. Columns flow from left to right in the following order:

1. State

2. Input or condition
3. Input Method

4. Next State

5. Output or action

6. Output Method

The first column is the current state. Each state identifies where to go in the finite state machine when the right conditions are met. The name of each state must be unique within the scope of the state transition table it belongs to. The second column specifies a condition that must be met to move to the next state. The condition can be but is not limited to a logical statement such as checking the value of a static variable or checking if the input received via a specific input method (specified in the third column) matches a given grammar production. The fourth column is the state to transition to upon satisfaction of the input or condition. The fifth column identifies the output to send or action to execute while transitioning to this next state. If the fifth column is an output instead of an action, the sixth column is the output method that the output will be sent through.

A.9 TEBNF Actions Elements

Actions elements contain a list of actions to be executed in the order they are listed. Actions elements can only be used within a state transition table element row. Since they are not required in a TEBNF grammar, actions can be listed directly inside a state transition table. Actions elements are similar to macros in C++, and can accept zero or more comma-delimited parameters, as shown in the example taken from appendix listing B.1. Actions elements can also contain calls to C or C++ functions, making them one of the most powerful elements available in TEBNF.

Listing A.1: A TEBNF Actions element.

```
ACTIONS @right (val)
    @tape.elem[@tape.$i] = val;
    @tape.$i++;
```
A.10 TEBNF Input and Output Method Elements

Table A.6 shows all of the possible inputs and outputs available in TEBNF. Each input method describes a way for the generated application to receive input. No other settings information is required by an input method because the generated application will provide a way for the user of to give it the needed information through the user interface. Console elements allow prompt s to be defined within their scope, which tie a prompt string to a typed value to be input by a user. Listing A.2 shows a console input element with two prompt values. The first prompt value will display the prompt "Number: " and treat the input provided through the console as a signed 64-bit integer. The second prompt value will display the prompt "Op: " and treat input as a signed 8-bit integer.

Listing A.2: A TEBNF Console Input element.

```
INPUT @ConsIn = CONSOLE
    num = INT_64 = "Number: ";
    op = INT_8 = "Op: ";
END
```

Table A.6: TEBNF input/output specifiers.

<table>
<thead>
<tr>
<th>Input/Output Types</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>UDP_IP</td>
<td>Read/write input from/to from UDP.</td>
</tr>
<tr>
<td>FILE</td>
<td>Read/write input from/to a file.</td>
</tr>
<tr>
<td>CONSOLE</td>
<td>Read/write input from/to command line.</td>
</tr>
</tbody>
</table>

Table A.6 shows all of the possible outputs available in TEBNF. Output methods describe a way for the generation application to send or display output.

Networking inputs and outputs in TEBNF are based on UDP/IP. There are many other networking protocols, but many of them are transport and session layer protocols. Thus, describing other protocols can be done by using a state transition table to describe the protocol that will work over UDP/IP.
Custom input/output (I/O) is accomplished by using the state transition table to specify which grammar is used when receiving data as input or for sending data as output. In the case of a custom input, a GUI is generated that will ask for input to match the described grammar. In the case of output, data will be sent to the desired output following the format described in the provided grammar.

### A.11 TEBNF Example 1: Calculator

A TEBNF example is shown in listing A.3 describing a calculator that supports addition, subtraction, multiplication, and division of integers.

Listing A.3: TEBNF grammar describing a calculator.

```
INPUT @ConsIn = CONSOLE
    num = INT_64 = "Number: ";
    op = INT_8 = "Op: ";
END

OUTPUT @ConsOut = CONSOLE END

GRAMMAR @Number
    num = INT_64;
    $result = INT_64;
END

GRAMMAR @addOp op = '+'; END
GRAMMAR @subOp op = '-'; END
GRAMMAR @mulOp op = '*'; END
GRAMMAR @divOp op = '/'; END
GRAMMAR @eqOp op = '='; END

ACTIONS @Assign @Number.$result = @Number.num; END;
ACTIONS @AddAssign @Number.$result += @Number.num; END
```
ACTIONS @SubAssign @Number.$result -= @Number.num; END
ACTIONS @MulAssign @Number.$result *= @Number.num; END
ACTIONS @DivAssign @Number.$result /= @Number.num; END

STATES @Calculator

# State | Input or | Input | Next | Output or | Output |
# | Condition | Method | State | Action | Method |
#
Init | @Number | @ConsIn.num | StateNum | @Assign | |
StateNum | @Number | @ConsIn.num | StateOp | |
StateOp | @addOp | @ConsIn.op | Print | @AddAssign | |
| @subOp | @ConsIn.op | Print | @SubAssign | |
| @mulOp | @ConsIn.op | Print | @MulAssign | |
| @divOp | @ConsIn.op | Print | @DivAssign | |
| @eqOp | @ConsIn.op | Done | @Number.$result | @ConsOut; |
| | | | Done | |
Print | | | StateNum | @Number.$result | @ConsOut; |
Done | | | | |
END

A.12 TEBNF Example 2: NITF 2.1 File Client

A TEBNF example is shown in listing A.4 that describes a client application that transfers NITF 2.1 files over UDP/IP. This client application guarantees one-time delivery of each packet or none at all. The generated application receives packets matching the description shown in the examples grammar element. Upon reception of a packet, it will increment the payloads static variable, check if all of the data (entire file) has been received, and send an ACK message to tell the sender that a packet with a specific packet number has been received successfully. Once all of the packets have been received to reconstruct the file being sent (tracked by $payloads), the output is written to file and $payloads is cleared.
and ready to receive more file packets.

Listing A.4: TEBNF grammar describing a UDP NITF 2.1 file transfer client.

```
INPUT @UDP_In = UDP_IP END # UDP/IP input socket.
OUTPUT @UDP_Out AS @UDP_In END
OUTPUT @File_Out = FILE END
OUTPUT @Console_Out = CONSOLE END

GRAMMAR @Nitf
# Describe the file to receive.
syncWord = 'N', 'I', 'T', 'F', '0', '2', '.', '1', '0';
skip1 = BYTE{333}; # FL offset is 342.
fileLength = UNSIGNED INT STR 96; # NITF file length field = 12 bytes.
skip2 = BYTE{,};
header = syncWord, skip1, fileLength;
file = header, skip2;
  = fileLength; # Overall size of this file.
END
GRAMMAR @Send startSend = "send"; END
GRAMMAR @Status recvMsg = "All files received from server, exiting."; END
GRAMMAR @Done done = "done"; END

STATES @File_Transfer
#
# State | Input or | Input | Next | Output or | Output | Method | Method
# | Condition | Method | State | Action | |
# Init | | | Start | @Send.startSend | @UDP_Out |
Start | @Nitf | @UDP_In | Init | @Nitf.file | @File_Out |
| | @Done | @UDP_In | Quit | @Status.recvMsg | @Console_Out |
Quit | | | | | |
END
```
Appendix B

TEBNF Turing Completeness Proof

B.1 Turing Completeness

Turing machines provide the most powerful computational model known to exist [40]. The Turing completeness of a programming language is important because anything computable can be computed using that language [40].

A Turing machine that can perform any operation of any other ordinary Turing machine is known as a universal Turing machine [41]. Therefore, a programming language that can simulate a universal Turing machine is Turing complete.

B.2 Proof

Multiple examples of universal Turing machines have been presented [42–44]. A universal Turing machine that simulates a 2-tag system can be implemented with relatively few states and symbols. Tag systems simulate the game of tag, where the goal is to see if it will ever terminate by reaching the end of the sequence of symbols.

Rogozhin proved the universality of several classes of tag systems including a 4-state 6-symbol universal Turing machine called UTM(4,6) [42]. The tag system simulated by UTM(4,6) consists of 22 commands and is the lowest known number of commands for a universal Turing machine [42]. The machine is comprised of:

- A set of states: $q_1, q_2, q_3, q_4$
- Input symbols: 0 (blank), b, x, y, c (mark)
- Tape symbols
- An initial state: $q_1$
• A transition function (executed in order):

1. Print (write) a symbol.

2. Move head left \( L \), right \( R \), none \(-\).

3. Go to the next state.

UTM(4,6) \([42]\) is described as a list of 5-tuples (table B.1). These 5-tuples are formatted in order of evaluation using the Turing/Davis convention \((q_i, S_j, S_k, \text{left } L, \text{right } R, \text{none } - , q_m)\) \([45]\):

1. Current state \( q_i \).

2. Scanned symbol \( S_j \).

3. Print symbol \( S_k \).

4. Move tape head left \( L \), right \( R \), none \(-\).

5. Next state \( q_m \).

Since Rogozhin proved the universality of UTM(4,6) \([42]\), an implementation of this machine in TEBNF is provided in listing B.1 to demonstrate the capabilities and Turing Completeness of TEBNF.

Table B.1: List of 5-tuples describing UTM(4,6).

\[
\begin{array}{cccc}
q_{11}\times Lq_1 & q_{210}Rq_3 & q_{311}Rq_3 & q_{410}Rq_4 \\
q_{1by}Rq_1 & q_{2by}Lq_3 & q_{3bx}Rq_4 & q_{4bc}Lq_2 \\
q_{1yb}Lq_1 & q_{2yx}Rq_2 & q_{3yb}Rq_3 & q_{4yx}Rq_4 \\
q_{1xb}Rq_1 & q_{2xy}Lq_2 & q_{3x}" & q_{4x}" \\
q_{10x}Lq_1 & q_{201}Lq_2 & q_{30c}Rq_1 & q_{40c}Lq_2 \\
q_{1c0}Rq_4 & q_{2cb}Rq_2 & q_{3c1}Rq_1 & q_{4cb}Rq_4 \\
\end{array}
\]

B.3 Stepping Through the Machine

The tag system simulated by UTM(4,6) \([42]\) has three stages. The 5-tuples each stage refers to are shown in table B.1. The corresponding TEBNF implementation is given in
listing B.1. The TEBNF implementation starts on the first line of the transition table at
the begin state. The begin state reads the contents of a file into the array \texttt{@tape.elements}
that functions as the tape.

Stage 1. The first stage is complete when the head of the machine moves right and
meets the mark. The mark is deleted and the first stage ends at \texttt{$q1c0Rq4$}. The end of this
stage corresponds to the seventh line in the TEBNF state table.

Stage 2. The machine executes a series of jumps to arrive at \texttt{$q40cLq2$}. If the head
reaches pair \texttt{xb}, the machine jumps to \texttt{$q2byLq3$} and halts at \texttt{$q3x-$}. Otherwise, the second
stage ends upon reaching pair \texttt{1b}.

Stage 3. The machine jumps to \texttt{$q3ybRq3$}, then \texttt{$q311Rq3$}. Upon moving to the right,
the machine head reaches \texttt{c} (the mark), deletes it, and jumps to \texttt{$q3c1Rq1$} to begin a new
cycle.

Upon reaching one of the halt states, the TEBNF implementation of the machine writes
the contents of the tape to a text file.

Listing B.1: Rogozhin’s UTM(4,6) implemented in TEBNF.

\begin{verbatim}
# TEBNF implementation of UTM(4,6) (a 4-state 6-symbol
# universal Turing machine) presented by Y. Rogozhin in
# "Small universal Turing machines", 1996.

INPUT @TpIn = FILE END; # For reading tape from file.
OUTPUT @TpOut AS @Tape.In END; # For writing to tape file.

GRAMMAR @tape
   elem = BYTE{,} ; # Array with no min or max number of elements.
   $i = 0 ;       # Index for moving left or right on tape.
END

ACTIONS @right (val)
   @tape.elem[@tape.$i] = val;
   @tape.$i++;;
\end{verbatim}
ACTIONS \texttt{\@left (val)}
\begin{verbatim}
\texttt{@tape.e\!l\!e\!m[@tape.$i] = val;}
\texttt{@tape.$i--;}
\end{verbatim}

# Read the tape and run the universal Turing machine. Moving right
# and left on the tape (represented by the \texttt{@tape.e\!l\!e\!m} array) is
# represented by incrementing and decrementing \$index, respectively.

# Symbols: 0 (blank), 1, b, x, y, c
# States: q1, q2, q3, q4

STATES @UTM_4,6

\begin{verbatim}
begin | @tape | @TpIn | q1 | | | |
| q1 | @tape.e\!l\!e\!m[@tape.$i]== '1'| | q1 | @left ('1') | | ;
| | @tape.e\!l\!e\!m[@tape.$i]== 'b'| | q1 | @right ('0')| | ;
| | @tape.e\!l\!e\!m[@tape.$i]== 'y'| | q1 | @left ('b') | | ;
| | @tape.e\!l\!e\!m[@tape.$i]== 'x'| | q1 | @right ('0')| | ;
| | @tape.e\!l\!e\!m[@tape.$i]== '0'| | q1 | @left ('x') | | ;
| | @tape.e\!l\!e\!m[@tape.$i]== 'c'| | q4 | @left ('0') | | ;
q2 | @tape.e\!l\!e\!m[@tape.$i]== '1'| | q2 | @right ('0')| | ;
| | @tape.e\!l\!e\!m[@tape.$i]== 'b'| | q3 | @left ('y') | | ;
| | @tape.e\!l\!e\!m[@tape.$i]== 'y'| | q2 | @left ('y') | | ;
| | @tape.e\!l\!e\!m[@tape.$i]== 'x'| | q2 | @left ('x') | | ;
| | @tape.e\!l\!e\!m[@tape.$i]== '0'| | q2 | @left ('1') | | ;
| | @tape.e\!l\!e\!m[@tape.$i]== 'c'| | q2 | @right ('y') | | ;
\end{verbatim}
q3 | @tape.elem[@tape.$i]== '1' | q3 | @right('1') | ;
| @tape.elem[@tape.$i]== 'b' | q4 | @right('x') | ;
| @tape.elem[@tape.$i]== 'y' | q3 | @right('b') | ;
| @tape.elem[@tape.$i]== 'x' | q4 | @tape | @TpOut;
| @tape.elem[@tape.$i]== '0' | q1 | @right('c') | ;
| @tape.elem[@tape.$i]== 'c' | q1 | @right('1') | ;
q4 | @tape.elem[@tape.$i]== '1' | q4 | @right('0') | ;
| @tape.elem[@tape.$i]== 'b' | q2 | @left('c') | ;
| @tape.elem[@tape.$i]== 'y' | q4 | @right('x') | ;
| @tape.elem[@tape.$i]== 'x' | q2 | @tape | @TpOut;
| @tape.elem[@tape.$i]== '0' | q2 | @left('c') | ;
| @tape.elem[@tape.$i]== 'c' | q4 | @right('b') | ;

END