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Characterization of Two-Phase Flows in Plunge Pools

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Characterization of Two-Phase Flows in Plunge Pools

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Abstract: The increasing magnitude of design floods has prompted re-evaluations of spillway capacity for large dams throughout the world. Current capacity of many spillways is inadequate. The overtopping creates new loading scenarios for the dam and raises questions about erosion and scour downstream from the dam. In this study, mean velocity was measured in different sections of the falling jet with optical fiber and with LS-PIV (Large Scale – Particle Image Velocimetry). Detailed studies of the submerged hydraulic jump downstream overflow nappe impinging jets are scarce. This work addresses such a situation, and compares numerical results against our own experiments. To advance the understanding of the phenomenon, instantaneous velocity was measured in the plunge pool with Acoustic Doppler Velocimeter (ADV) equipment, and mean velocities and air entrainment rate were obtained with optical fiber instrumentation. At the same time, transient numerical simulations were carried out with computational fluid dynamics (CFD) programs. Due to the variation of the air concentration in the plunge pool, optical fiber obtained valid velocities near to the impingement point, while ADV was used once the air concentration was small, allowing for the measurement of the velocity in the whole submerged hydraulic jump. In general, the CFD simulations provided results fairly close to the laboratory values measured, in spite of having used a simple two-phase flow model.

Keywords: air-water flow, energy dissipation, falling jets, numerical simulations, overtopping, plunge pool.

1. Introduction

In recent years, the increase in the magnitude of design floods has promoted the revaluation of the spillways capacity and the operational scenarios for large dams around the World. Several studies have shown that the current capacity of many spillways is inadequate, and dams may overflow during extreme events. Increasing the capacity of spillways is costly and sometimes technically impracticable. In these cases, the dams’ owners could consider the overflow as an additional strategy of operation during extreme events. This situation creates new loading scenarios, raising questions about the hydrodynamic actions and scour downstream of the dams (Wahl et al., 2008; FEMA, 2014).

The choice of the type of plunge pool is usually a technical-economic decision between a deep and uncoated stilling basin and a shallow stilling basin with lining. It is necessary to know the magnitude and frequency of the dynamic pressure in the bottom of the plunge pool. The required water cushion depth depends on the characteristics of the impingement jet so that most of the energy is dissipated, avoiding scour downstream of the dam (Annandale, 2006). The energy dissipation mechanisms in the free-flow jets can be divided into the following (Fig. 1a): (a) aeration and disintegration of the jet during its fall, (b) entrainment of air and diffusion of the jet in the water cushion, (c) impact on the basin bottom, and (d) recirculation in the basin (Castillo et al., 2015).

In this work, the free falling jet velocity was measured with Large Scale-Particle Image Velocimetry (LS-PIV) technique and with optical fiber equipment. Results were compared with three-dimensional numerical simulations.

In recent years several researchers have analyzed the near-flow field below the impingement point of free falling jets. Table 1 summarizes the main characteristics of experimental and numerical settings. However, the current understanding on this highly-aerated, highly-turbulent flow is still scarce, and there is lack of experimental study providing detailed benchmark data (Wang et al., 2018).

Although there are progresses of two-phase flows in hydraulic jumps, detailed theoretical and numerical models of the internal flow features have yet to be developed for a wide range of Froude numbers (Bombardelli, 2012).

The submerged hydraulic jump downstream of the impingement point is a particular case with scarce studies. This work needs to be addressed in order to improve this research field. The submerged hydraulic jump generated in the plunge pool has been analyzed with several procedures. The aeration has been measured with optical fiber equipment, obtaining air concentrations, mean velocities, bubble frequencies, and bubbles’ mean diameters. Besides this, the mean velocity and turbulent kinetic energy have been measured in the less aerated region of the water
cushion with Acoustic Doppler Velocimeter (ADV). Laboratory data are compared with the numerical simulations carried out using ANSYS CFX (v. 18).

Table 1. Flow conditions and instrumentation in recent studies of the near-flow field below the impingement point of free falling jets.

<table>
<thead>
<tr>
<th>Authors</th>
<th>Nozzle diameter (m)</th>
<th>Free falling distance (m)</th>
<th>Impingement velocity (m/s)</th>
<th>Instrumentation</th>
</tr>
</thead>
<tbody>
<tr>
<td>Chanson et al. (2004)</td>
<td>0.025</td>
<td>0.1</td>
<td>3.5-4.4</td>
<td>Prandtl-Pitot tube; hot-film probe; single-tip phase-detection probe</td>
</tr>
<tr>
<td></td>
<td>0.0125</td>
<td>0.05</td>
<td>2.42-3.46</td>
<td></td>
</tr>
<tr>
<td></td>
<td>0.0273</td>
<td>0.0273</td>
<td>1.79-2.49</td>
<td></td>
</tr>
<tr>
<td>Ma et al. (2010)</td>
<td>0.025</td>
<td>0.10</td>
<td>3.5-4.4</td>
<td>Computational multiphase fluid dynamics (CMFD) code</td>
</tr>
<tr>
<td>Qu et al. (2013)</td>
<td>0.06</td>
<td>0.10</td>
<td>2.0-2.5</td>
<td>Particle Image Velocimetry (PIV)</td>
</tr>
<tr>
<td>Bertola et al. (2017)</td>
<td>0.012</td>
<td>0.10</td>
<td>2.49-7.43</td>
<td>Dual-tip phase-detection probe; total pressure sensor; Prandtl-Pitot tube; acoustic displacement meter</td>
</tr>
<tr>
<td>Boualouache et al. (2017)</td>
<td>0.005</td>
<td>0.01</td>
<td>2.54</td>
<td>ANSYS CFX and Fluent codes</td>
</tr>
<tr>
<td>Wang et al. (2018)</td>
<td>0.012</td>
<td>0.05-0.15</td>
<td>2.4-5.5</td>
<td>Dual-tip phase-detection probe; total pressure sensor</td>
</tr>
</tbody>
</table>

2. Material and Methods

2.1. Experimental Device

The Hydraulic Laboratory of the Universidad Politécnica de Cartagena has an experimental device designed for the study of turbulent jets and energy dissipation in overtopping weirs.

The mobile device of the weir has been modified from that used by Carrillo (2014) to improve the energy dissipation in the inlet channel before the weir, to increase the range of flows tested and the discharge heights. The infrastructure is designed to analyze flows between 10 l/s and 200 l/s, discharge heights between 2.20 m and 3.50 m, and different water cushions (Fig. 1b).

![Figure 1](image-url)
The fixed stilling basin is 1.05 m wide, 3.00 m long, and 1.60 m high. It is built in methacrylate to observe the flow inside. It allows different depths of water cushions, from direct impact to depths of 1.00 m.

Pressure measurements are currently being measured with piezoresistive sensors located in the bottom of the plunge pool, together with the study of velocities in different sections of the water cushion using Doppler equipment and aeration rates using optical fiber methodology.

### 2.2. Optical Fiber

To measure the air concentration in the free-falling jet and in the dissipation basin, an optical fiber equipment with double-tip probe of RBI-Instruments was used. This equipment allows the detection of the phase change between air and water. The rise and fall of the signal detected by the probe are, respectively, the arrival and departure of the gas phase at the sensor tip. The threshold values were set at 1.0 V and 2.5 V (Boes and Hager, 1998). The void fraction is defined as the ratio between the total time the probe is in gas ($\Sigma t_G$) and the time duration $t$ of the experiment.

According to Stutz and Reboud (1997a, 1997b), this equipment allows for the measurement of water-air flows with velocities up to 20 m/s. The relative uncertainty of the void fraction is estimated at approximately 15% of the measured value. A source of error in estimating the presence of air in the flow is due to the statistical count of the number of air bubbles in contact with the tips of the probe (Stutz, 1996). Therefore, a short duration of the measurement would contribute to a smaller accuracy of the results.

To evaluate the minimum duration of the measurements, André et al. (2005) analyzed the time required to stabilize the mean value during the measurement and found that the quasi-stationary values were statistically representative of the air concentration. Based on the sensitivity study of the probe behavior, the authors recommend a 60 s sampling sequence as a good compromise between precision and duration of the experiments.

Boes and Hager (2003) carried out experiments with 4000 air bubbles and samplings of 30 s. The authors considered that the accuracy of the air concentration and velocity measurements is related to the variation of the $N_b$ phase, air-water variation or the inverse, rather than the sample duration $t$.

A sample sequence of 90 s was considered in this study. Fig. 2 shows the evolution of the void fraction until it reaches a relative uncertainty of about 1%, as well as the sum of bubbles detected during the test.

Following these ideas, the two-phase flow characteristics were measured downstream of the stagnation point in different cross-sections spaced 0.10 m.

![Figure 2. Evolution of the void fraction and the number of bubbles detected by the optical fiber equipment during the test.](image)

### 2.3. Acoustic Doppler Velocimeter

In this study, the characteristics of the Acoustic Doppler Velocimeter equipment (ADV) were selected considering that the main objective was to characterize the turbulence. We used Nortek A.S. Vectrino Plus equipment. The velocity range was selected as ± 4.00 m/s (the maximum available in the equipment). With this adjustment, the ADV can measure horizontal velocities up to 5.25 m/s and vertical velocity up to 1.50 m/s (maximum jet velocity before impact ≈ 6.75 m/s). Due to the fact that Doppler equipment needs to be fully immersed in water, the first 5-6 cm of the water column could not be measured with this instrumentation.
Turbulent kinetic energy was measured 0.50 m upstream of the weir in inlet of the experimental facility to obtain the boundary conditions in the numerical simulations. This distance ensures that the streamlines are horizontal upstream of the weir in the range of the flows tested (0.50 m > 5h).

In the dissipation basin, velocities were recorded in different cross-sections spaced 0.10 m downstream of the stagnation point. In order to characterize the macro-turbulence of the flow, 5000 data were recorded at each measured point using a frequency of 10 Hz (more than 8 minutes of observation).

As the flows are highly turbulent and aerated, the values obtained with ADV may be affected by spurious or "spike" signals. Each time series should be filtered with velocity and acceleration thresholds (Wahl, 2000, 2003).

In addition to this, air may also affect the ADV signal. Frizell (2000) analyzed the influence of air concentrations ranging from 0% to 3.61%. As air concentrations and bubble sizes increase, the correlation values decrease drastically as the acoustic signals are absorbed and reflected by the two-phase flow. Matos et al. (2002) also found that air bubbles affect the accuracy of velocity measurements obtained with ADV. However, their experiment results suggest that ADV can provide reasonable estimations of velocity for low air concentrations (up to 8%).

As the flow in the plunge pool is highly turbulent and aerated, the Phase-Space Thresholding filter (Goring and Nikora, 2002, modified by Castillo, 2009) was used. The spikes were replaced on each record by the mean value of the twelve closest points. Details of the filtering method used may be obtained in Castillo et al. (2017).

2.4. Large Scale-Particle Image Velocimetry

Large-Scale Particle Image Velocimetry (LS-PIV) is an extension of particle image velocimetry (PIV), which provides velocity fields spanning large flow areas in laboratory or field conditions. Additional data, such as mappings of large-scale flow structures and discharges, are readily obtainable using LS-PIV. While the images and data-processing algorithms are similar to the conventional PIV technique, adjustments are required for illumination, seeding procedures, and pre-processing of the recorded images (Fujita et al., 1998). This technique has been used to estimate the velocity of free falling jets (Bercovitz et al., 2016).

In present work, the flow was recorded with a high-speed camera FASTCAM SA3 Model 120K (Photron Limited), a zoom lens with 50 mm focal length by Nikkor, lens aperture f/5.6, 1024x1024 pixels resolution, 8 bits→255 shades, and a horizontal distance from the camera to the jet recorded of around 3.50 m. Hence, the recording window dimensions were around 0.9 m x 0.9 m. Illumination of experiment was reached with 8 regular 800 w light bulbs with reflecting mounts in front of the flow. The speed camera used was 500 Hz: 0.00105 (m/pixel). Frames were analyzed in consecutive pairs by cross-correlation algorithm in an interrogation area of 64 x 64 pixels with sub-windows of 32 x 32 pixels in a single pass search and overlapping of 50% (Adrian and Westerweel, 2010). No background slide subtraction or noise remove techniques were applied. The PIVlab 1.41 software was used for the cross-correlation. This program is an open-source time-resolved particle image velocimetry tool in MATLAB® (Thielicke and Stamhuis, 2014). In each test, 1360 images were recorded and each test was repeated four times. The velocity values were averaged at each sub-window. Fig. 3 shows the velocity field obtained with a pair of images. Distances in the recorded window were calibrated considering a vertical plane located at the toe of the jet, at 3.30 m of horizontal distance to the camera. These distances were projected over the upper nappe profile to achieve the real displacements of the flow, with ratios from 1/1.15 in the upper zone, to 1/1.00 in the lower part of the recorded window. To do this, it was assumed that the shape of the upper nappe profile agrees with that proposed by Scimemi (1930) at each sub-window. The agreement between the lab measurements and the Scimemi (1930) formula was verified by Carrillo (2014). Fig. 3c shows the sub-window length obtained from the projection of each segment in the vertical plane used to calibrate the distance.

2.5. Numerical Simulations

Computational Fluid Dynamics (CFD) allows to solve problems in fluid mechanics, providing great results with great flexibility and speed. However, for its correct application it is necessary to compare and calibrate with results obtained in physical models and/or prototypes.

This work compares the results simulated with ANSYS CFX (v.18.0) and the data obtained in the laboratory. The fluid domain of the study area is divided into control volumes. In each one, the flow parameters (velocity, pressures, etc.) are calculated in discrete times, considering the equilibrium of the Navier-Stokes equations.
To solve the closure problem, the Shear-Stress-Transport (SST) turbulence model was selected. This model has been designed to obtain greater accuracy in flow separation under adverse pressure gradients (Menter, 1994). The SST model takes into account the precision of the $k-\omega$ model in the region close to the walls and changes to the $k-\varepsilon$ model in the outer part of the boundary layer. The best behavior of this turbulence model has been demonstrated in numerous validation studies in this type of flows (Carrillo, 2014; Castillo et al., 2014, 2017).

For the resolution of the air-water two-phase flow, the homogeneous model was chosen (ANSYS Inc., 2016). This model can be considered as a limiting case of the inhomogeneous model, where the transfer rate at the interface of both fluids is very large. In this way, it solves the interface considering that in these zones both fluids share the same field of velocities.

A mesh based on hexahedral elements of 0.01 m was used to solve the three-dimensional domain.

The boundary conditions were the water level in the inlet and outlet sections and hydrostatic pressures distributions. In the inlet condition, the turbulence measured in the laboratory with ADV was considered.

A transient calculation of 60 s was considered with a time-step interval of 0.05 s. After 20 s, it is considered that the steady state has been reached, obtaining the average of the different parameters.

The numerical model was previously validated considering the evaluation of the mesh size and the choice of the turbulence model. After the validation process, differences in the mean pressure at the stagnation point and the pressure distribution around it show a maximum error from -4 to 7%. This level of agreement is understandable given the observed air concentrations with the homogeneous-type models (Jha and Bombardelli, 2010; Bombardelli, 2012). Details of the validation and the boundary conditions may be obtained in Carrillo (2014), and Castillo et al., (2014, 2017).

3. Results and Discussion

3.1. Jet velocity

Following a streamline that starts on the weir, Fig. 4a shows the free falling jet velocity when different mesh sizes were considered. The results are compared with optical fiber and LS-PIV measurements. The mesh size has a small influence in the falling jet velocity. Velocity obtained with the different methods tended to be slightly smaller than the free-falling velocity due only to the gravity effects. This indicates the effect of air-water friction. The LS-PIV measurements were less accurate due to the difficulties to illuminate the falling jet. LS-PIV results are in agreement with the measurements carried out by Bercovitz el al. (2016).
3.2. Void Fraction in the Plunge Pool

Fig. 4b shows the void fraction \( \alpha = \Sigma t G_i / t \) obtained by the optical fiber equipment in different cross-sections downstream of the stagnation point \( (X = \text{horizontal distance to the stagnation point}) \). The largest values of void fraction were obtained close to the impact point of the rectangular jet, reaching values around 15%. As the flow moves away from the impact zone of the jet, the void fraction detected by the probe tends to reduce its value. The profiles located more than \( X = 0.40 \) m from the impact point show a void fraction smaller than 8%, reaching values around 3% in the profile located at \( X = 1.00 \) m.

The velocity profiles in the forward flow of hydraulic jumps may be compared if they are normalized with a velocity scale equal to the maximum velocity, \( V_{\text{max}} \), at any section, and with a length scale \( \delta \) equal to the elevation \( y \) from the bottom where the local velocity \( V = V_{\text{max}} / 2 \), and the velocity gradient is negative (Rajaratnam, 1965; Wu and Rajaratnam, 1996).

The maximum velocity \( V_{\text{max}} \) and the length scale \( \delta \) were obtained in each cross-section of the submerged hydraulic jump. Fig. 5 shows the non-dimensional velocity profiles in different cross sections located downstream of the stagnation point. Laboratory measurements were obtained with Doppler and optical fiber equipment. Laboratory equipments were used considering their limitations. The Doppler measurements were obtained for \( X > 0.40 \) m. Upstream this section, the air concentration was higher than 8% and the Doppler equipment did not allow to obtain valid results (see Matos et al., 2002). On the other hand, beyond section \( X = 0.40 \) m and above \( y/\delta > 1.5-2.0 \), the flow was non-unidirectional and the optical fiber obtained erratic values.

In the same cross sections, the results of the CFD simulations were obtained. In general, the results of the numerical simulations show the same behavior as the values obtained in the laboratory.

Fig. 5 also shows the turbulent kinetic energy (TKE) obtained in different sections of the plunge pool with the ADV equipment. The turbulent kinetic energy tends to dissipate quickly as the as the flow moves away from the impact zone, reaching maximum values around 0.30 m\(^2\)/s\(^2\) in the profile located 0.80 m from the stagnation point. The results obtained with the turbulence model follow the evolution of energy dissipation (Castillo et al., 2017).

3.3. Bubbles Frequency and Size in the Plunge Pool

The frequency of the bubbles detected by the probe has been analyzed by different authors in hydraulic jumps (Murzyn et al., 2005; Murzyn and Chanson, 2007).

Fig. 6 shows the frequency of bubbles detected by the probe. In most of the profiles, the highest values are obtained in the vicinity of the bottom. In the profile located 0.10 m downstream of the stagnation point, a maximum of 8700 bubbles were detected with a frequency of 96 Hz. The maximum values tend to reduce as the flow moves from the impact zone of the jet. In the profile \( X = 1.00 \) m, the values tend to be constant in all the depth, with a detection frequency of bubbles around 30 Hz.
These values are similar to the results measured by Murzyn et al. (2005), who obtained maximum frequencies around 85 Hz in hydraulic jumps with a Froude number of 4.82, and by Murzyn and Chanson (2007), who recorded maximum frequencies around 120 Hz for hydraulic jumps with Froude number of 8.30.

Assuming the hypothesis that bubbles are spherical, equally distributed in the time and that their movement is unidirectional, the size of the bubbles detected by the optical fiber equipment may be characterized by the mean diameter of Sauter, \( d_s \) (Clift et al. 1978, RBI-Instrumentation 2012). This is the diameter of the bubbles whose volume/surface ratio is the same that the calculated for all the bubbles detected during the test. The mean diameter of Sauter may be calculated as:

\[
d_s = \frac{3\alpha u^2}{2F}
\]

where \( \alpha \) is the void fraction, \( u \) the mean velocity of the bubbles, and \( F \) the bubble detection frequency.

Considering the velocity profiles in the previous section, Fig. 6 also shows the size of the bubbles detected in different sections of the plunge pool. Beyond section \( X = 0.40 \) m the flow is non-unidirectional and Eq. (1) may not be used. Mostly values are below 6 mm, with maximum values around 10 mm. These diameters are slightly lower than the results obtained by Murzyn et al. (2005) and by Murzyn (2010) in hydraulic jumps.
4. Conclusions

To observe and to predict two-phase flows in hydraulic structures is very complicated because of the undiluted nature of the flow. Under these conditions, the experimental data, and the results of the simulations are difficult to compare in a clear way.

In this work we have analyzed the characteristics of the air-water flow produced downstream of a free spillway. Using uniform illumination, the LS-PIV methodology may be used to estimate the velocity of the free falling jet.

Optical fiber and ADV equipment were used considering their limitations. In this way, the velocity profiles of the complete hydraulic jump could be measured. The optical fiber measurements complement the flow velocity obtained in previous studies (Castillo et al., 2017).

There are scarce data of air entrainment in submerged hydraulic jumps downstream of free falling jets. In general, the characteristics of the air-water flow (void fraction, bubble frequency, and size) are similar to those observed by different researchers in hydraulic jumps.

The CFD simulations provided results close to the values measured in the laboratory, despite having used a simple two-phase flow model. The “homogeneous” model seems to be able to predict the phenomenon.

In order to advance in the knowledge, we plan to study the behavior of two-phase flows in the plunge pool with different experimental techniques. In addition, the laboratory results will be compared with several CFD codes (open source and commercial codes).

5. Acknowledgments

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6. References


