

TPU from Atmospheric Correction of Landsat 8 OLI Imagery

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Work performed under USGS Contract [G15PCXXXX]

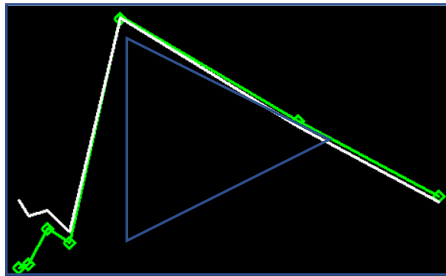


Total Propagated Uncertainty due to Atmospheric Correction of Landsat 8 OLI Imagery

TPU

$$J \cdot \Sigma \cdot J^T$$

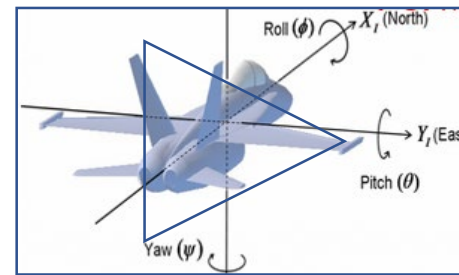
Atmospheric
Correction



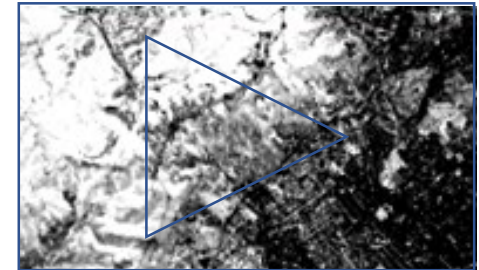
TPU gov. Eq.
ATCOR

$$(\sigma_{\rho_i})^2 = \left(\frac{\partial \rho_i}{\partial \tau_a} \sigma_{\tau_a} \right)^2$$

Lidar TPU
(position data)



TPU example
(NDVI)



TPU, Uncertainty Chain



Sat. Imagery (OLI)

SAR, Lidar data

x σ_x

y σ_y

z σ_z

ρ_{B1}

ρ_{B2}

ρ_R

ρ_G

ρ_{NIR}

ρ_{SW1}

ρ_{SW2}

$\sigma_{\rho_{B1}}$

$\sigma_{\rho_{B2}}$

σ_{ρ_G}

σ_{ρ_R}

$\sigma_{\rho_{NIR}}$

$\sigma_{\rho_{SW1}}$

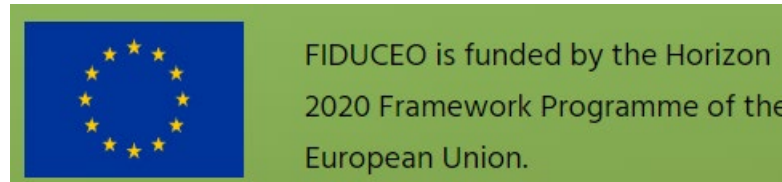
$\sigma_{\rho_{SW2}}$

Each and every pixel ?

Each and every point ?

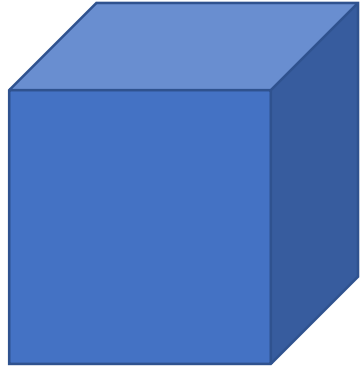
NAVY & NOAA (sonar & lidar)

FIDUCEO (satellite imagery)

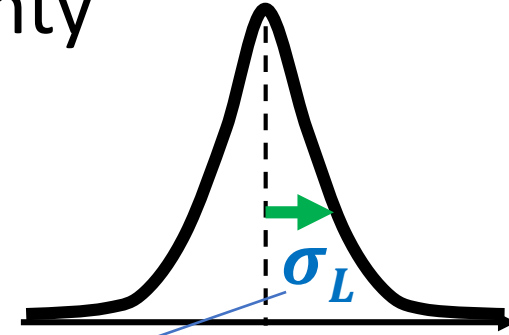


Fidelity and uncertainty in climate data records from Earth Observations

Total Propagation of uncertainty



$$V = L^3 \longrightarrow \Delta V = \frac{dV}{dL} \Delta L$$



Repeated length measurement

$$\sigma_V = 3L^2 \cdot \sigma_L$$

volume uncertainty ←

Propagates through
(vol) Equation

← Length uncertainty

Total uncertainty
due to ATCOR

← Propagates through
ATCOR Equation

← Multiple uncertainty sources
from Atmosphere
(aerosol, O₃, H₂O, P, SZA, VZA,...)

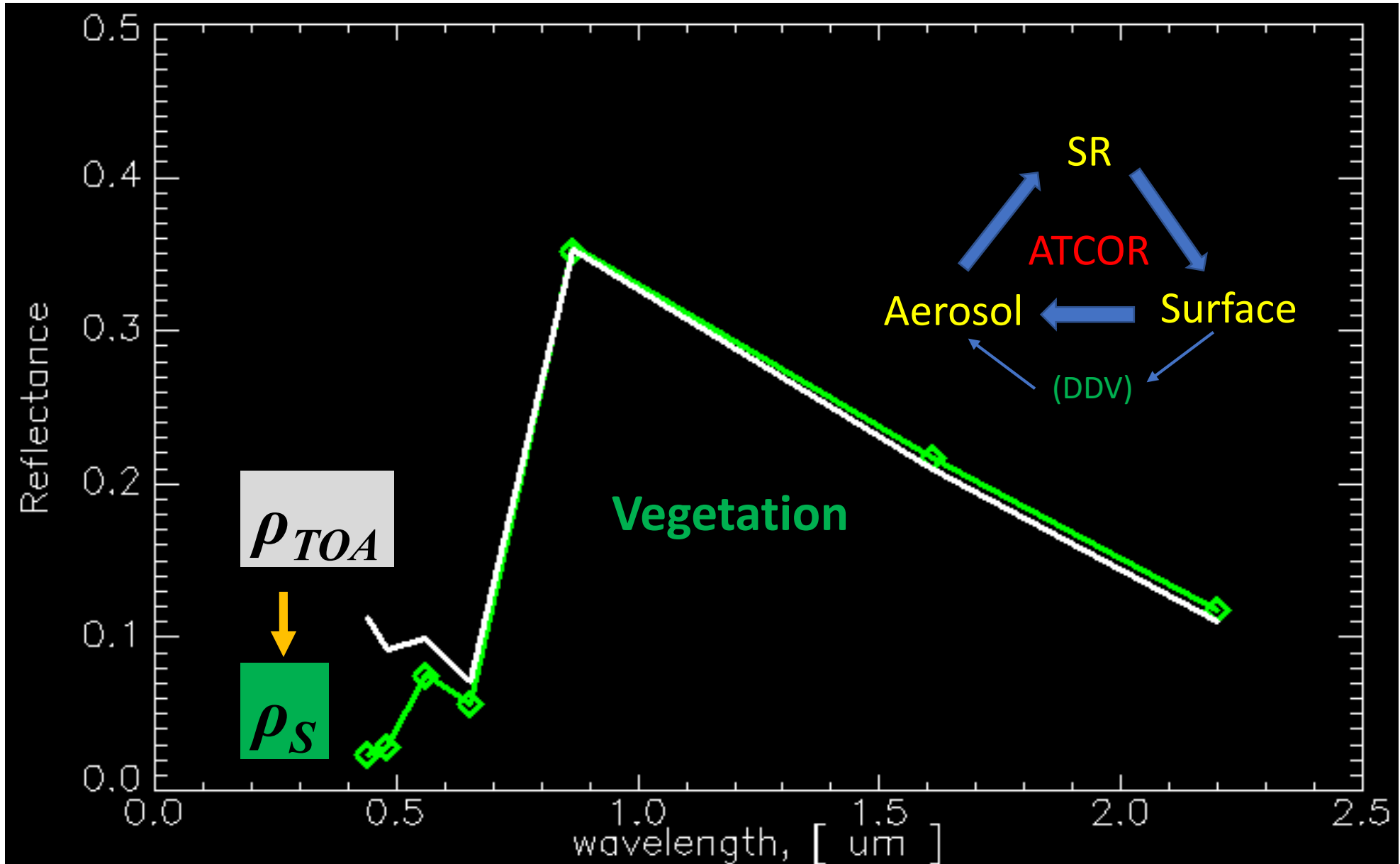
L8 OLI

$$\begin{matrix} \sigma_{\rho_{B1}} \\ \sigma_{\rho_{B2}} \\ \sigma_{\rho_G} \\ \sigma_{\rho_R} \end{matrix} = TPU = J \cdot \Sigma \cdot J^T$$

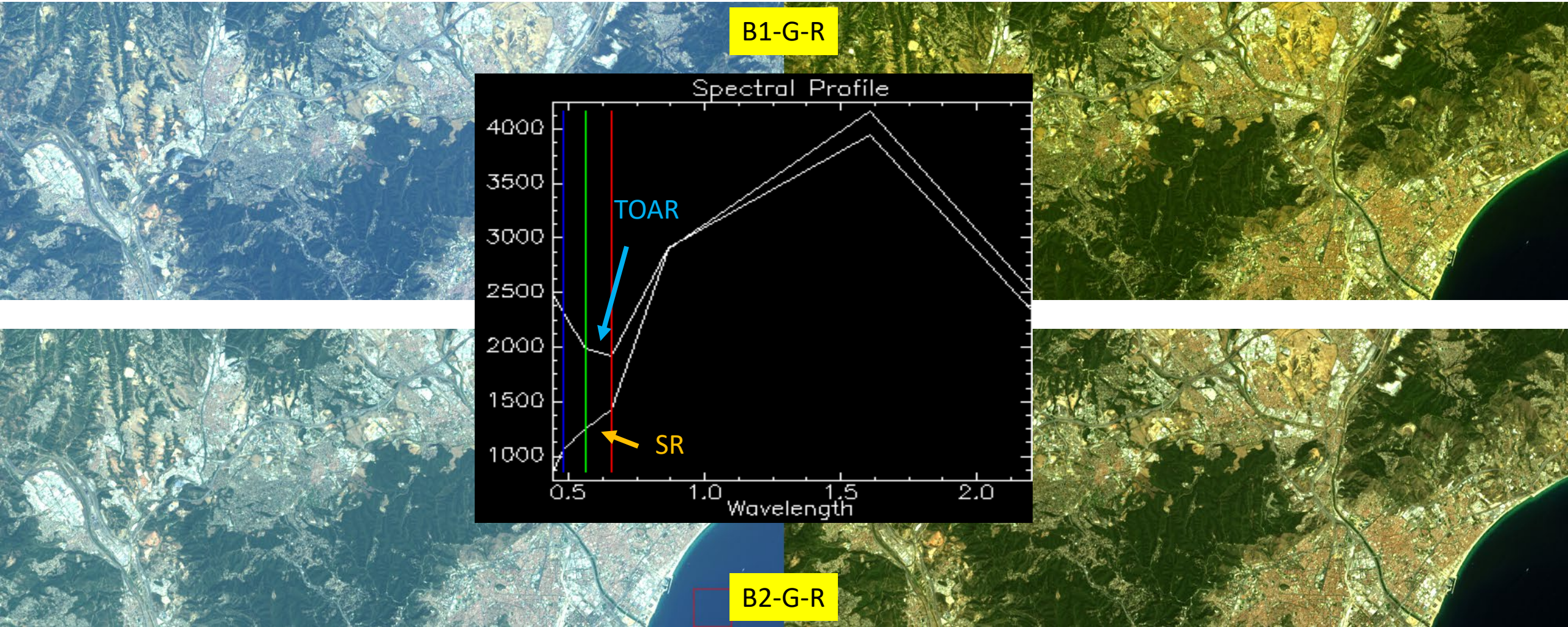
- (1) Define ATCOR equation
- (2) Derive Jacobian

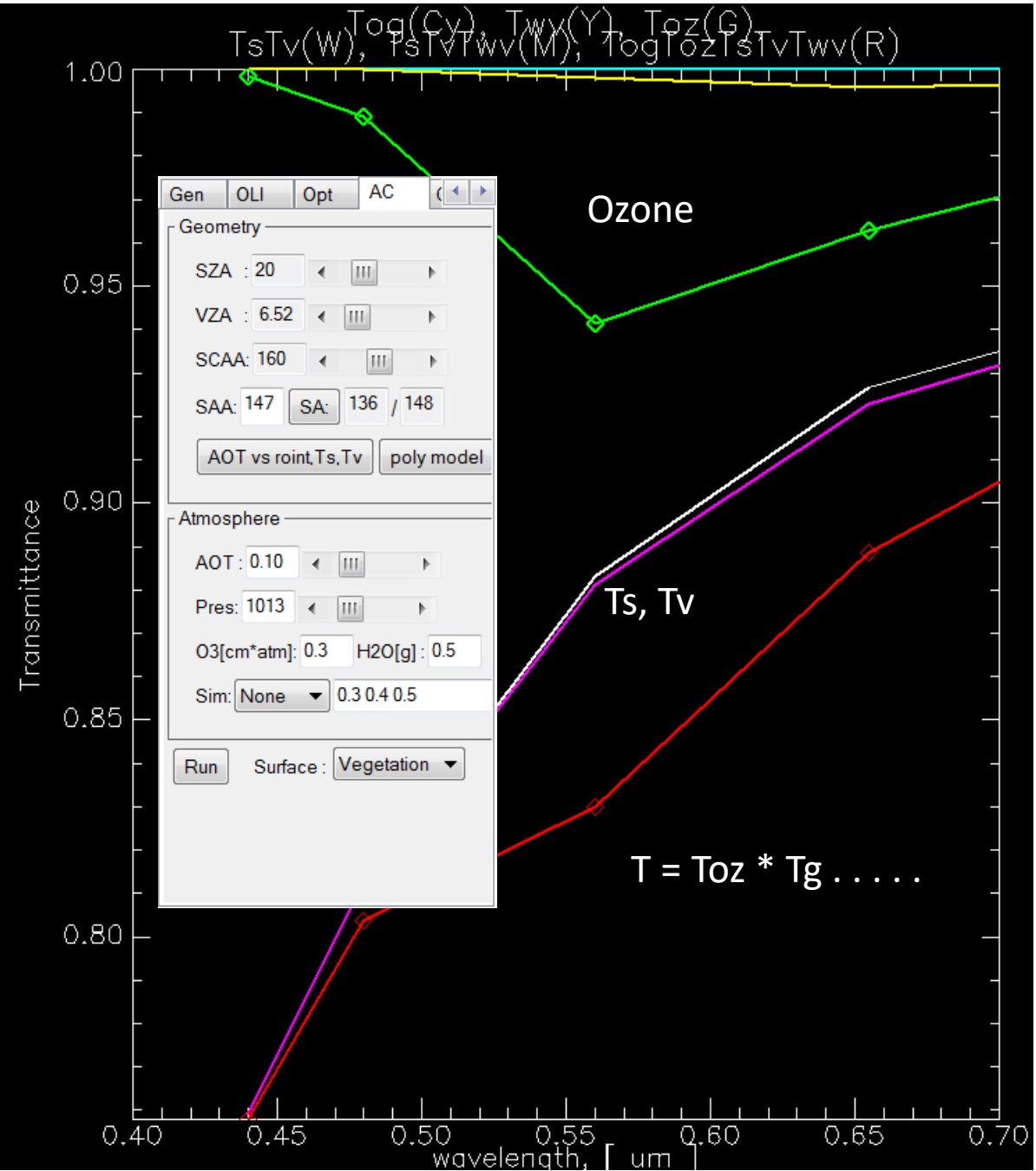
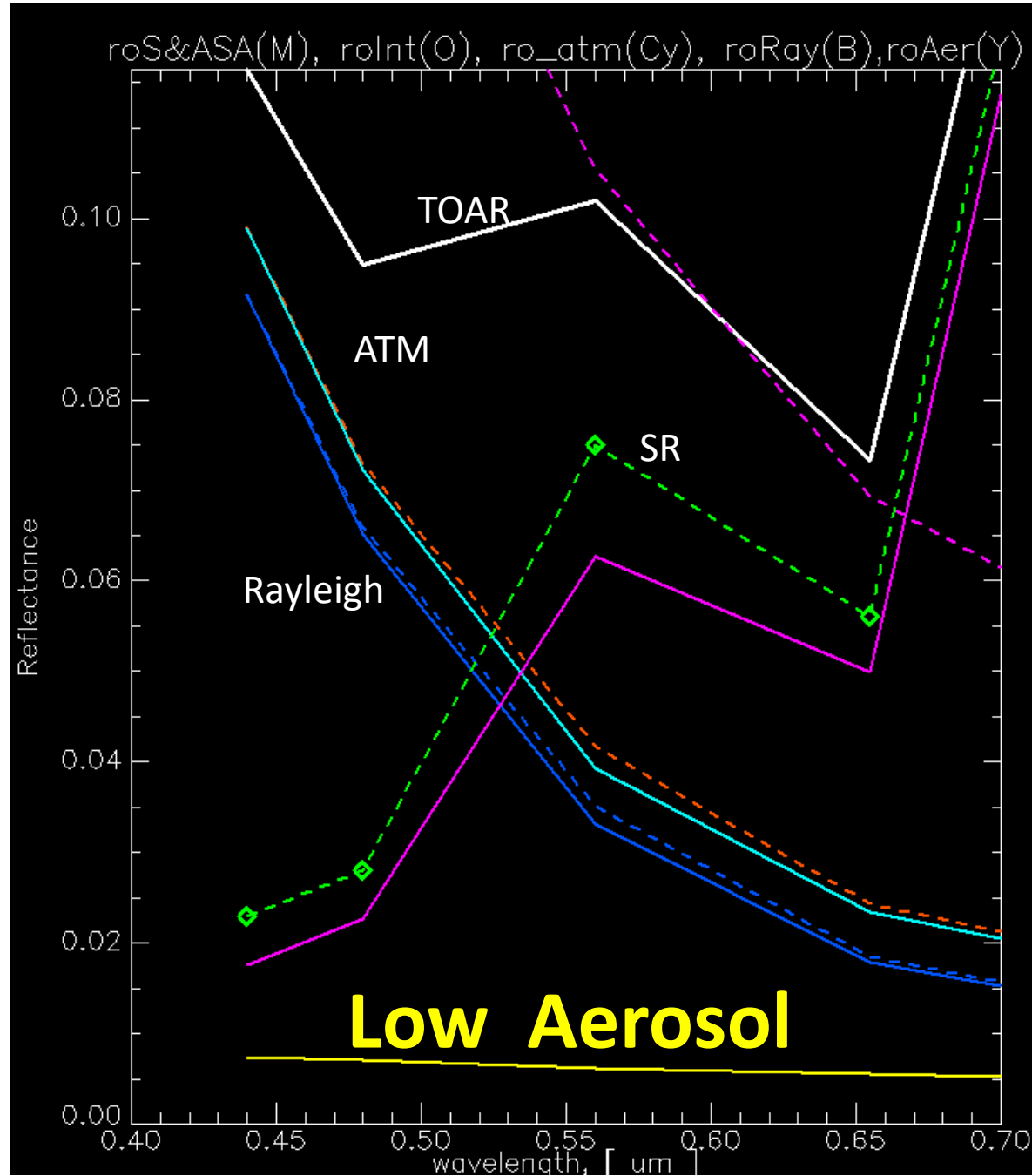


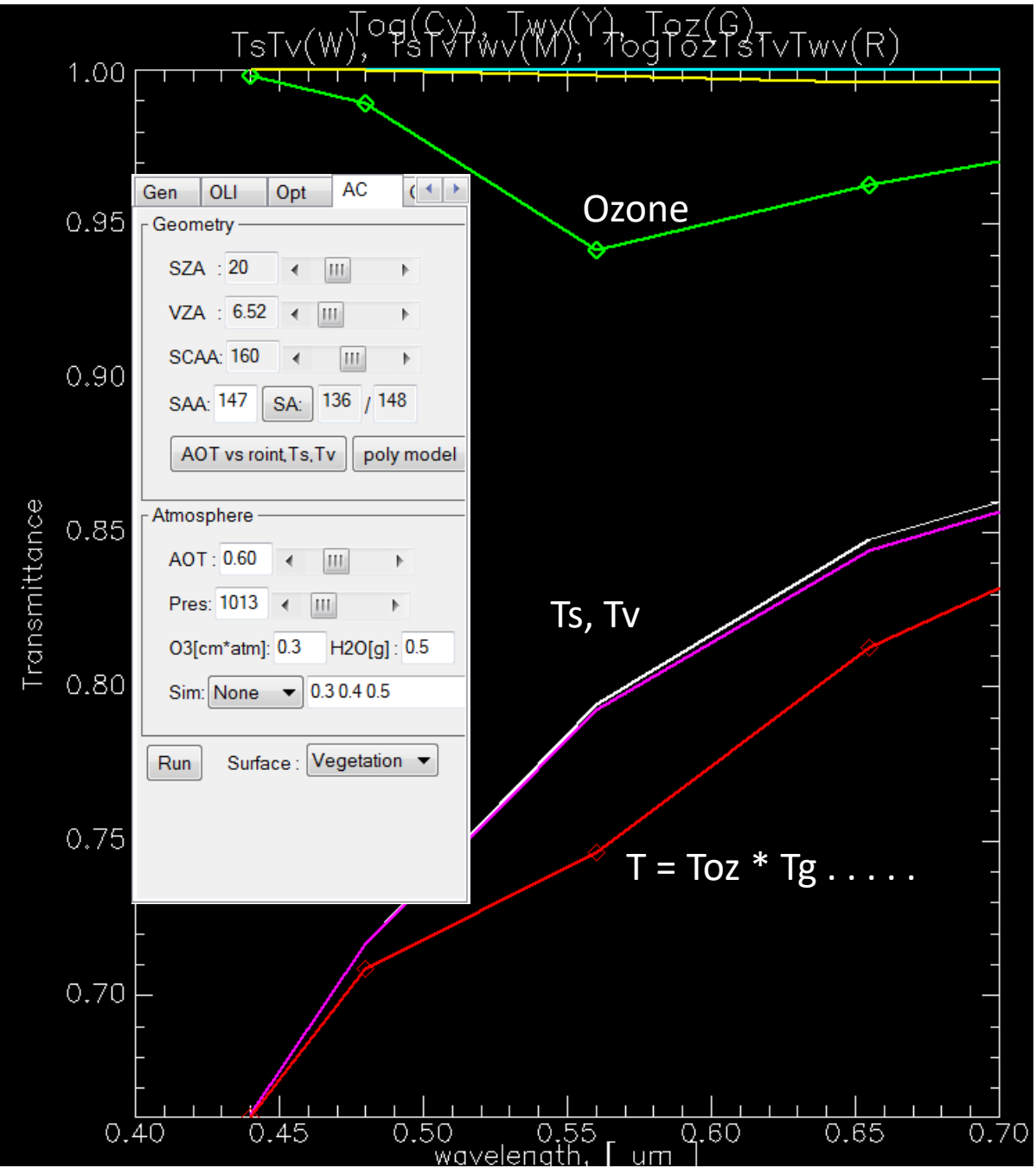
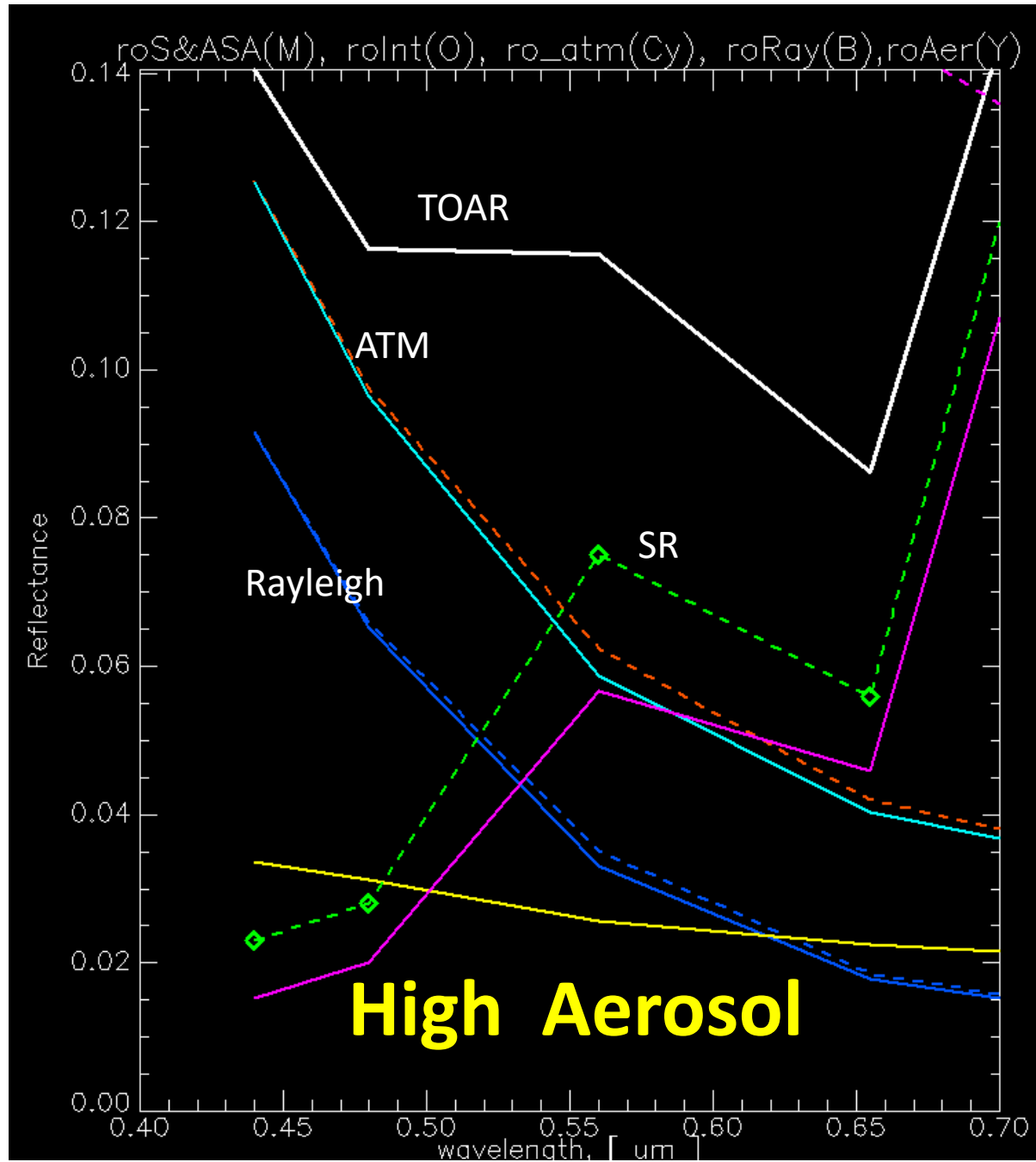
Atmospheric Correction

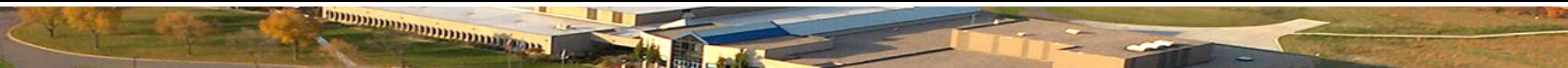
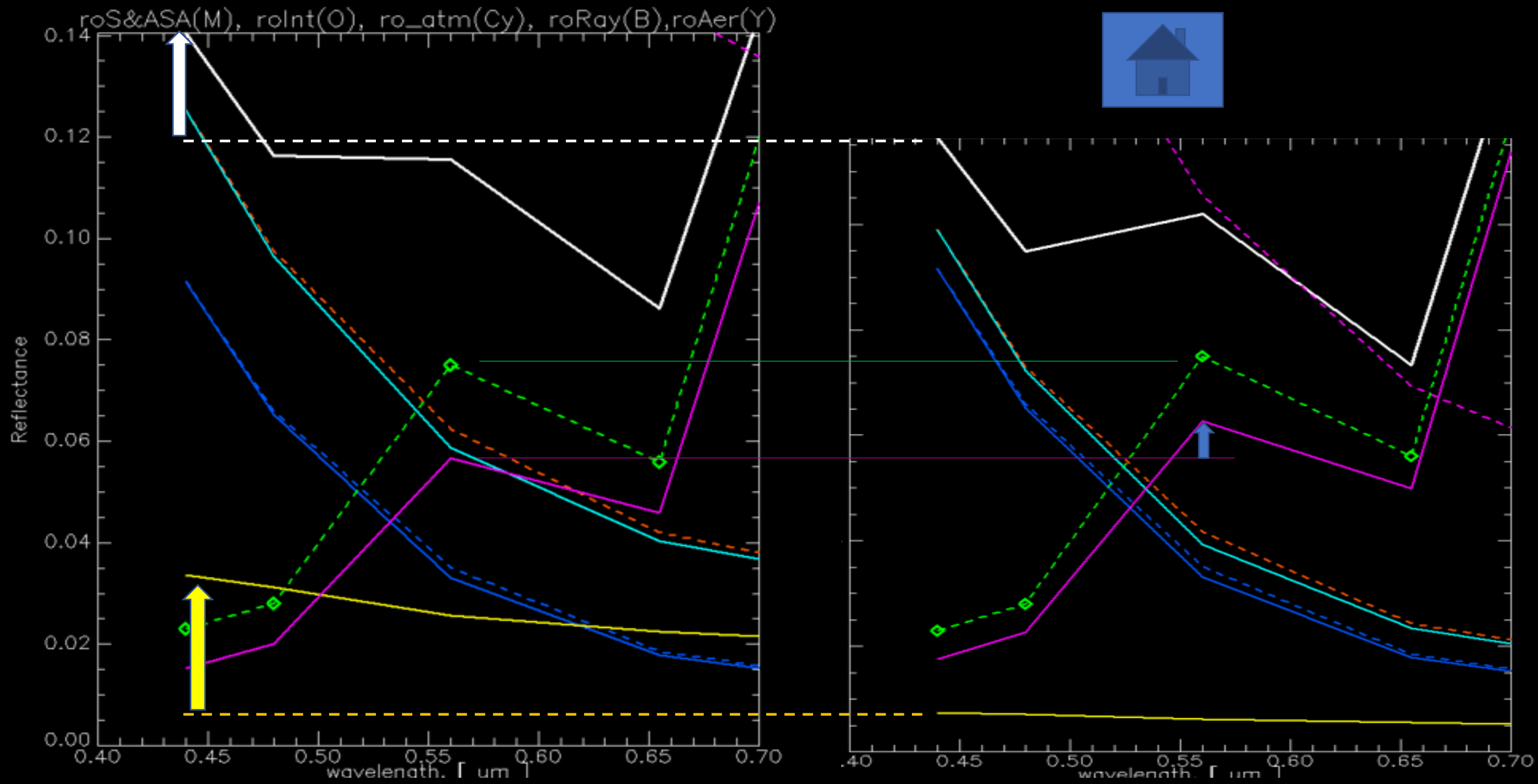


TOAR → Atmospheric Correction → SR









Governing Eq.

$$L_{TOA} = L_{atm} + L_{ground}$$

$$\frac{\rho}{\pi} E_d \cdot (e^{-\tau/\mu_v} + t_d(\theta_v))$$

$$L_{TOA} = L_{atm} + \frac{\rho}{\pi} \mu_s E_o \cdot (e^{-\tau/\mu_s} + t_d(\theta_s)) \frac{1}{1 - \rho S} (e^{-\tau/\mu_v} + t_d(\theta_v))$$

$$L_{TOA} = L_{atm} + \frac{\rho}{\pi} \mu_s E_o \cdot T_s \frac{1}{1 - \rho S} T_v$$

$$\rho_{TOA} = \rho_{atm} + \frac{\rho T_s T_v}{1 - \rho S}$$

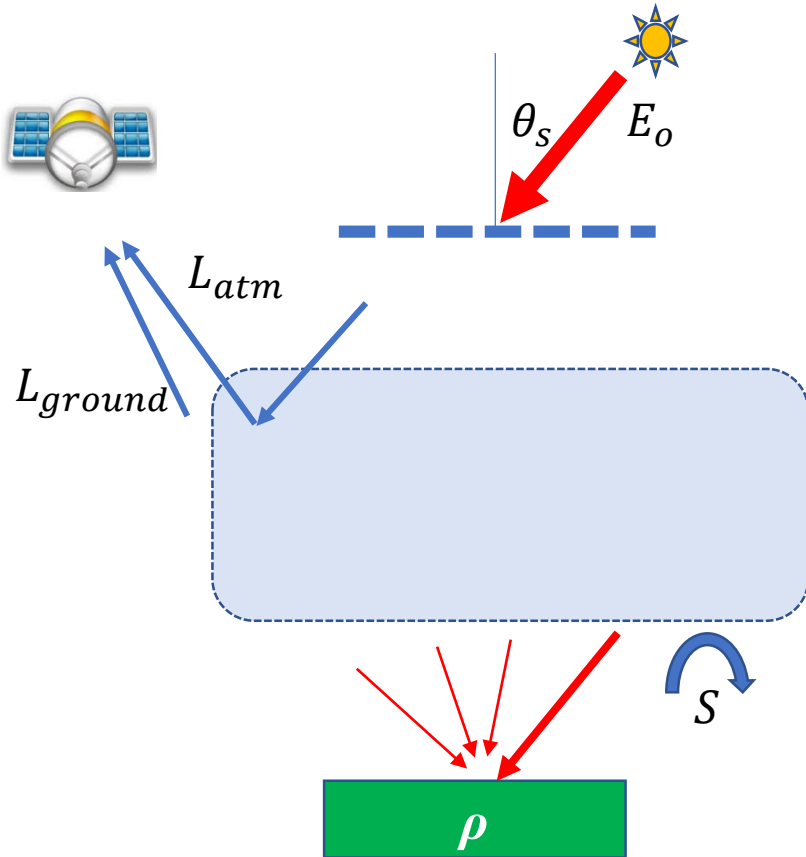
$$\rho_{TOA} = T_g^{og} T_g^{oz} T_g^{cww} \left[\rho_{atm} + \frac{\rho T_s T_v}{1 - \rho S} \right]$$

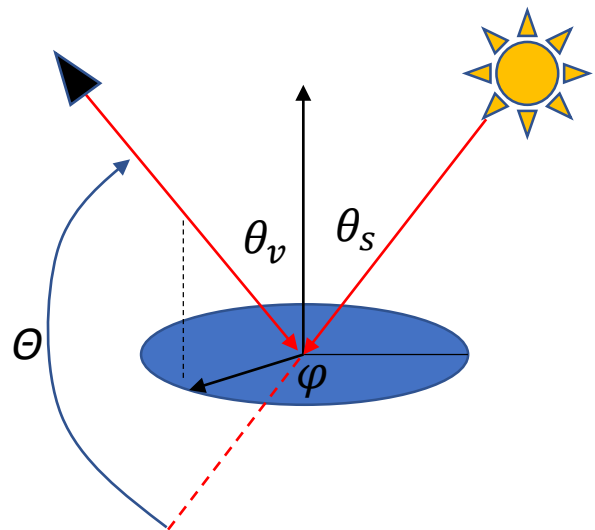
$$E_d = \mu_s E_o \cdot (e^{-\tau/\mu_s} + t_d(\theta_s)) \frac{1}{1 - \rho S}$$

total downwelling irradiance

$$\rho_{TOA} = T_g^{og} T_g^{oz} T_g^{cww} \left[\{(\rho_{atm}^{int} - \rho_{Ray}) \cdot T_{g,Half}^{cww} + \rho_{Ray}\} / T_g^{cww} + \frac{\rho T_s T_v}{1 - \rho S} \right]$$

6S modification (Coupling: Abs-Scat interaction)





$$\cos\Theta = -\cos\theta_s\cos\theta_v - \cos\varphi\sin\theta_s\sin\theta_v$$

$$= -\mu_s\mu_v - \cos\varphi\sqrt{1-\mu_s\mu_s}\sqrt{1-\mu_v\mu_v}$$

scattering angle

$$\rho_i = f(\rho_{TOA_i}, \lambda_i; \tau_a, P, U_{oz}, U_{wv}, \theta_s, \theta_s, \varphi)$$

SR

$\sigma_{\theta_s}, \sigma_{\theta_v}, \sigma_{\varphi} \sim 0$

$$\rho_i = f(\rho_{TOA_i}, \lambda_i; \tau_a, P, U_{oz}, U_{wv})$$

$$TPU = J \cdot \Sigma \cdot J^T$$

$$\begin{bmatrix} \sigma_{\rho_1} \\ \vdots \\ \sigma_{\rho_N} \end{bmatrix} = \begin{bmatrix} \frac{\partial \rho_1}{\partial \tau_a} & \cdots & \frac{\partial \rho_1}{\partial U_{wv}} \\ \vdots & \ddots & \vdots \\ \frac{\partial \rho_N}{\partial \tau_a} & \cdots & \frac{\partial \rho_N}{\partial U_{wv}} \end{bmatrix} \begin{bmatrix} \sigma_{\tau_a}^2 & \cdots & \sigma_{U_{wv}} \sigma_{\tau_a} \\ \vdots & \ddots & \vdots \\ \sigma_{\tau_a} \sigma_{U_{wv}} & \cdots & \sigma_{U_{wv}}^2 \end{bmatrix} \begin{bmatrix} \frac{\partial \rho_1}{\partial \tau_a} & \cdots & \frac{\partial \rho_N}{\partial \tau_a} \\ \vdots & \ddots & \vdots \\ \frac{\partial \rho_1}{\partial U_{wv}} & \cdots & \frac{\partial \rho_N}{\partial U_{wv}} \end{bmatrix}$$

TPU after ATCOR ATCOR TPU Before-ATCOR TPU (Rad.Corr. Etc)

$$(\sigma_{\rho_i})^2 \leq (\sigma_{\rho_i})^2 + (\sigma_{TOA_i})^2$$

Assuming negligible covariances

$$(\sigma_{\rho_i})^2 = \left(\frac{\partial \rho_i}{\partial \tau_a} \sigma_{\tau_a} \right)^2 + \left(\frac{\partial \rho_i}{\partial P} \sigma_P \right)^2 + \left(\frac{\partial \rho_i}{\partial U_{oz}} \sigma_{U_{oz}} \right)^2 + \left(\frac{\partial \rho_i}{\partial U_{wv}} \sigma_{U_{wv}} \right)^2$$

Surface reflectance Equation (← Atmospheric Correction)



SR

$$\rho = \frac{\frac{\rho_{TOA}}{T_g} - \rho_{atm}^{int}}{T_s T_v + \left(\frac{\rho_{TOA}}{T_g} - \rho_{atm}^{int} \right) \cdot S}, T_g = T_g^{og} T_g^{oz} T_g^{cwv}$$



$$(\sigma_{\rho_i})^2 = \left(\frac{\partial \rho_i}{\partial \tau_a} \sigma_{\tau_a} \right)^2 + \left(\frac{\partial \rho_i}{\partial P} \sigma_P \right)^2 + \left(\frac{\partial \rho_i}{\partial U_{oz}} \sigma_{U_{oz}} \right)^2 + \left(\frac{\partial \rho_i}{\partial U_{wv}} \sigma_{U_{wv}} \right)^2 + \dots$$

τ_a terms : $F(\tau_a)$

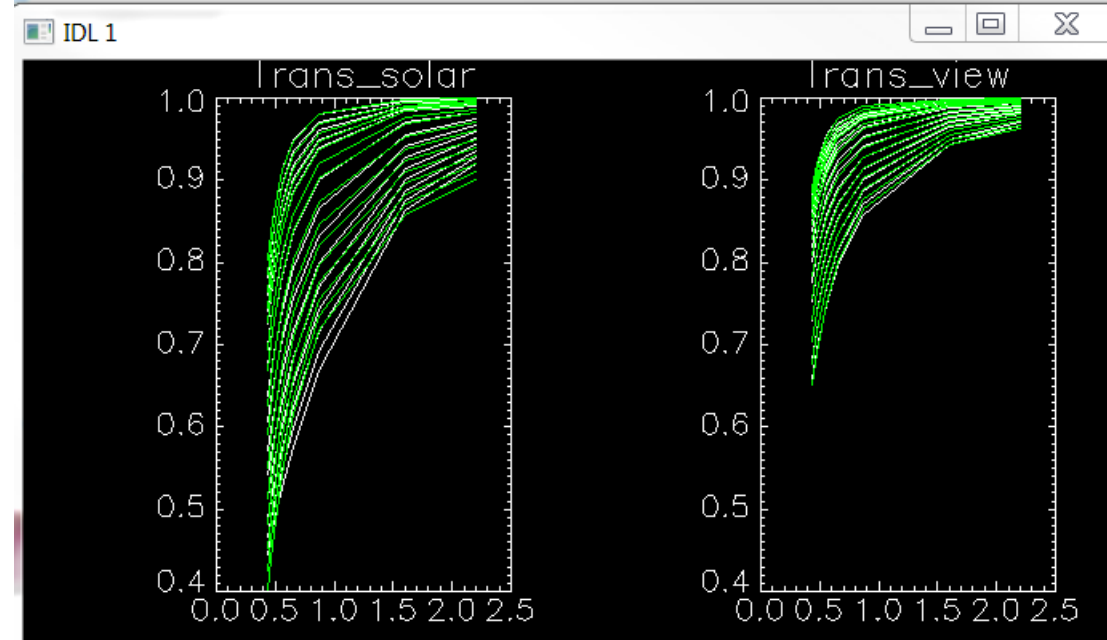
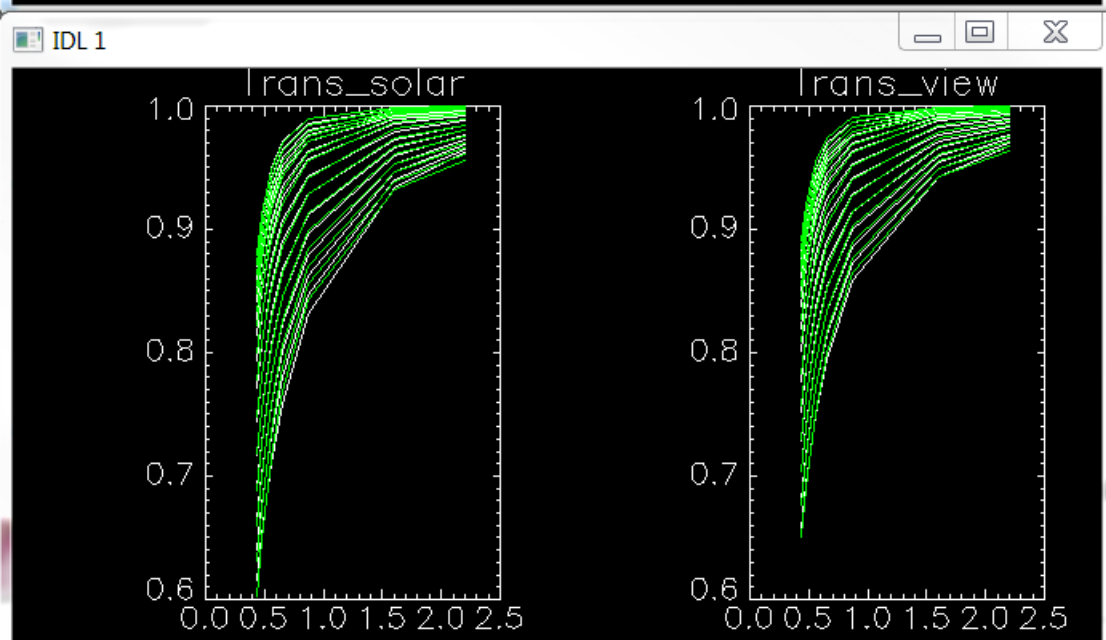
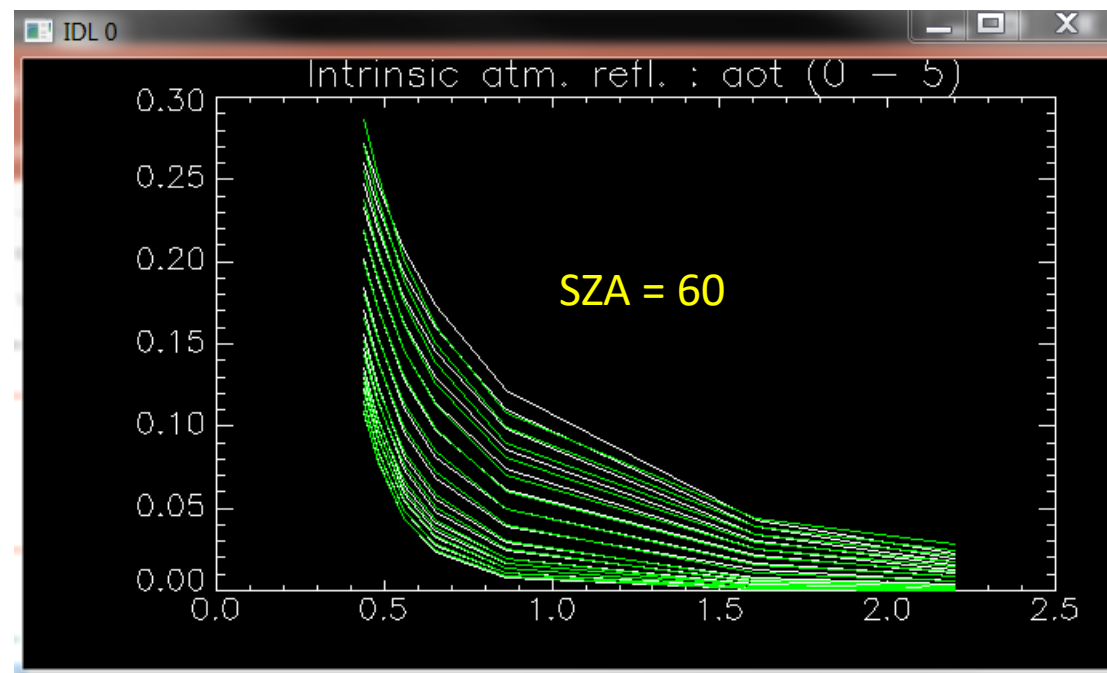
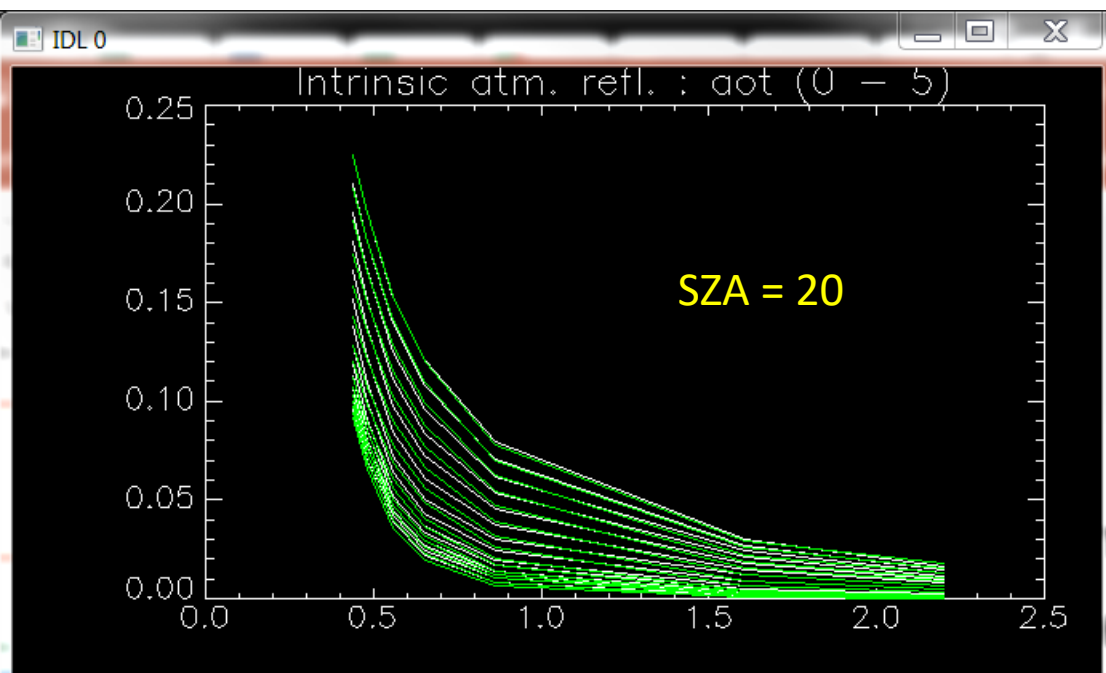
$$\frac{\partial \rho}{\partial \tau_a} = \frac{-\frac{\partial \rho_{atm}^{int}}{\partial \tau_a} \left[T_s T_v + \left(\frac{\rho_{TOA}}{T_g} - \rho_{atm}^{int} \right) S \right] - \left(\frac{\rho_{TOA}}{T_g} - \rho_{atm}^{int} \right) \left[\frac{\partial T_s}{\partial \tau_a} T_v + \frac{\partial T_v}{\partial \tau_a} T_s + \left(\frac{\rho_{TOA}}{T_g} \right) \frac{\partial S}{\partial \tau_a} - \left(\frac{\partial \rho_{atm}^{int}}{\partial \tau_a} S + \rho_{atm}^{int} \frac{\partial S}{\partial \tau_a} \right) \right]}{\left[T_s T_v + \left(\frac{\rho_{TOA}}{T_g} - \rho_{atm}^{int} \right) S \right]^2}$$

τ_a derivative terms : $\partial F(\tau_a) / \partial \tau_a$



$$\begin{aligned} T_s &\sim f(\lambda; P, \tau_a, \theta_s) & S &\sim f(\lambda; P, \tau_a) \\ T_v &\sim f(\lambda; P, \tau_a, \theta_v) & \rho_{atm}^{int} &\sim f(\lambda; P, \tau_a, \theta) \end{aligned}$$



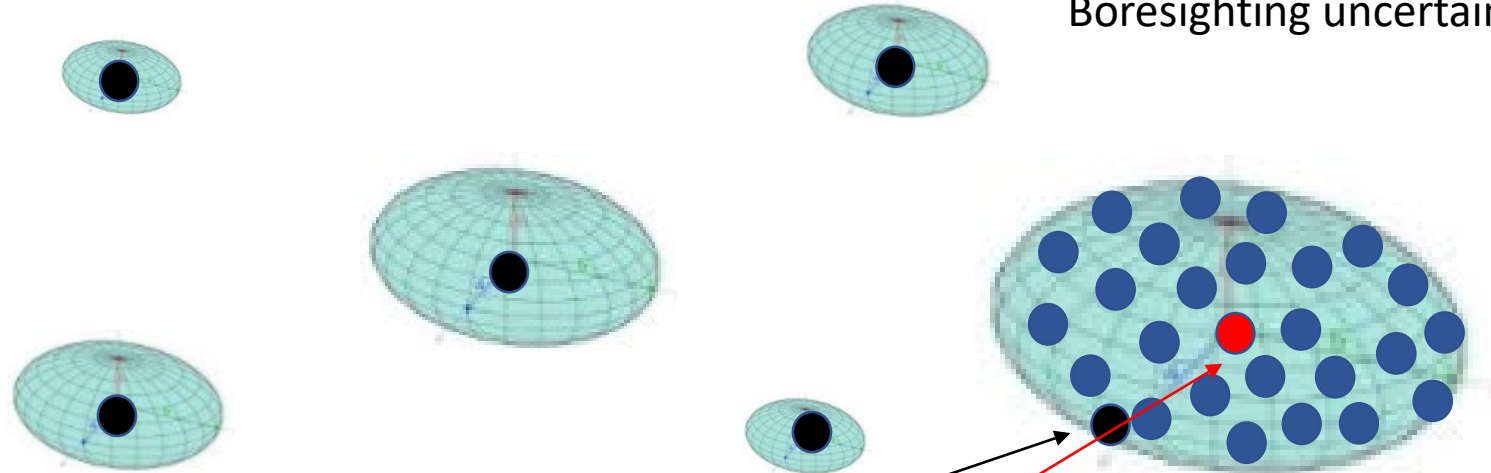


measurement uncertainty ←

GNSS position uncertainty
IMU orientation uncertainty
Ranging uncertainty
Scanner uncertainty
Boresighting uncertainty



TPU ellipsoid

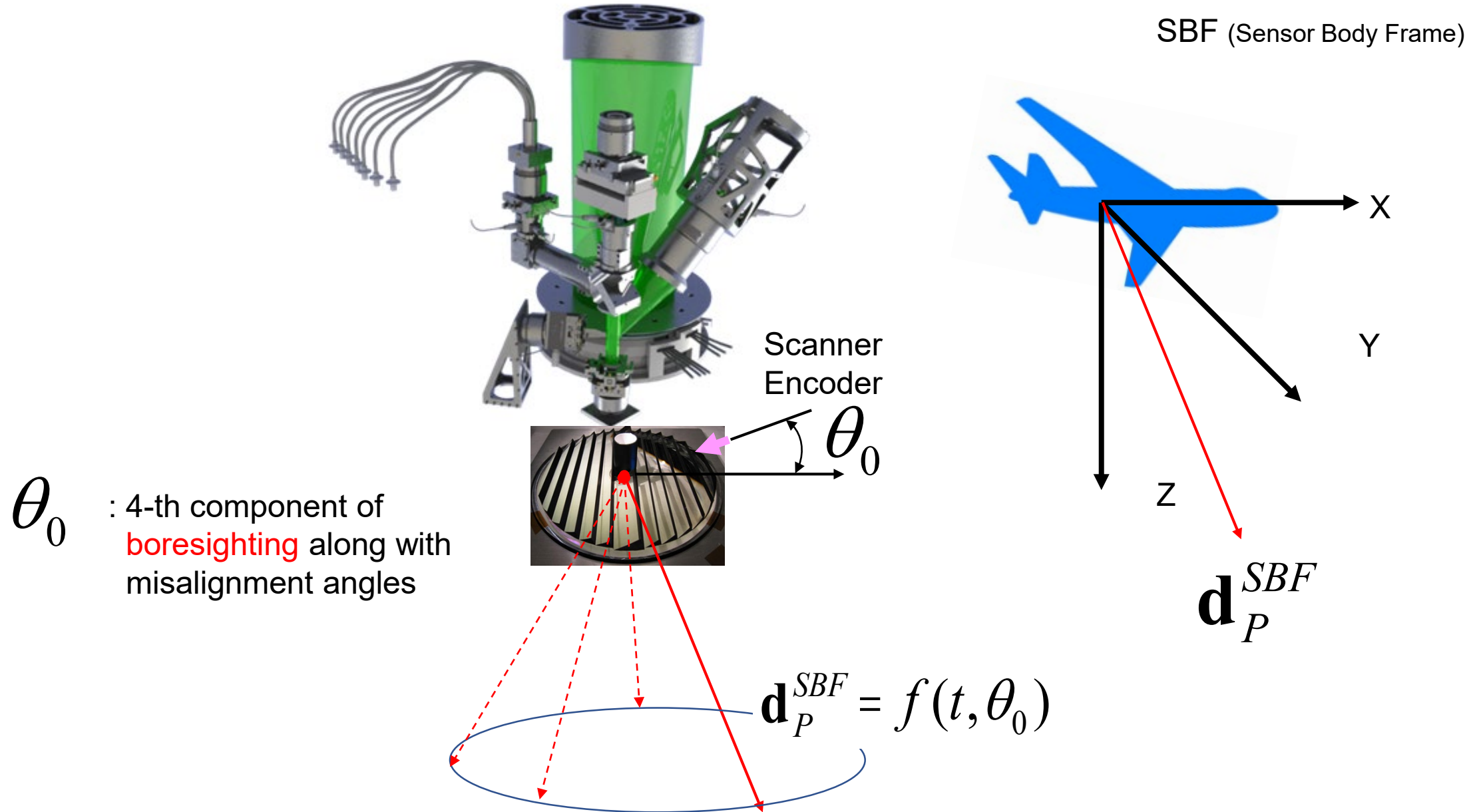


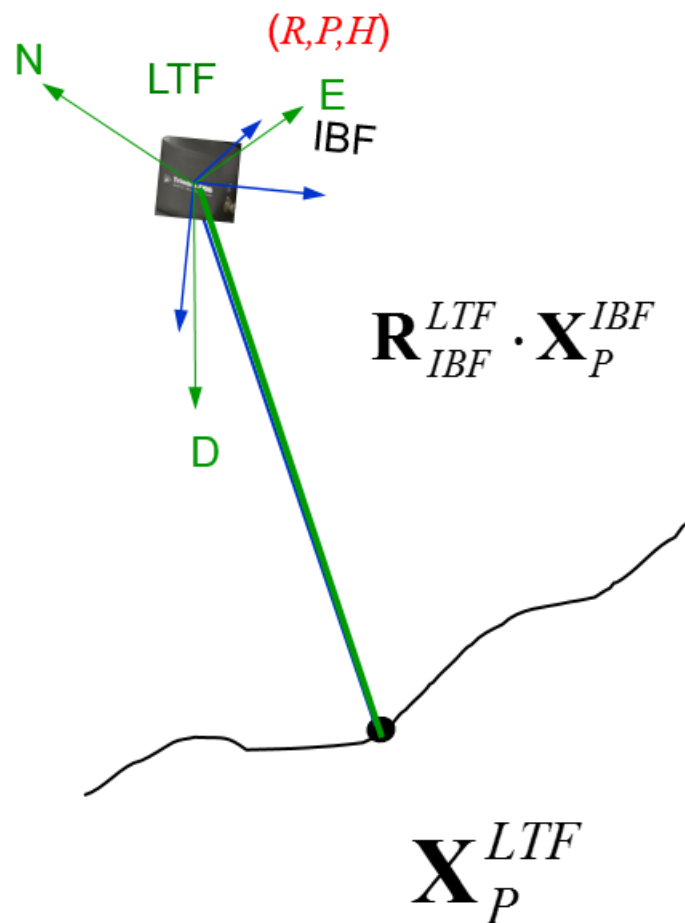
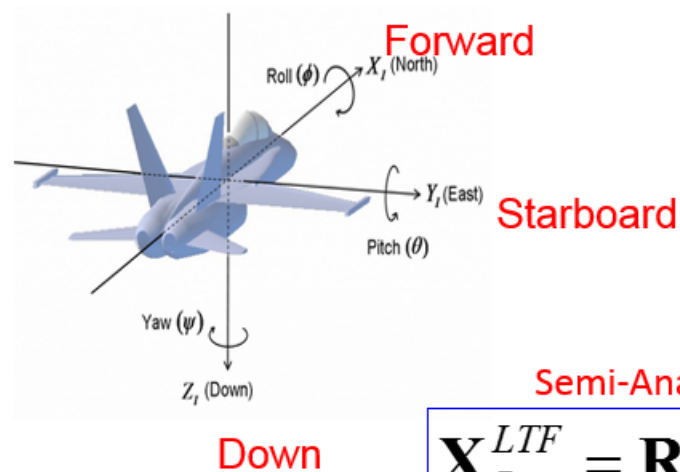
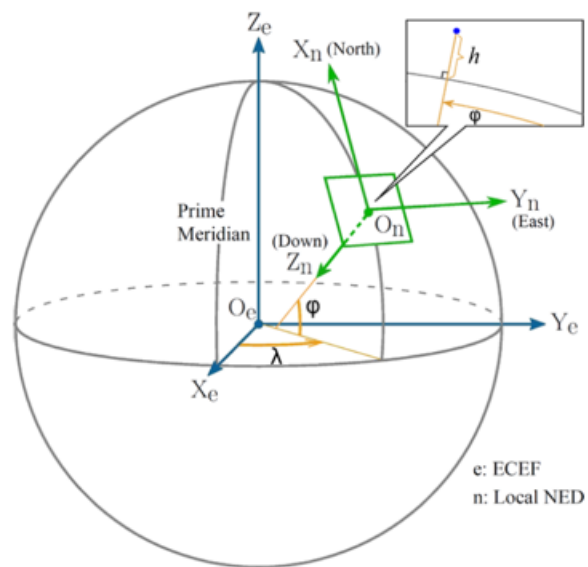
Lidar point : a specific realization
based on measurement uncertainty

True point : **unknown** (exist only in the simulation)

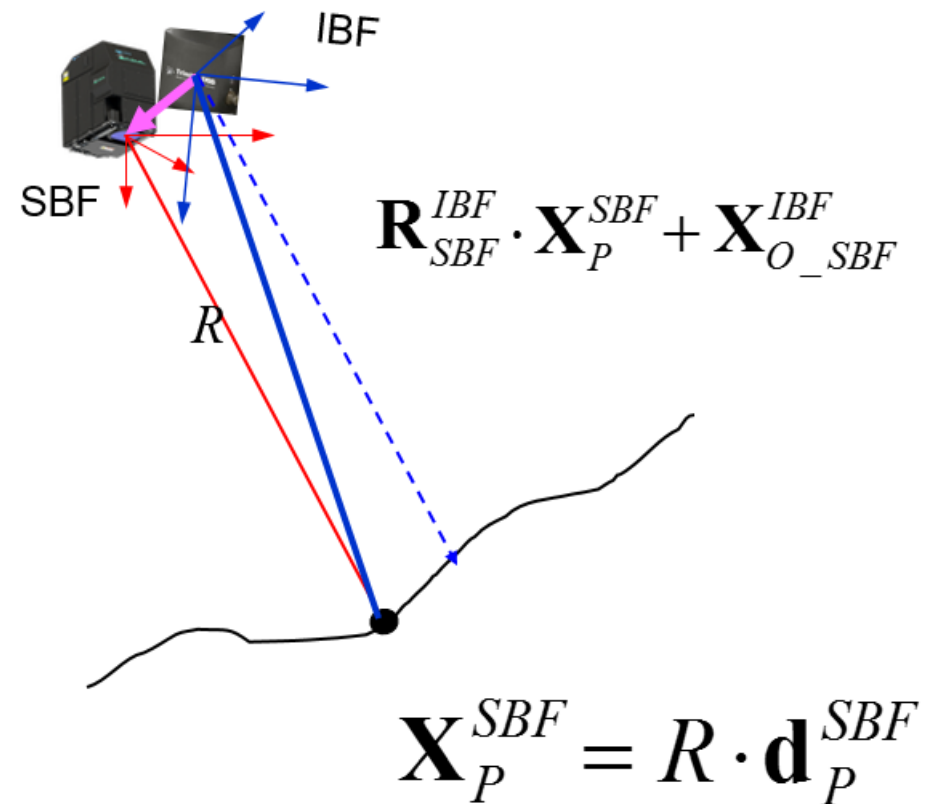
TPU : uncertainty cloud (center : true point)

Direct Georeferencing of lidar point





Boresight angles (ω, φ, κ)



Semi-Analytical TPU calculation usually stops here.

$$\mathbf{X}_P^{LTF} = \mathbf{R}_{IBF}^{LTF} \cdot (\mathbf{R}_{SBF}^{IBF} \cdot \rho \cdot \mathbf{n}_P^{SBF} + \mathbf{X}_{O_SBF}^{IBF}) + \mathbf{X}_{O_IBF}^{LTF}$$

Uncertainty : calibration parameters

SBF-IBF misalignment [deg] :

omega	phi	kappa
<input type="text" value="0.02"/>	<input type="text" value="0.02"/>	<input type="text" value="0.02"/>
1	2	3

O_SBF position in IBF [m] :

x	y	z
<input type="text" value="0.02"/>	<input type="text" value="0.02"/>	<input type="text" value="0.02"/>
4	5	6

Uncertainty : measurement parameters

POSAV510 ▼

O_IBF GNSS position in LTF [m] :

x	y	z
<input type="text" value="0.1"/>	<input type="text" value="0.1"/>	<input type="text" value="0.3"/>
7	8	9

IMU orientation [deg] :

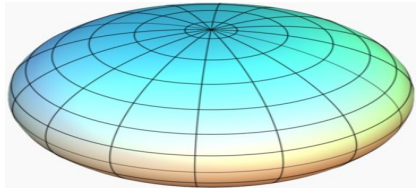
Roll	Pitch	Heading
<input type="text" value="0.005"/>	<input type="text" value="0.005"/>	<input type="text" value="0.008"/>
10	11	12

Range uncertainty [m] : 13

Scan angle uncertainty [deg] : 14

$$\begin{bmatrix} \sigma_x^2 & \sigma_x \sigma_y & \sigma_x \sigma_z \\ \sigma_y \sigma_x & \sigma_y^2 & \sigma_y \sigma_z \\ \sigma_z \sigma_x & \sigma_z \sigma_y & \sigma_z^2 \end{bmatrix} = \mathbf{J} \begin{bmatrix} \sigma_{x_0}^2 & 0 & 0 \\ 0 & \ddots & 0 \\ 0 & 0 & \sigma_{\kappa}^2 \end{bmatrix} \mathbf{J}^T$$

14 x 14



$$\mathbf{J} = \begin{bmatrix} \frac{\partial x}{\partial x_0} & \frac{\partial x}{\partial y_0} & \frac{\partial x}{\partial z_0} & \frac{\partial x}{\partial x_1} & \frac{\partial x}{\partial y_1} & \frac{\partial x}{\partial z_1} & \frac{\partial x}{\partial \rho} & \frac{\partial x}{\partial \theta} & \frac{\partial x}{\partial R} & \frac{\partial x}{\partial P} & \frac{\partial x}{\partial H} & \frac{\partial x}{\partial \omega} & \frac{\partial x}{\partial \varphi} & \frac{\partial x}{\partial \kappa} \\ \frac{\partial y}{\partial x_0} & \frac{\partial y}{\partial y_0} & \frac{\partial y}{\partial z_0} & \frac{\partial y}{\partial x_1} & \frac{\partial y}{\partial y_1} & \frac{\partial y}{\partial z_1} & \frac{\partial y}{\partial \rho} & \frac{\partial y}{\partial \theta} & \frac{\partial y}{\partial R} & \frac{\partial y}{\partial P} & \frac{\partial y}{\partial H} & \frac{\partial y}{\partial \omega} & \frac{\partial y}{\partial \varphi} & \frac{\partial y}{\partial \kappa} \\ \frac{\partial z}{\partial x_0} & \frac{\partial z}{\partial y_0} & \frac{\partial z}{\partial z_0} & \frac{\partial z}{\partial x_1} & \frac{\partial z}{\partial y_1} & \frac{\partial z}{\partial z_1} & \frac{\partial z}{\partial \rho} & \frac{\partial z}{\partial \theta} & \frac{\partial z}{\partial R} & \frac{\partial z}{\partial P} & \frac{\partial z}{\partial H} & \frac{\partial z}{\partial \omega} & \frac{\partial z}{\partial \varphi} & \frac{\partial z}{\partial \kappa} \end{bmatrix}$$



Compact version of TPU equations

$$\mathbf{X}_P^{LTF} = \mathbf{R}_{IBF}^{LTF} \cdot (\mathbf{R}_{SBF}^{IBF} \cdot \rho \cdot \mathbf{d}_P^{SBF} + \mathbf{X}_{O_SBF}^{IBF}) + \mathbf{X}_{O_IBF}^{LTF}$$

$$\begin{bmatrix} x \\ y \\ z \end{bmatrix} = \mathbf{R}_{IBF}^{LTF} \cdot (\mathbf{R}_{SBF}^{IBF} \cdot \rho \cdot \mathbf{d}_P^{SBF} + \begin{bmatrix} x_0 \\ y_0 \\ z_0 \end{bmatrix}) + \begin{bmatrix} x_1 \\ y_1 \\ z_1 \end{bmatrix}$$

$$\begin{aligned} \sigma_x^2 = & \left(\frac{\partial x}{\partial x_0} \sigma_{x_0} \right)^2 + \left(\frac{\partial x}{\partial y_0} \sigma_{y_0} \right)^2 + \left(\frac{\partial x}{\partial z_0} \sigma_{z_0} \right)^2 \\ & + \left(\frac{\partial x}{\partial x_1} \sigma_{x_1} \right)^2 + \left(\frac{\partial x}{\partial y_1} \sigma_{y_1} \right)^2 + \left(\frac{\partial x}{\partial z_1} \sigma_{z_1} \right)^2 + \\ & \left(\frac{\partial x}{\partial \rho} \sigma_\rho \right)^2 + \left(\frac{\partial x}{\partial \theta} \sigma_\theta \right)^2 \\ & + \left(\frac{\partial x}{\partial R} \sigma_R \right)^2 + \left(\frac{\partial x}{\partial P} \sigma_P \right)^2 + \left(\frac{\partial x}{\partial H} \sigma_H \right)^2 \\ & + \left(\frac{\partial x}{\partial \omega} \sigma_\omega \right)^2 + \left(\frac{\partial x}{\partial \varphi} \sigma_\varphi \right)^2 + \left(\frac{\partial x}{\partial \kappa} \sigma_\kappa \right)^2 \end{aligned}$$

$$\begin{bmatrix} \frac{\partial \mathbf{X}_P^{LTF}}{\partial x_0} & \frac{\partial \mathbf{X}_P^{LTF}}{\partial y_0} & \frac{\partial \mathbf{X}_P^{LTF}}{\partial z_0} \end{bmatrix} = \mathbf{R}_{IBF}^{LTF},$$

$$\begin{bmatrix} \frac{\partial \mathbf{X}_P^{LTF}}{\partial x_1} & \frac{\partial \mathbf{X}_P^{LTF}}{\partial y_1} & \frac{\partial \mathbf{X}_P^{LTF}}{\partial z_1} \end{bmatrix} = \mathbf{I}.$$

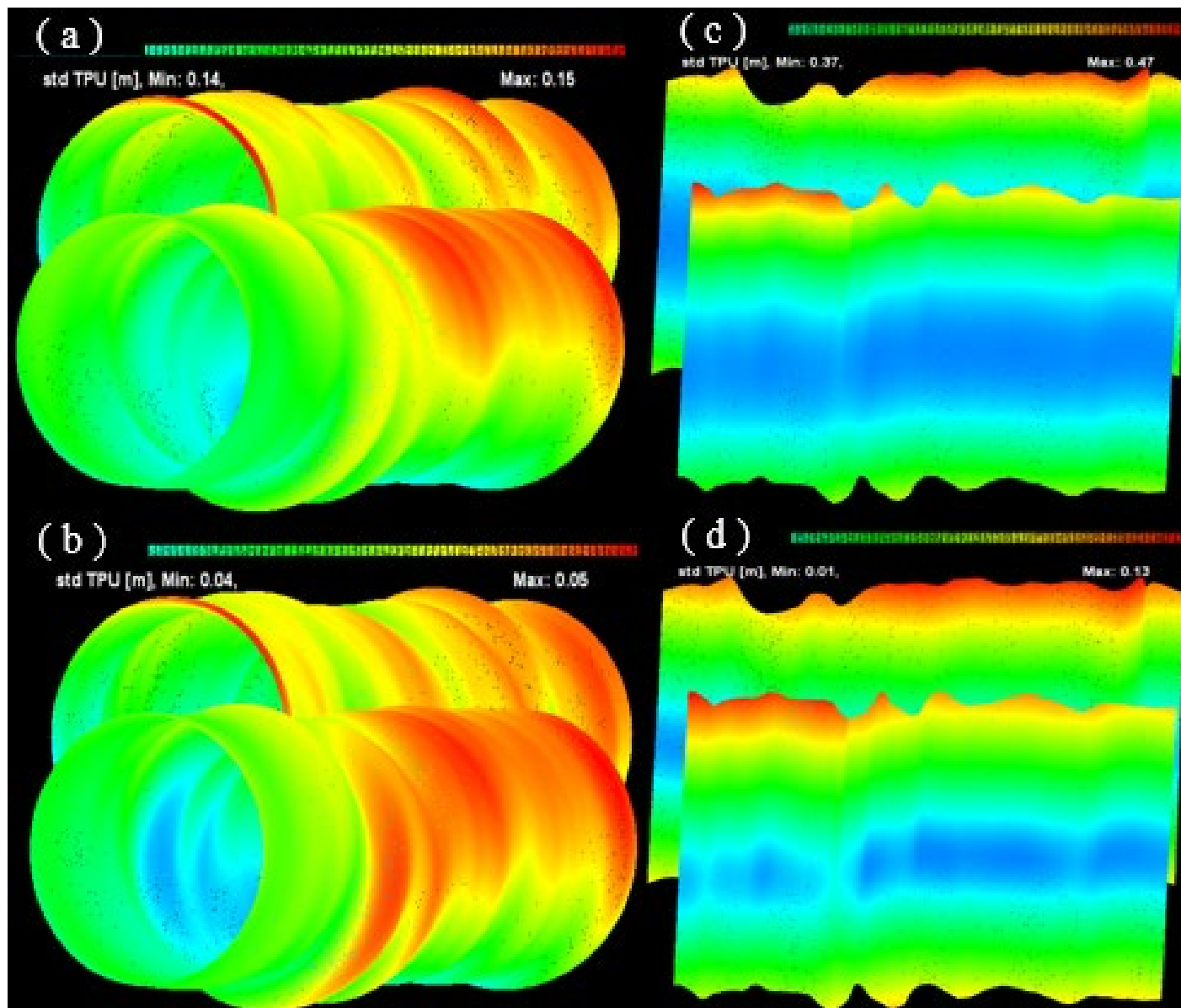
$$\frac{\partial \mathbf{X}_P^{LTF}}{\partial \rho} = \mathbf{R}_{IBF}^{LTF} \cdot \mathbf{R}_{SBF}^{IBF} \cdot \mathbf{d}_P^{SBF},$$

$$\frac{\partial \mathbf{X}_P^{LTF}}{\partial \theta} = \rho \cdot \mathbf{R}_{IBF}^{LTF} \cdot \mathbf{R}_{SBF}^{IBF} \cdot \frac{\partial \mathbf{d}_P^{SBF}}{\partial \theta}.$$

$$\frac{\partial \mathbf{X}_P^{LTF}}{\partial \chi} = \rho \cdot \mathbf{R}_{IBF}^{LTF} \cdot \frac{\partial \mathbf{R}_{SBF}^{IBF}}{\partial \chi} \cdot \mathbf{d}_P^{SBF}, \quad (\chi = \omega, \varphi, \kappa)$$

$$\frac{\partial \mathbf{X}_P^{LTF}}{\partial \chi} = \rho \cdot \frac{\partial \mathbf{R}_{IBF}^{LTF}}{\partial \chi} \cdot \mathbf{R}_{SBF}^{IBF} \cdot \mathbf{d}_P^{SBF}, \quad (\chi = R, P, H)$$





↓ (a), (b)

Circular

POSAV610

GNSS O_IBF in LTF :

x	y	z
0.03	0.03	0.01

IMU orientation [deg] :

Roll	Pitch	Heading
0.003	0.003	0.005

↓ (c), (d)

Galvo-mirror

POSAV210

GNSS O_IBF in LTF :

x	y	z
0.03	0.03	0.01

IMU orientation [deg] :

Roll	Pitch	Heading
0.015	0.015	0.035

(1) Laser P R F [KHz] : 90

Pulse function Gaussian

e^{-2} beam div IFOV [mrad] : 0.25

(2) Scanner Galvo-mirror

Scan Freq [Hz] : 44

HFOV [deg] : 20

AGL[m] : 1000 Overlap [0-1] : 0.6

Speed [kt] (~ 1.15mph ~2 mps) : 120

Swath Length to Width ratio: 1.5

Flight pattern:

SBF-IBF misalignment [deg] :

omega	phi	kappa
0.001	0.001	0.001

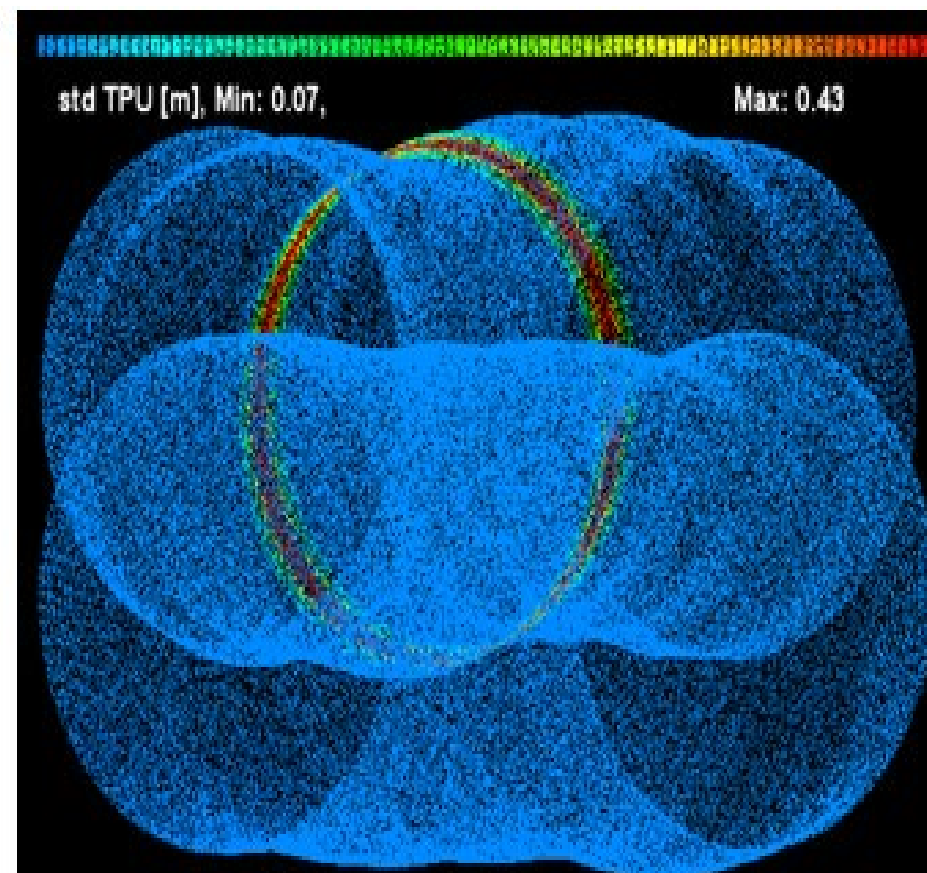
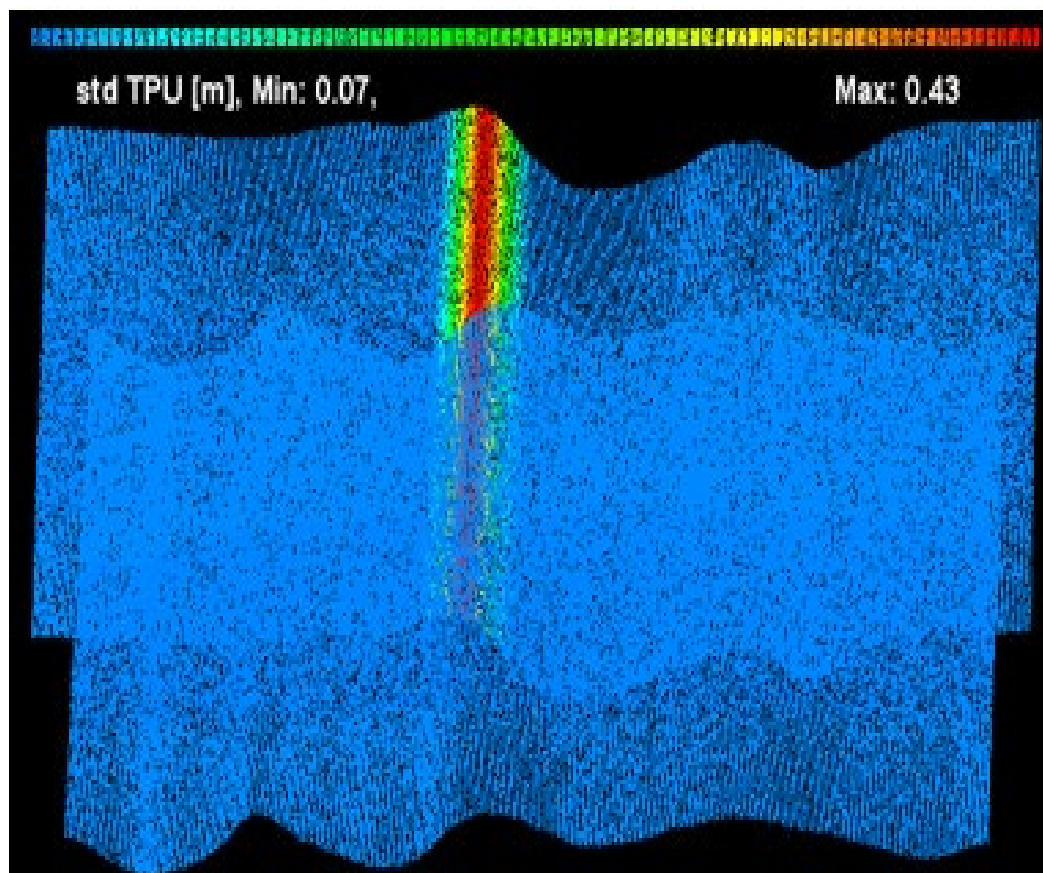
O_SBF position in IBF [m] :

x	y	z
0.001	0.001	0.001

Range uncertainty [m] : 0.01

Scan angle uncertainty [deg] : 0.001

TPU from a momentary poor PDOP



$$\rho_{toa} = [\rho_{B1}, \rho_{B2}, \rho_G, \rho_R, \rho_{NIR}, \rho_{SW1}, \rho_{SW2}]^T$$

TPU_NDVI

$$NDVI = \frac{\rho_{NIR} - \rho_R}{\rho_{NIR} + \rho_R}$$

$$\sigma_{NDVI} = ???$$

$$(\sigma_{NDVI})^2 = \left(\frac{\partial NDVI}{\partial \rho_R} \Big|_{\rho_R, \rho_{NIR}} \cdot \sigma_{\rho_R} \right)^2 + \left(\frac{\partial NDVI}{\partial \rho_{NIR}} \Big|_{\rho_R, \rho_{NIR}} \cdot \sigma_{\rho_{NIR}} \right)^2$$

Because it is a derivative-based approach,
as long as the scientific application is based on
analytical formula, it is applicable.
However, non-analytical, e.g. decision tree,
categorical outcome, etc

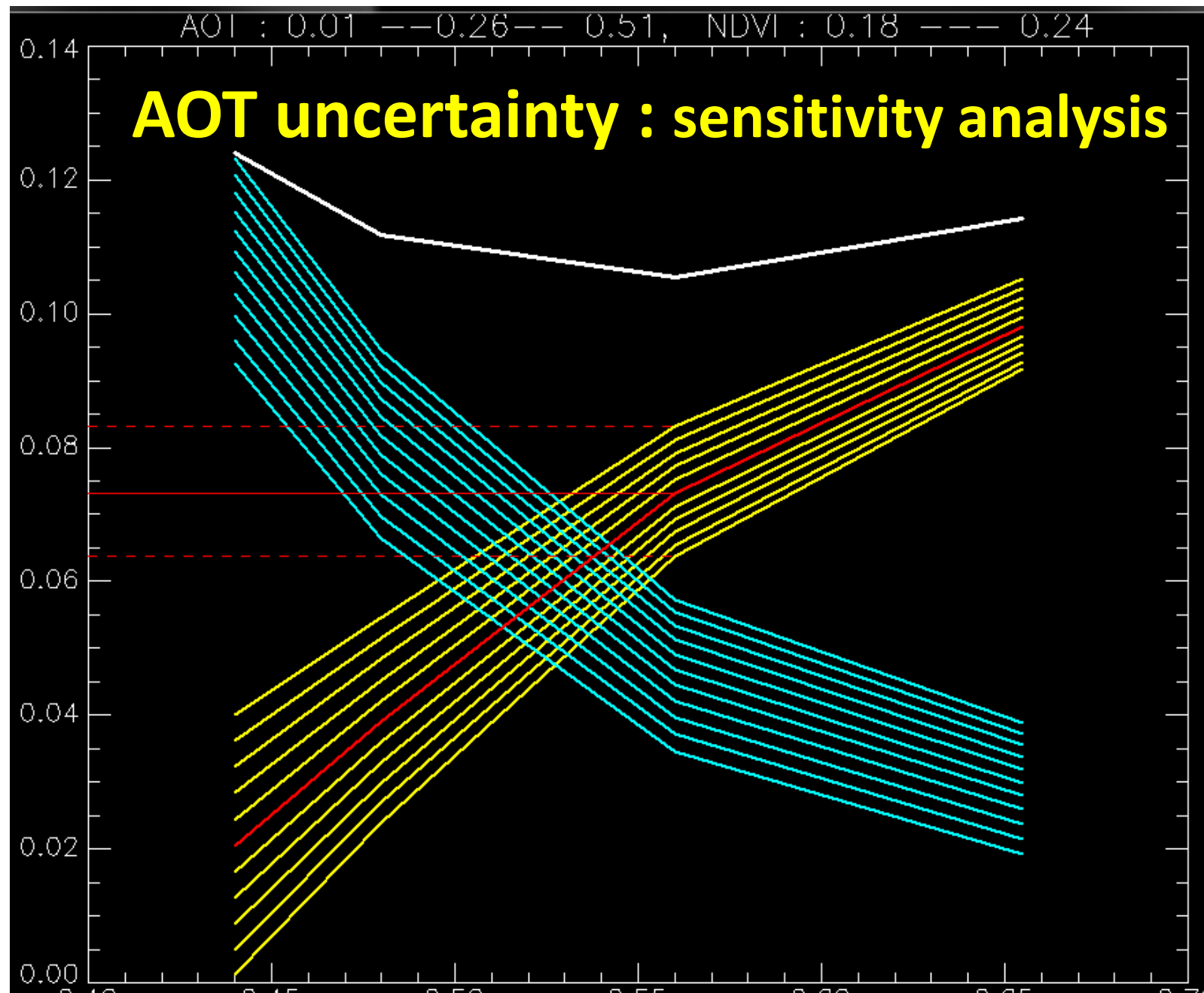
σ_{ρ_R} $\sigma_{\rho_{NIR}}$

Landsat 8 OLI image

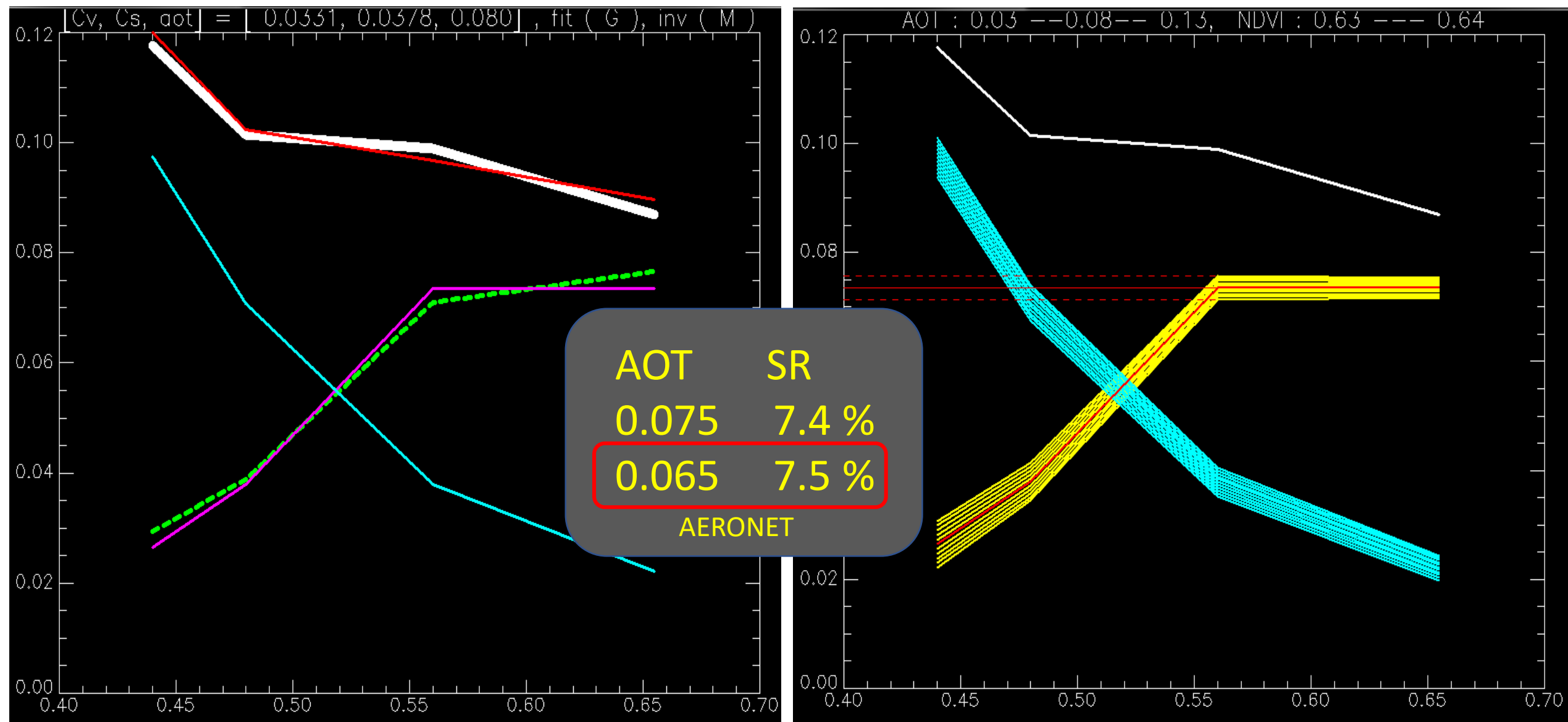
Selective
mosaic
Using TPU

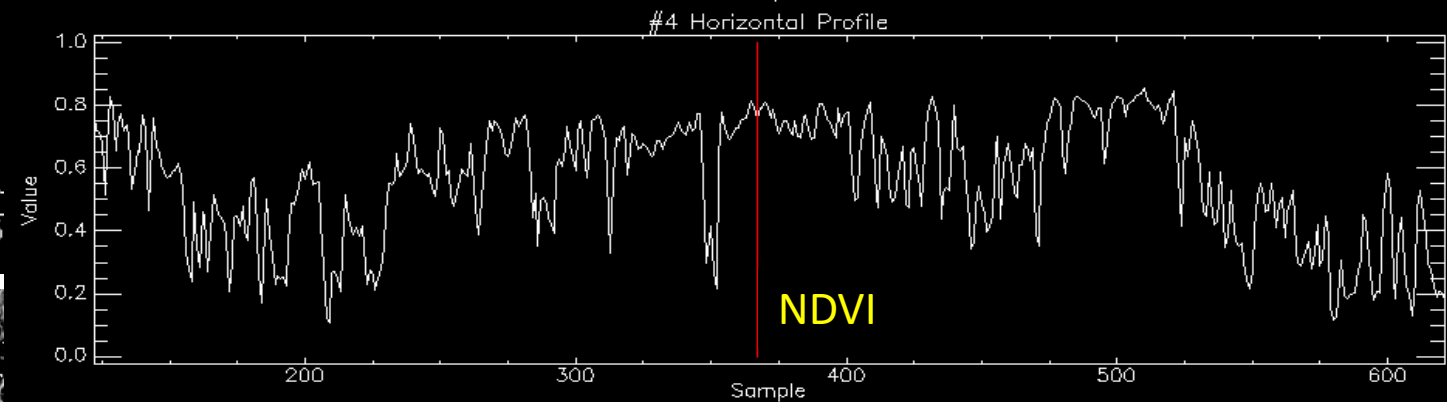
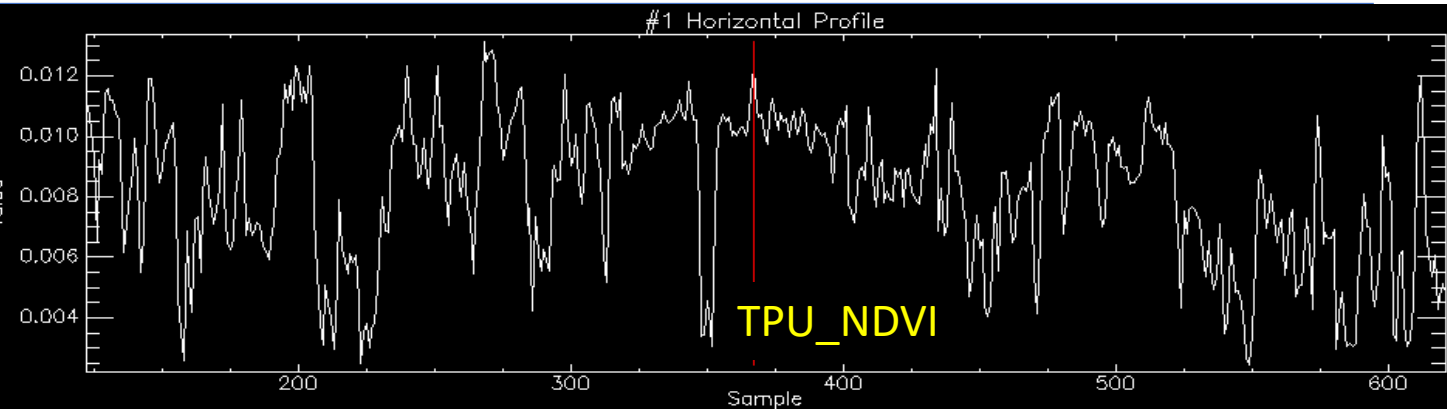
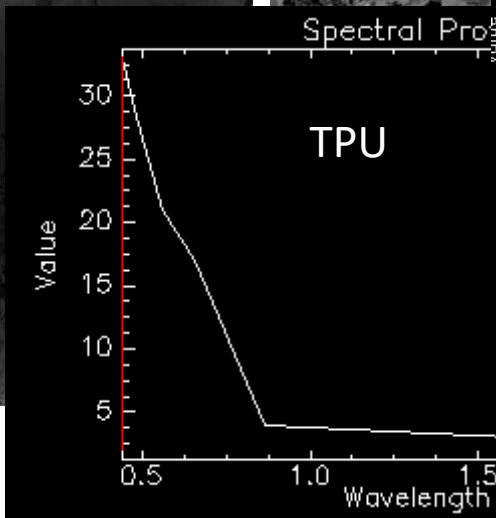
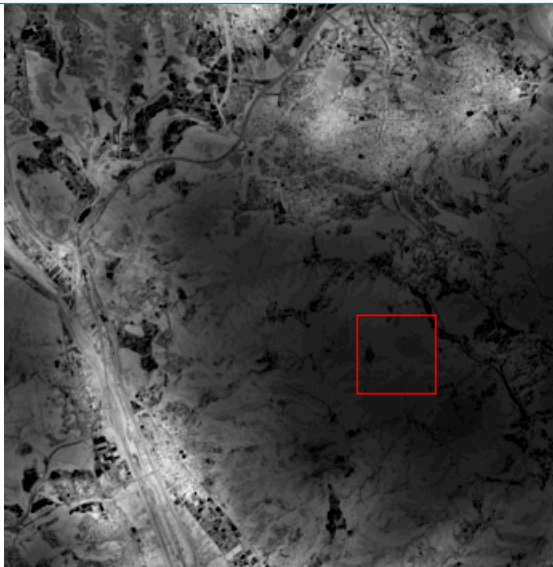
AOT	SR
0.25	7.35 %
0.35	6.95 %

AERONET

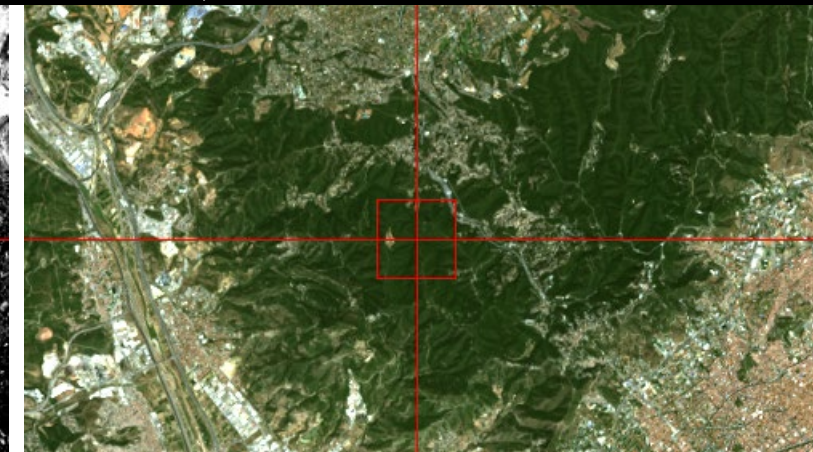
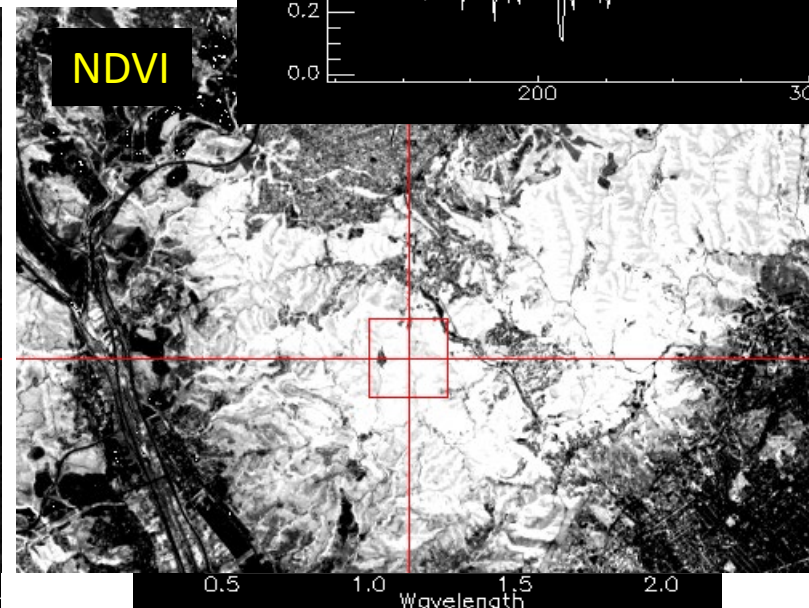
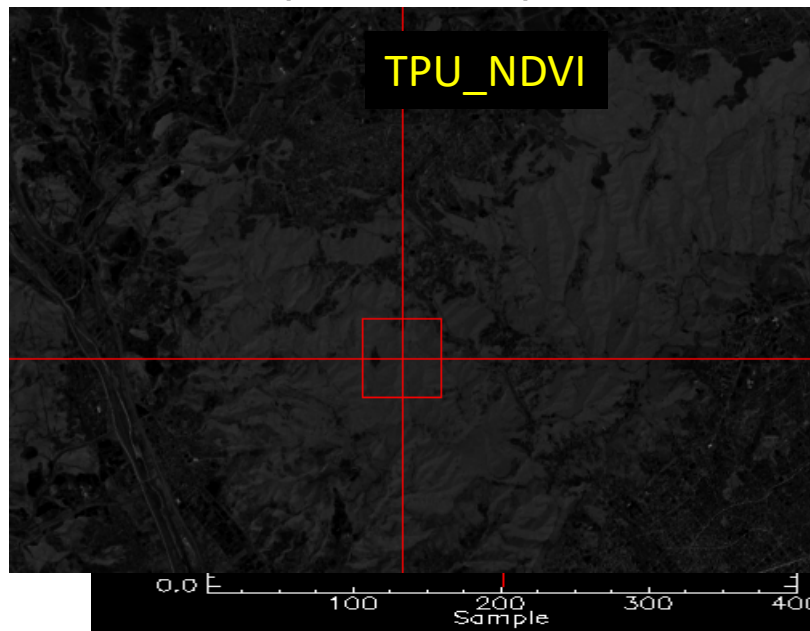


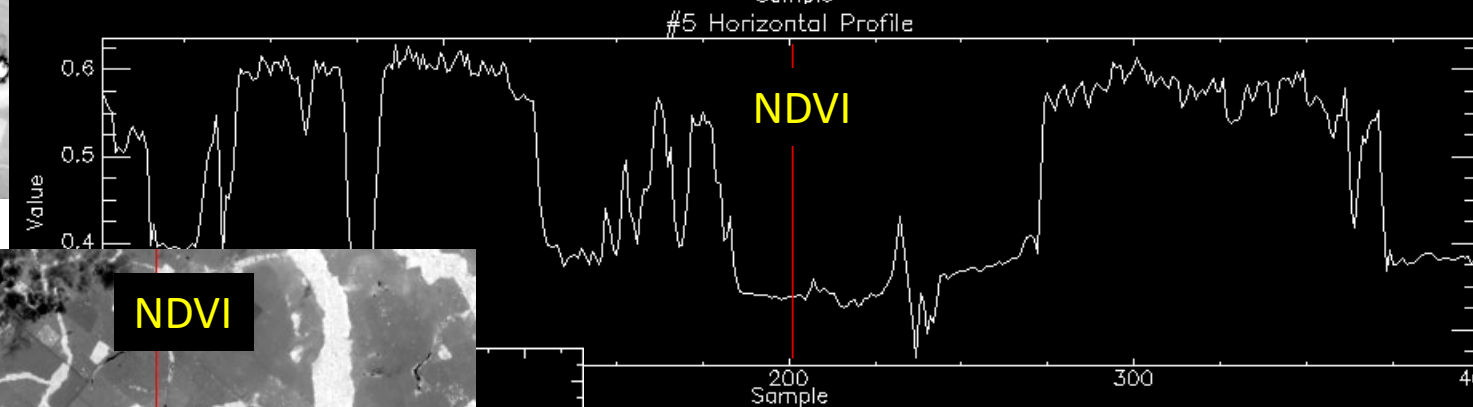
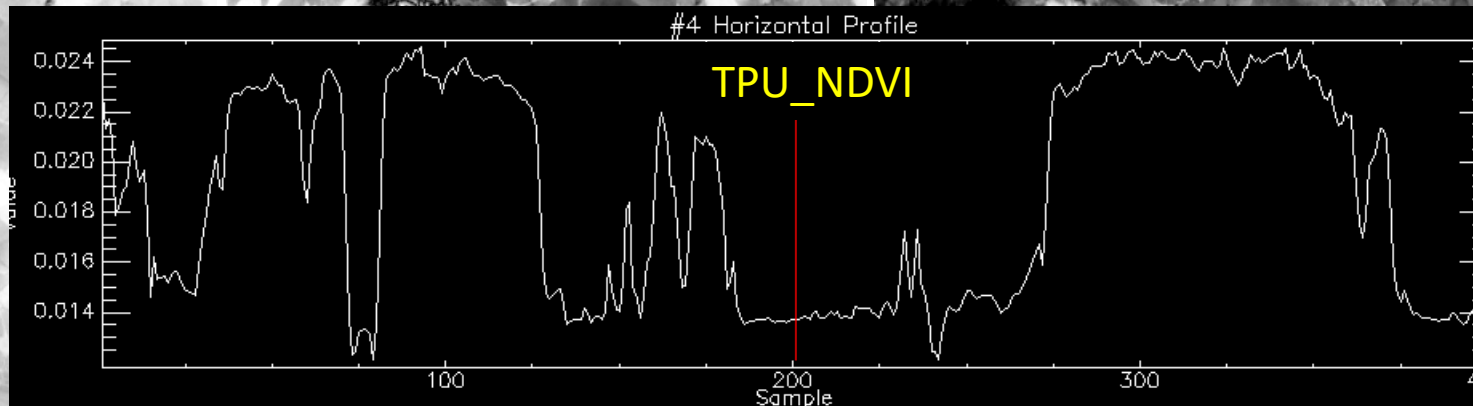
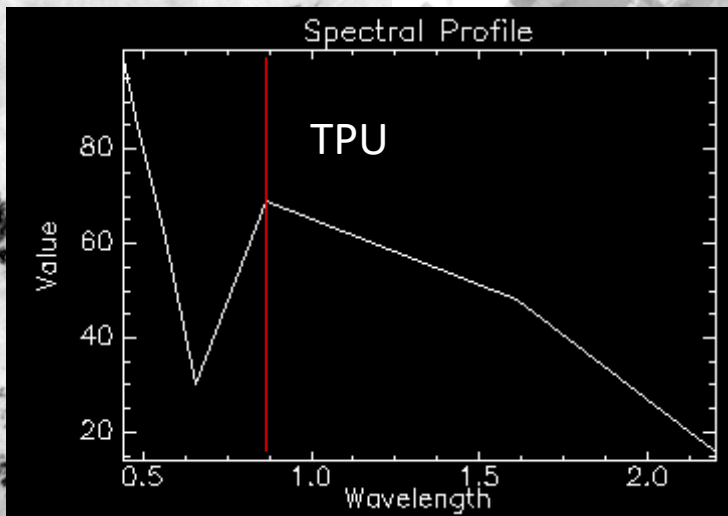
AOT sensitivity on Surface Reflectance





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