



Workshop Agenda (All times in MDT)

- ▶ 0730-0840 Sphere Theory and Applications (Durell)
- ▶ 0840-0910 Uniform Source Tutorial (Durell)
- ▶ 0910-0920 Sphere Calibrations (Durell)
- ▶ 0920-0930 (Virtual) Coffee Break
- ▶ 0930-1010 Considerations for Uniform Source Specifications (Scharpf)
- ▶ 1010-1020 Commercial considerations (Scharpf)
- ▶ 1020-1040 NASA GLAMR Case Study (Brendan McAndrew, NASA GSFC)
- ▶ 1040-1050 If time permits: Uniform Source Case Studies (Durell)

Integrating Sphere Theory

CALCON Workshop 2020

Sphere Technology

▶ DIFFUSE REFLECTANCE COATINGS AND MATERIALS

- ▶ Geometry & Spectrum
- ▶ Applications

▶ INTEGRATING SPHERES

- ▶ Theory
- ▶ Design
- ▶ Applications

Diffuse Reflecting Materials & Coatings

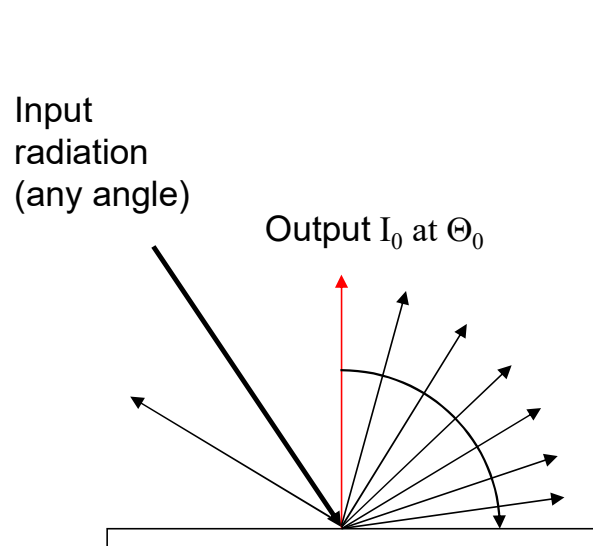
GEOMETRY

Ideal is perfectly Lambertian (diffuse)

SPECTRUM

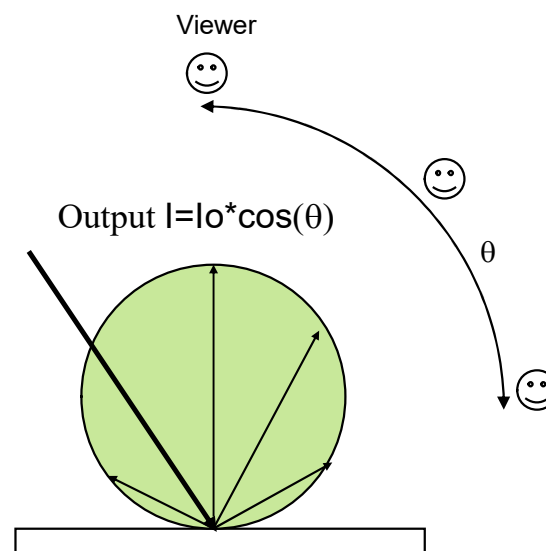
Ideal is perfectly reflecting (100%)

Geometry - Lambertian Reflector



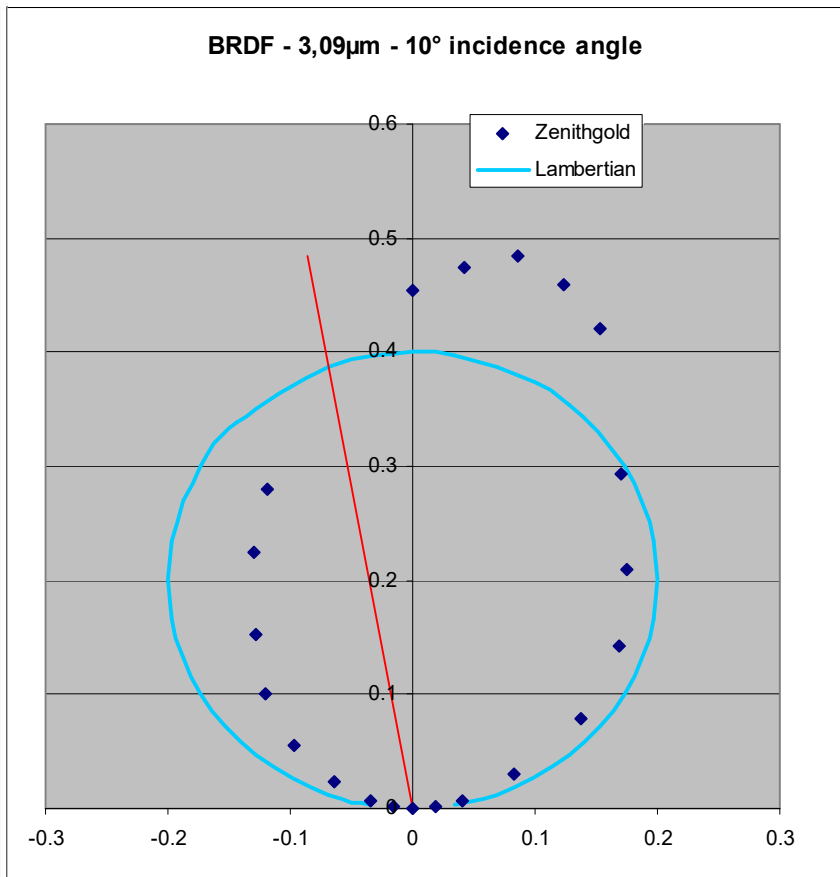
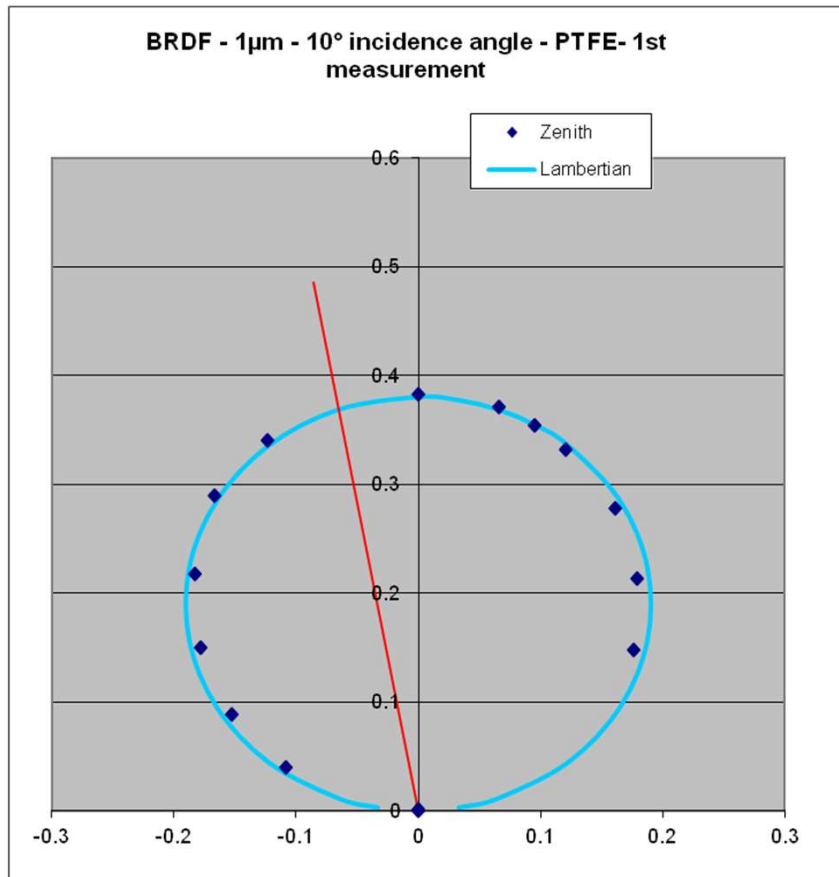
Equal Energy scattered at all angles over π steradians with 100% Reflectance

OR



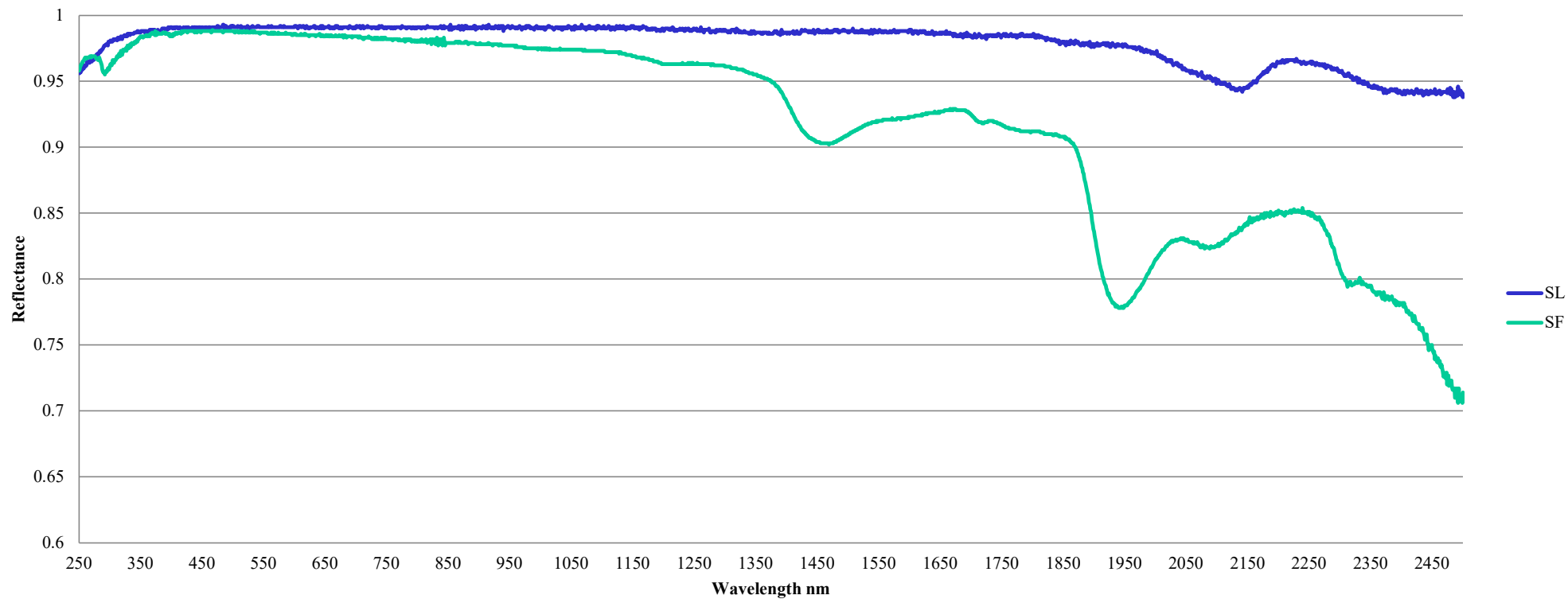
To an observer, I_0 seems to vary as to cosine of the angle θ . Intensity is a function of the area of the target presented to the angle of the viewer.

Real “Lambertian” Materials – Spectralon & Infragold

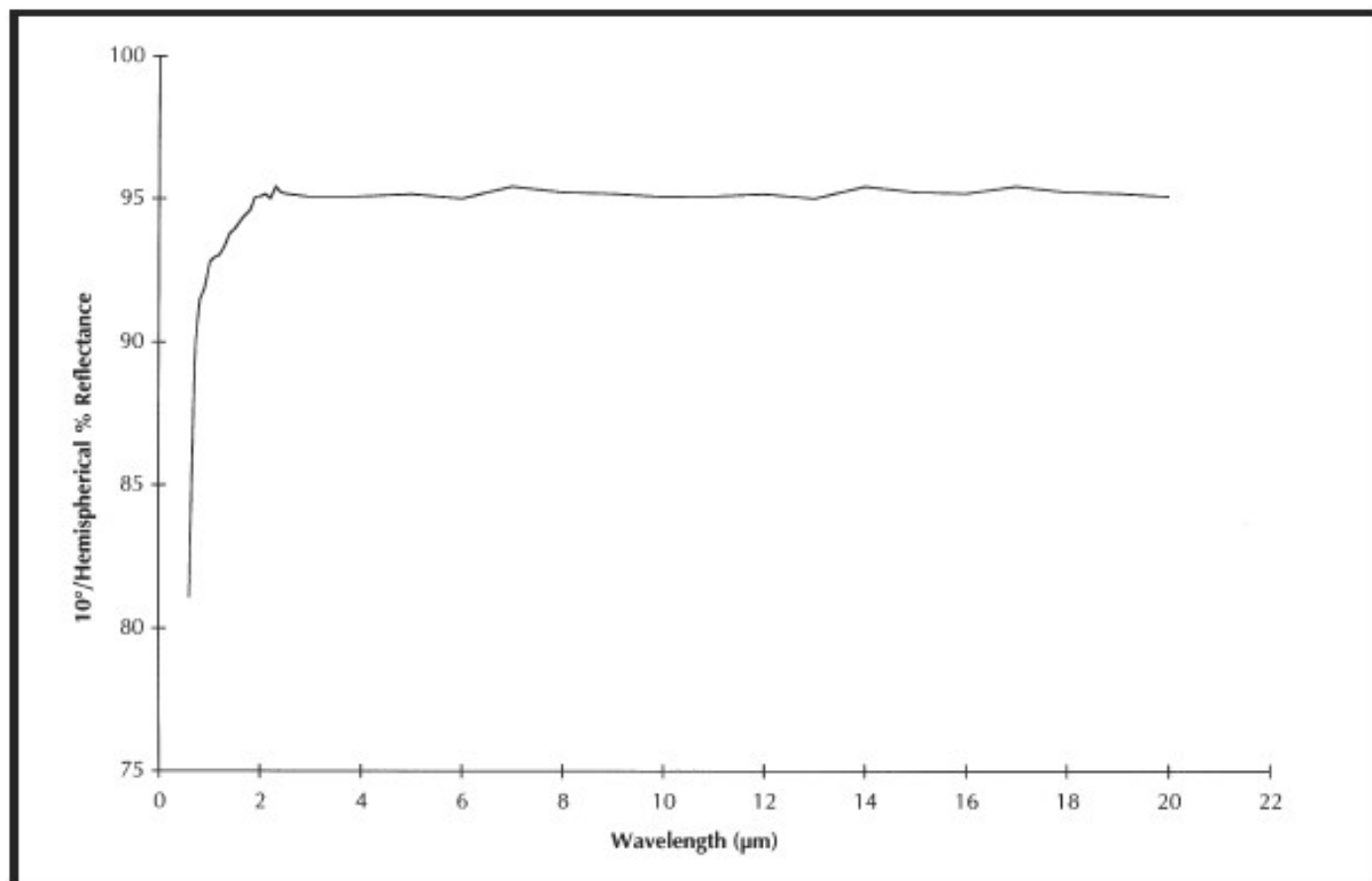


Real “White” Reflectance Materials

Typical reflectance data: Spectralon (PTFE) & Spectrafect (BaSO4)

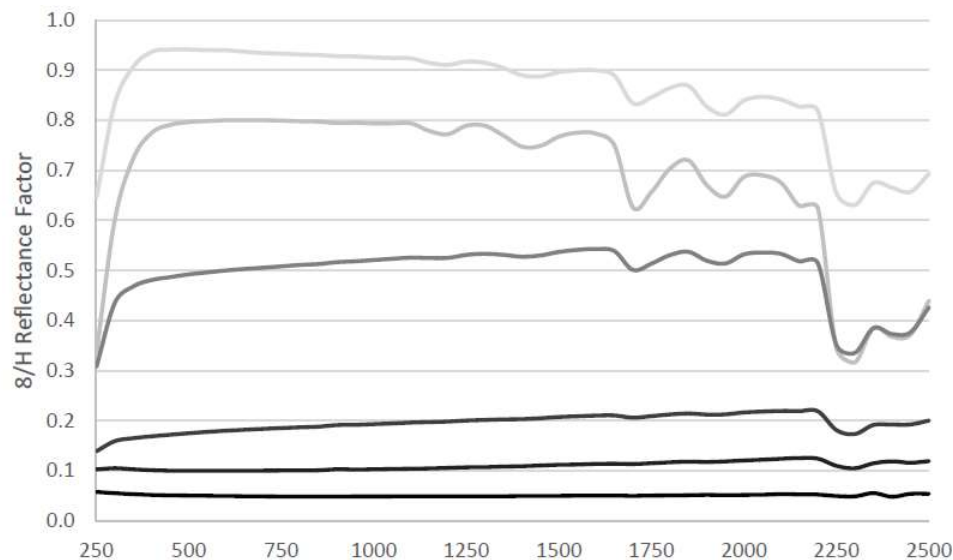


InfraGold for >650nm (IR Applications)

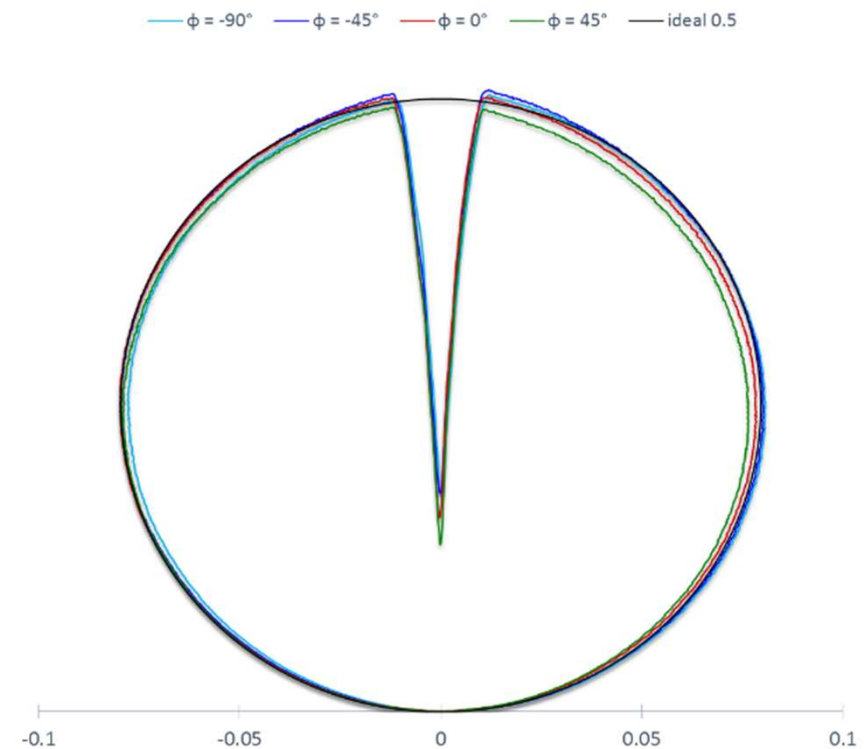


Permaflect - Lightweight Targets

- ▶ Washable & Weather Proof
- ▶ Reflectance from 5%-95%
- ▶ Various Substrates & Mountings
- ▶ Available Travel Cases
- ▶ Mosaics/Patterns



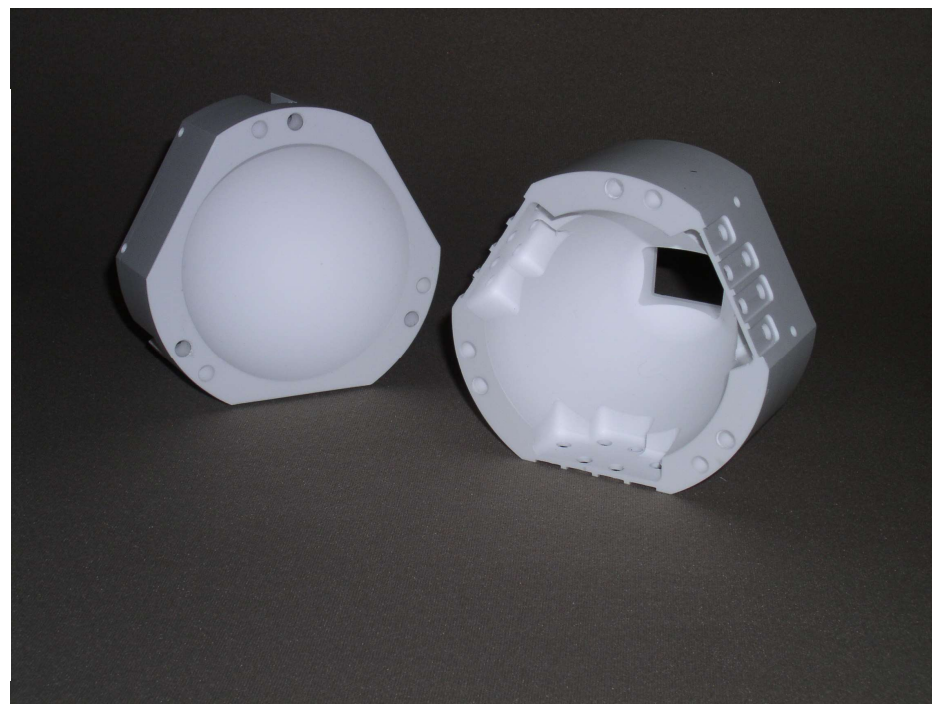
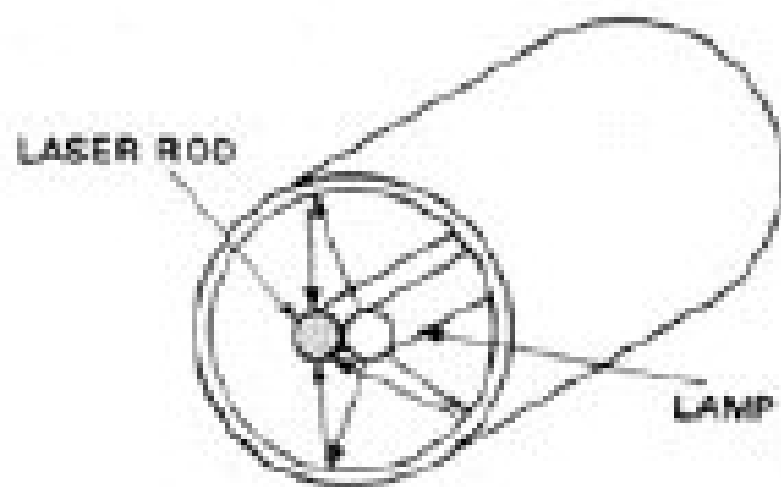
50% Reflectance Flexispect on Primed Latex
Polar BRDF with Θ Lighting = 0°



Reflectance Material & Coating Applications

- Integrating Spheres
- Reflectance Standards
- Lambertian Targets
- Backlighting
- Laser Chambers

Laser Pump & LED Chambers



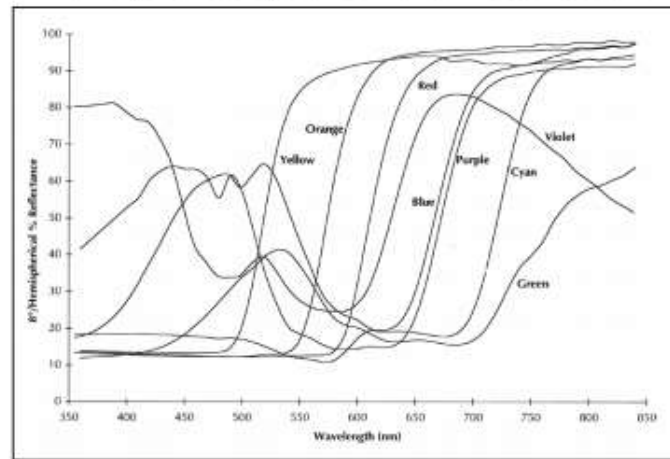
Lambertian Targets – Spectralon and Permaflect



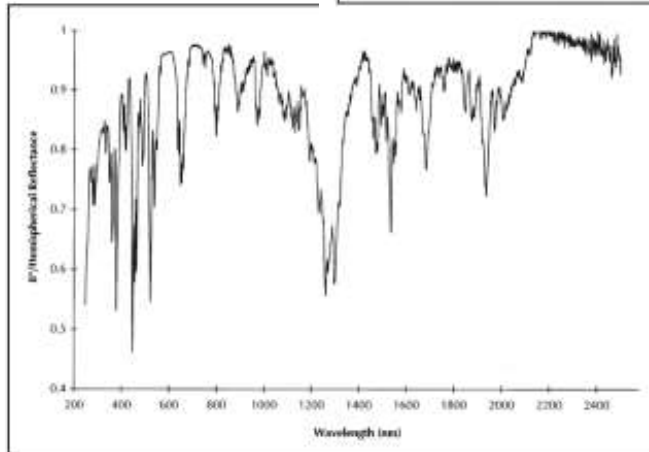
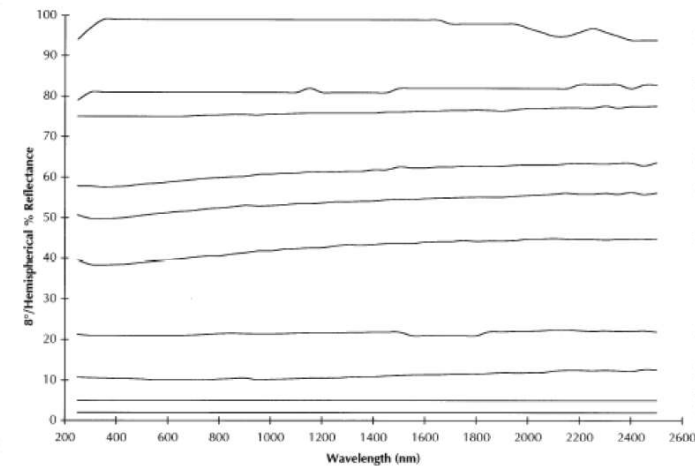
Spectralon Standards – Color, Grey & Wavelength



Hemispherical Spectral Reflectance Factors



Hemispherical Spectral Reflectance Factors for Spectralon Standards

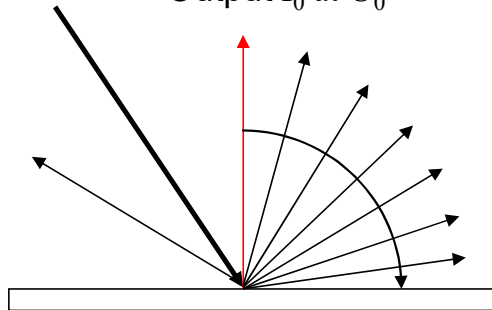


Practical Integrating Sphere Theory

Lambertian Reflector & Spherical Shape

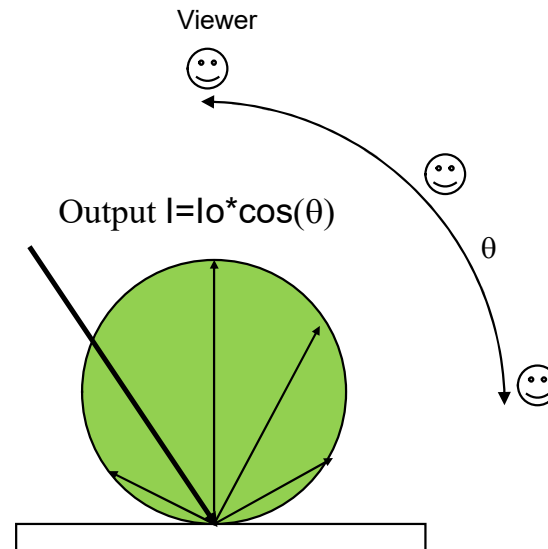
Input
radiation
(any angle)

Output I_0 at Θ_0



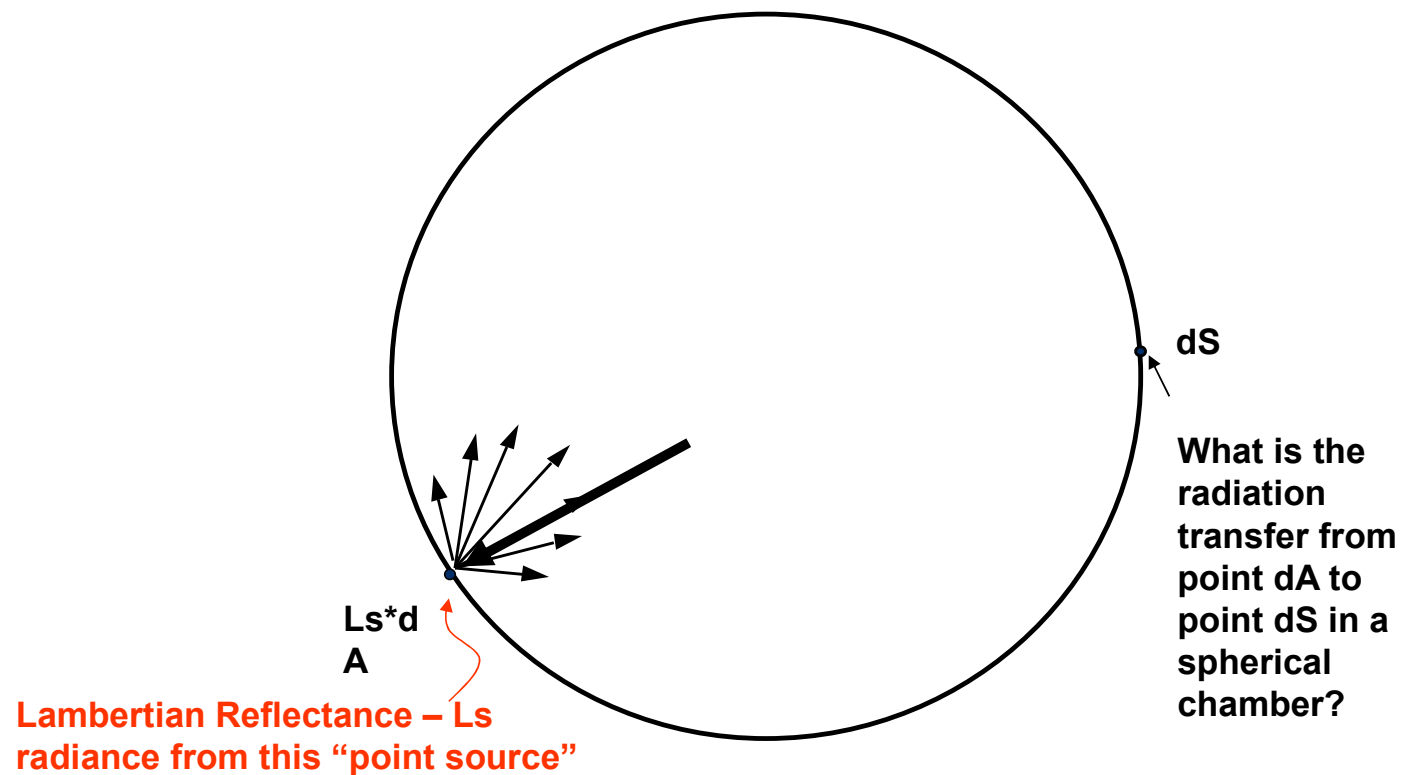
Equal Energy scattered at
all angles over π
steradians with 100%
Reflectance

OR

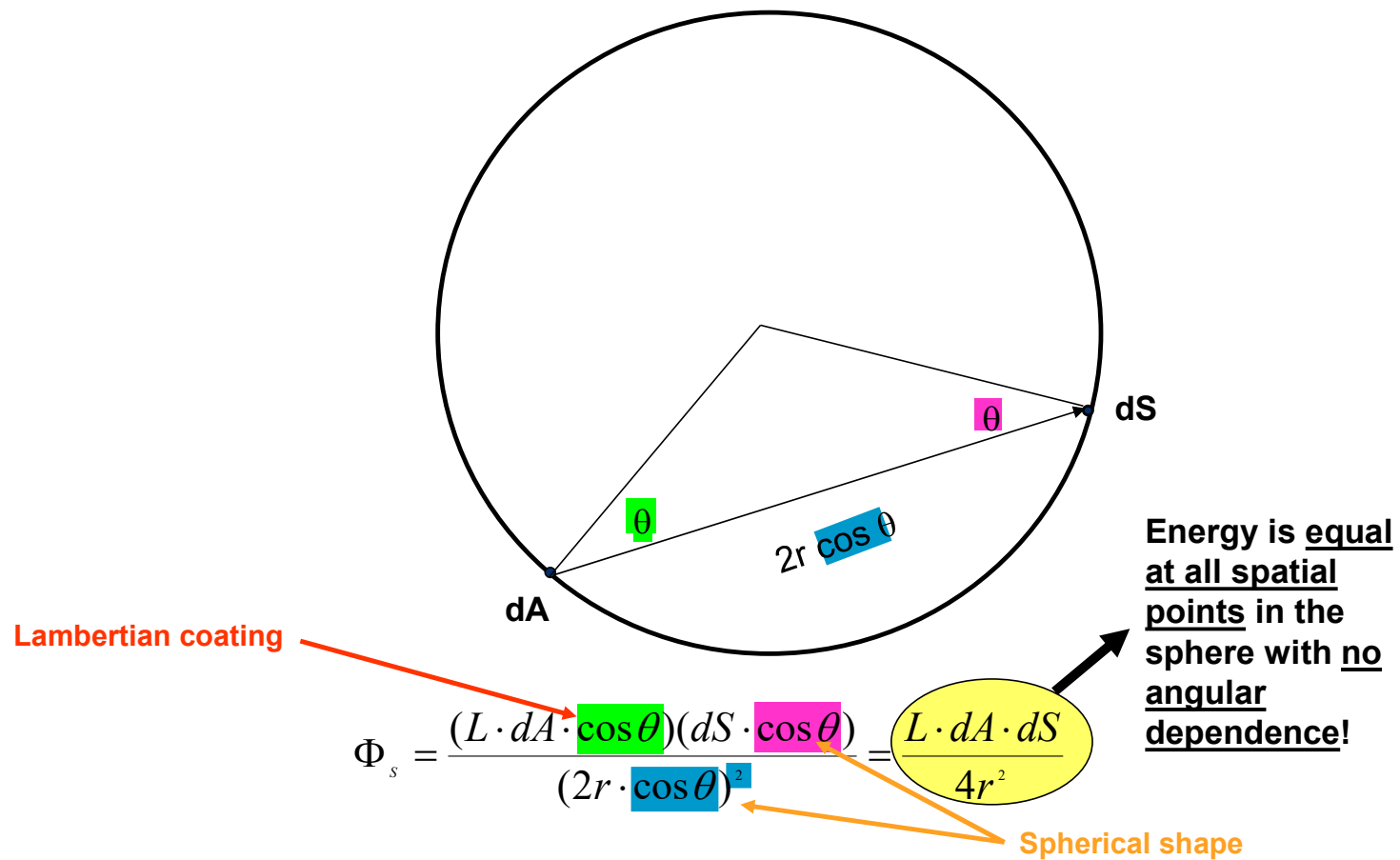


To an observer, I_0 seems to vary as to
cosine of the angle θ . Intensity is a
function of the area of the target
presented to the angle of the viewer.

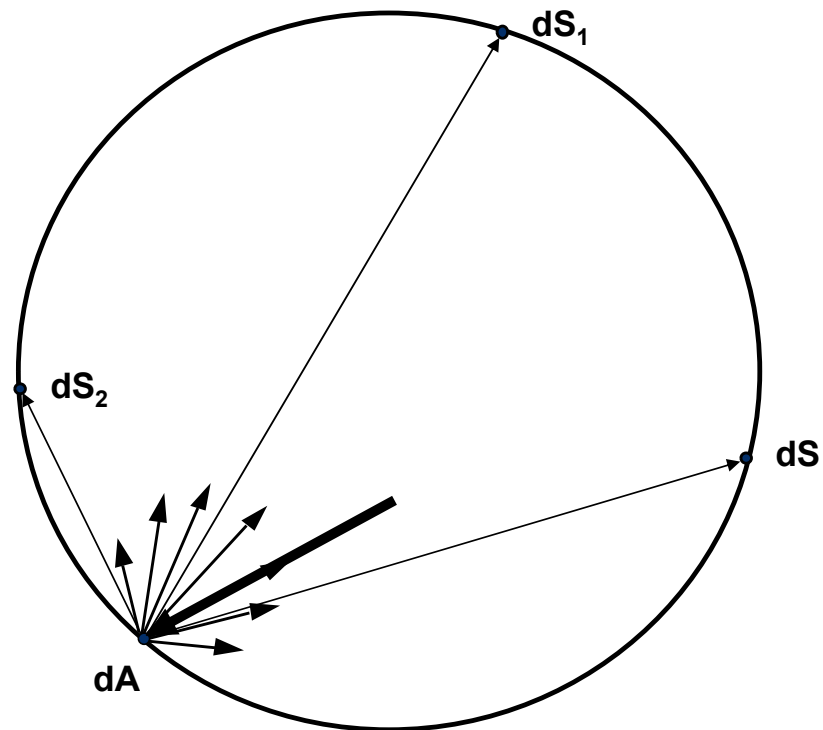
Put a Lambertian Reflector in a Spherical Shape...



Sphere + Lambertian



Sphere – Equal Energy at ALL points.



The Sphere Multiplier

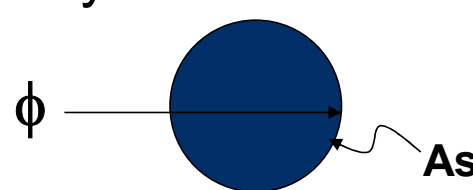
- ▶ There are multiple bounces in the sphere and there are ports in the sphere
 - ▶ The summation of multiple bounces reduces to a Taylor Series
- ▶ The Sphere Multiplier (M) is the resulting summation of the multiple reflections and losses for ports.

$$M = \frac{\rho_0}{1 - \rho_0(1 - f)}$$

- ▶ “ ρ_0 ” is the first reflection in the sphere or the actual reflectivity of the sphere wall.
 - ▶ “ f ” is the fractional area of the sphere of all ports and non-reflective surfaces (lost photons)
- ▶ The M factor is usually around 10-25 for most normal spheres and is driven most directly ρ_0 and the number of ports (port fraction= f). It also implies the average # of reflections in the sphere.
- ▶ M is also a “Sensitivity Factor” to sphere degradation.

Energy Density at the Sphere Wall

- ▶ Energy at any point on the sphere wall after the first reflection is given by:



The diagram shows a dark blue sphere. A horizontal arrow labeled ϕ points from the left towards the sphere's surface. A curved arrow labeled A_s points to the surface of the sphere where the arrow ϕ is hitting.

$$\frac{\phi_i}{A_s} \text{ (W/m}^2\text{)}$$

- ▶ But now, we have *multiple bounces* which leads to some “average” increase so we apply the “Sphere Multiplier”:

$$\frac{\phi_i}{A_s} * M = \frac{\phi_i}{A_s} * \frac{\rho_0}{1 - \rho_0(1 - f)} \text{ (W/m}^2\text{)}$$

- ▶ This is **Average Energy Density at the Sphere Wall**.

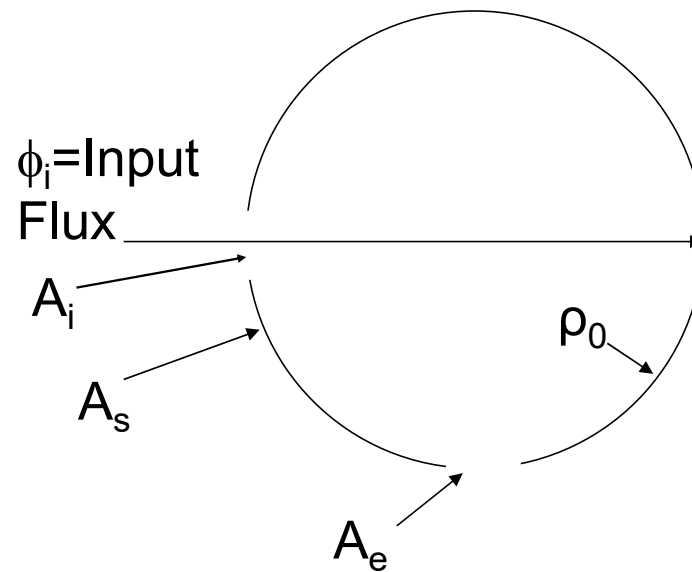
Radiance of the Sphere Wall

- ▶ Since we know the energy density (W/m²) at the sphere wall, the radiance of any point of the sphere wall can also be determined by dividing by π steradians:
- ▶ The **Sphere Radiance Equation** is therefore: $\frac{\phi_i}{\pi A_s}$ (W/m²-sr)

$$\text{Sphere Radiance (L)} = \frac{\phi_i}{\pi A_s} * \frac{\rho_0}{1 - \rho_0(1 - f)}$$

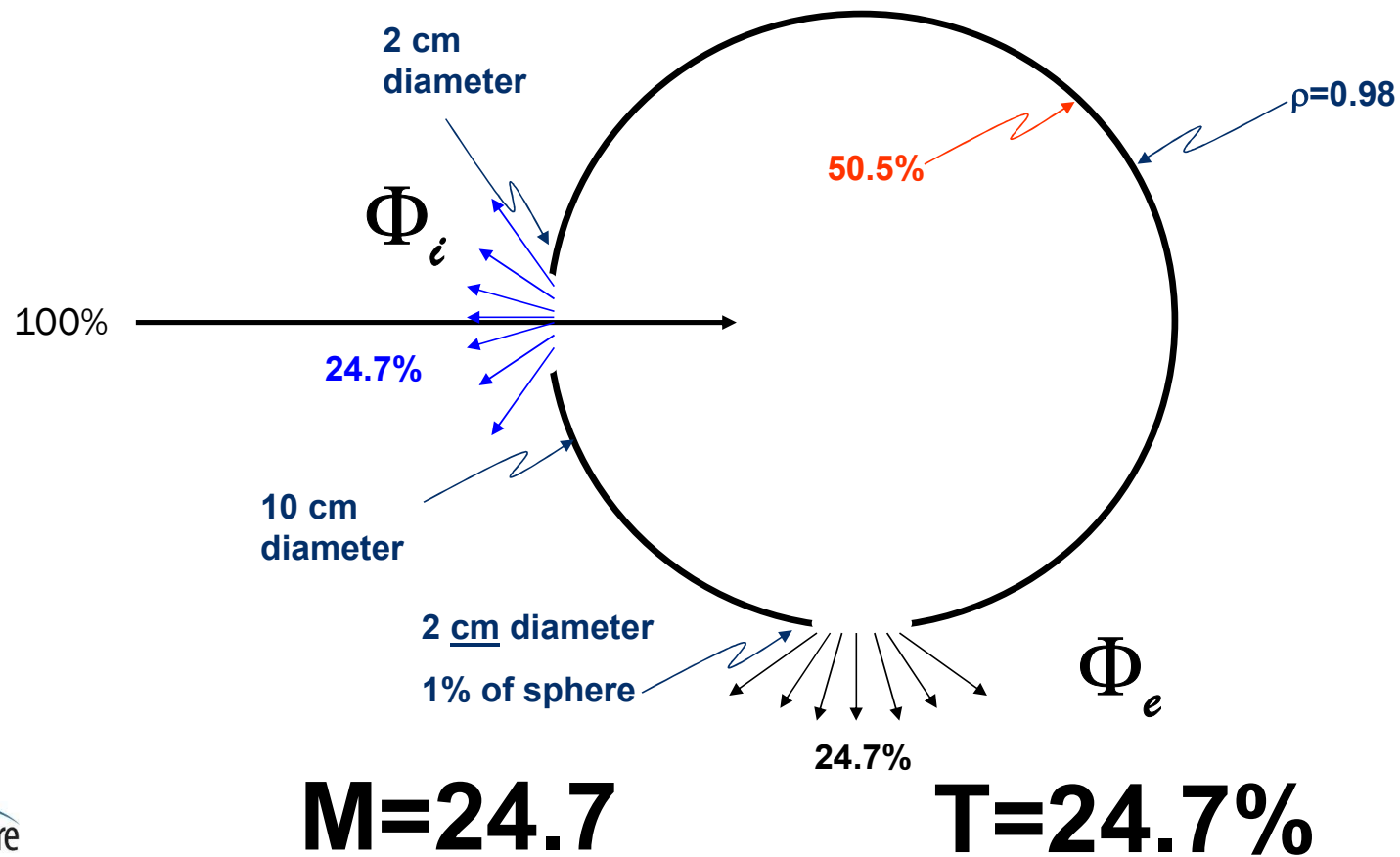
Throughput – Energy at a Port

- ▶ Energy at a port means we assume pi-steradian solid angle (drops pi from Sphere Radiance).
- ▶ Efficiency Calculation: 10cm sphere (98%) w/(2) 2cm ports
 - ▶ f is the fractional area of all ports in the sphere
- ▶ ~Equals 24.7% at the exit port.



$$Flux = \phi_i * \left(\frac{A_e}{A_s} \right) * \frac{\rho_0}{1 - \rho_0(1 - f)}$$

So...where does the energy go?



Throughput for a Detector

- ▶ Sphere Wall Radiance, $L = \frac{\phi_i}{\pi A_s} * \frac{\rho_0}{1 - \rho_0(1 - f)}$

- ▶ Throughput for Detector:

$$T_{Detector} = \phi_i * \frac{1}{\pi A_s} * \frac{\rho_0}{1 - \bar{\rho}} * A_d * \Omega$$

- ▶ $L * \text{Detector Area } (A_d) * \text{Solid Angle } (\Omega)$
- ▶ Example: 0.5cm detector – 10cm Sphere
 - ▶ -15-20dB (NA 1.0)

Throughput for a Fiber Optic

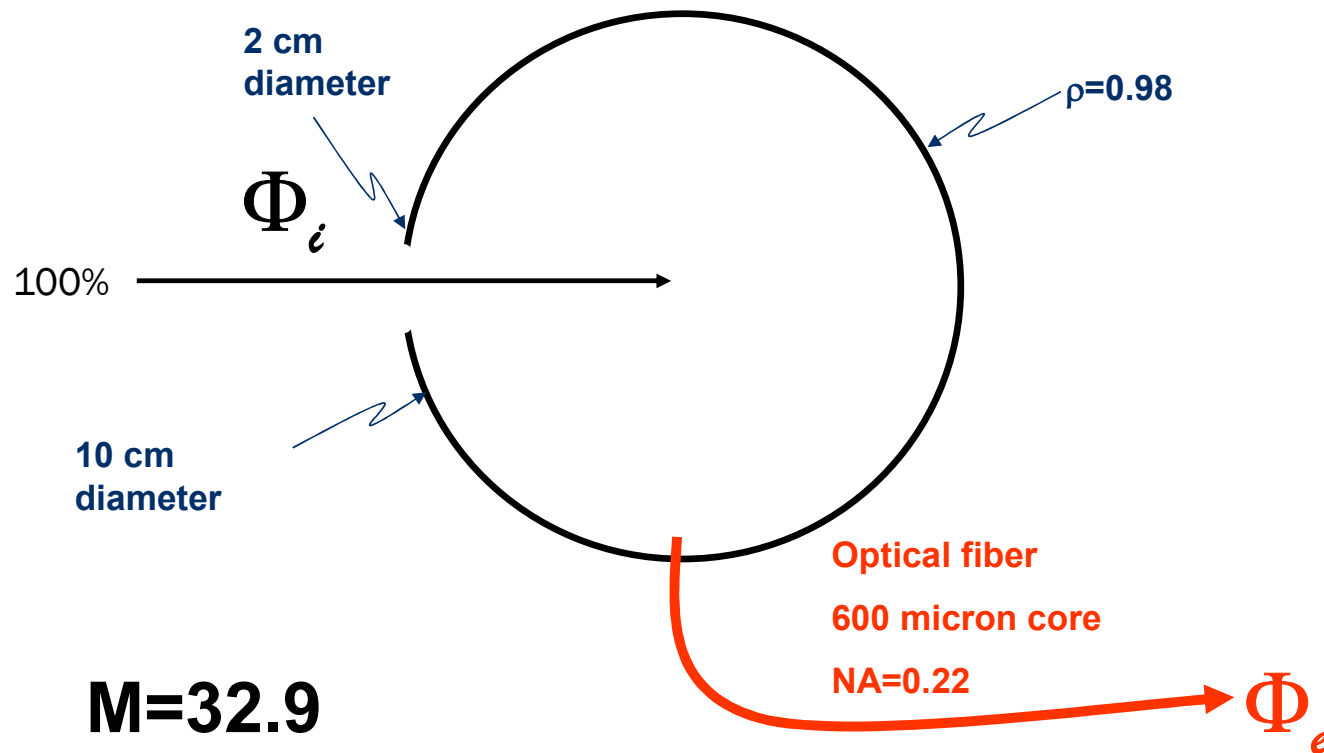
- ▶ Sphere Wall Radiance, $L = \frac{\phi_i}{\pi A_s} * \frac{\rho_0}{1 - \rho_0(1 - f)}$

- ▶ Throughput for Fiber:

$$T_{Detector} = \phi_i * \frac{1}{\pi A_s} * \frac{\rho_0}{1 - \bar{\rho}} * A_f * \Omega * (1 - r)$$

- ▶ $L * \text{Fiber Core Area (A}_d) * \text{Numerical Aperture (Field of View, } (\Omega)) * (1 - \text{Reflectance of Fiber Face (r))}$
- ▶ Example: Telecom Fiber (10cm Sphere, 98%):
 - ▶ 9um Fiber/NA 0.2 = (>-95dB!)

Throughput to a typical fiber-fed spectrometer



$$M=32.9$$

$$T=1.4 \times 10^{-5} = 0.0014\% = -48.5\text{dB}$$

Throughputs for a 10cm, 98% Reflectance Sphere.

dB to Detector									
		NA	0.018	0.126	0.178	0.399	0.691	1.000	
		Solid Ang.	0.001	0.05	0.1	0.5	1.5	3.142	
mm	Det. Active Area		sr	sr	sr	sr	sr	sr	
1	0.01 cm2		-67.73	-50.74	-47.73	-40.74	-35.97	-32.76	dB
2	0.04 cm2		-61.71	-44.72	-41.71	-34.72	-29.95	-26.74	dB
5	0.25 cm2		-53.75	-36.76	-33.75	-26.76	-21.99	-18.78	dB
7.5	0.5625 cm2		-50.23	-33.24	-30.23	-23.24	-18.47	-15.26	dB
10	1 cm2		-47.73	-30.74	-27.73	-20.74	-15.97	-12.76	dB
25.4	2.25 cm2		-44.21	-27.22	-24.21	-17.22	-12.45	-9.24	dB
dB to Fiber									
		NA	0.12	0.2	0.3	0.4	0.6	1	
Refl Fiber	0.8 Sr		0.045	0.126	0.283	0.503	1.131	3.142	
um - diam	Fiber Area		sr	sr	sr	sr	sr	sr	
9	6.36E-07 cm2		-100.13	-95.69	-92.17	-89.67	-86.15	-81.71	dB
12	1.13E-06 cm2		-97.63	-93.19	-89.67	-87.17	-83.65	-79.22	dB
25	4.91E-06 cm2		-91.26	-86.82	-83.30	-80.80	-77.28	-72.84	dB
100	7.85E-05 cm2		-79.22	-74.78	-71.26	-68.76	-65.24	-60.80	dB
250	4.91E-04 cm2		-71.26	-66.82	-63.30	-60.80	-57.28	-52.84	dB
1000	7.85E-03 cm2		-59.22	-54.78	-51.26	-48.76	-45.24	-40.80	dB
5000	1.96E-01 cm2		-45.24	-40.80	-37.28	-34.78	-31.26	-26.82	dB

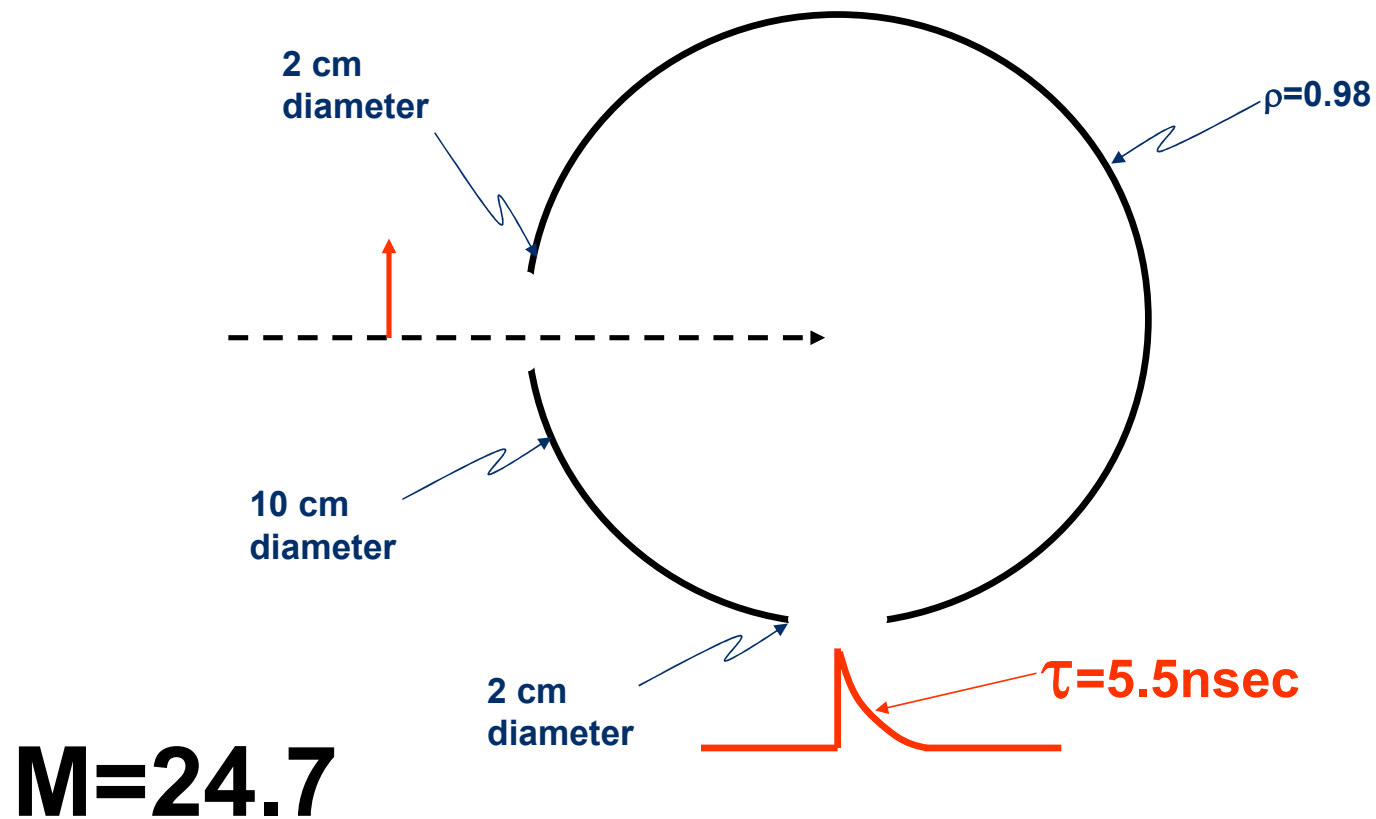
Sphere Time Constants

- ▶ Due to the multiple reflections in a sphere and the “random” path length of each photon, not all photons arrive at a designated point at the same time.
- ▶ A sphere acts very much like a “photon-capacitor” and has a time constant similar to that capacitor analogy.
- ▶ This Time Constant is driven by the D (diameter of the sphere), ρ_0 (the reflectance) and, c (the speed of light).

$$e^{-t/\tau} \text{ where } \tau = -\frac{2}{3} \cdot \frac{D}{c} \cdot \frac{1}{\ln \rho_0}$$

- ▶ Typical time constants are 2-10ns (100-500Mhz)

Sphere Time Constants – Impulse Input



Sphere Practical Advice

- ▶ Ratio of 1:3 largest port to Diameter of Sphere.
- ▶ 5% Port Area-to-Surface Area Ratio.
- ▶ Spheres do not remove speckle (coherence) – but you can play tricks!
- ▶ M factor is also a “sensitivity factor” to dust and changes to the sphere.
- ▶ Spheres are depolarizing.
- ▶ Baffle placement or use depends on the application.
- ▶ Throughput most directly follows D_1^2/D_2^2 Ratio (Surface Area).
- ▶ Spectrally homogenous field even with multispectral sources.

Optical Modeling Uniformity with Spheres

- ▶ **Computer (Monte Carlo) modeling of sphere performance is possible, but only really useful for special cases.**
- ▶ **REASONS:**
 - ▶ **BRDF of coating not fully known**
 - ▶ **Statistical fluctuations in the result are greater than parameter being investigated**
- ▶ **SPECIAL CASES:**
 - ▶ **Overly “filled” spheres with low performance requirements**
 - ▶ **Example – Irradiance uniformity on multiple samples positioned inside a sphere**
 - ▶ **Poor BRDF**
 - ▶ **Example – Rough surface at 100 and 200 microns**

Sphere Coating Advice (1 of 2)

BaSO₄ (350 - 1300nm)

- ▶ Cheapest coating
- ▶ “Likes” hydrocarbons & dust
- ▶ Hydroscopic & Water Soluble
- ▶ Damage threshold ~1.0W/cm²
- ▶ Vacuum compatible
- ▶ Thickness ~1.5mm
- ▶ Does Not like vibration or shock
- ▶ Heat limited to 80C
- ▶ Do not use with UV

PTFE (< 250 - 2500nm)

- ▶ Best throughput and function
- ▶ “Likes” hydrocarbons & dust
- ▶ Hydrophobic
- ▶ Damage Threshold ~8.0W/cm²
- ▶ Vacuum Compatible
- ▶ Requires thick walls (~7mm) – translucent
- ▶ OK Vibration & Shock
- ▶ OK to 300C
- ▶ OK for UV
- ▶ Thermal Expansion/Contraction – avoid thermal cycling

Sphere Coating Advice (2 of 2)

ZenithGold (0.8um to >26um)

- ▶ Best IR coating >2500nm
- ▶ Not that reflective (94-95%)
- ▶ Not that diffuse
 - ▶ Gets worse with longer wavelengths
- ▶ OK for pretty much all liquids
- ▶ Thermally stable to >500C
- ▶ Damage threshold ~20W/cm²
- ▶ Vacuum compatible
- ▶ Thickness ~0.010mm
- ▶ OK vibration & shock & thermal cycles

Historical Sphere Coatings

- ▶ MgO₂
- ▶ Packed PTFE

Other Coatings

- ▶ Deep UV – MgF₂/Al
 - ▶ <200-1000nm
- ▶ UV to IR – MgF₂/Ag
 - ▶ <0.2 to >3.0um

Integrating Sphere Applications

Uses of Integrating Spheres

Radiometers/Photometers

Reflectance/transmittance measurements

Uniform source

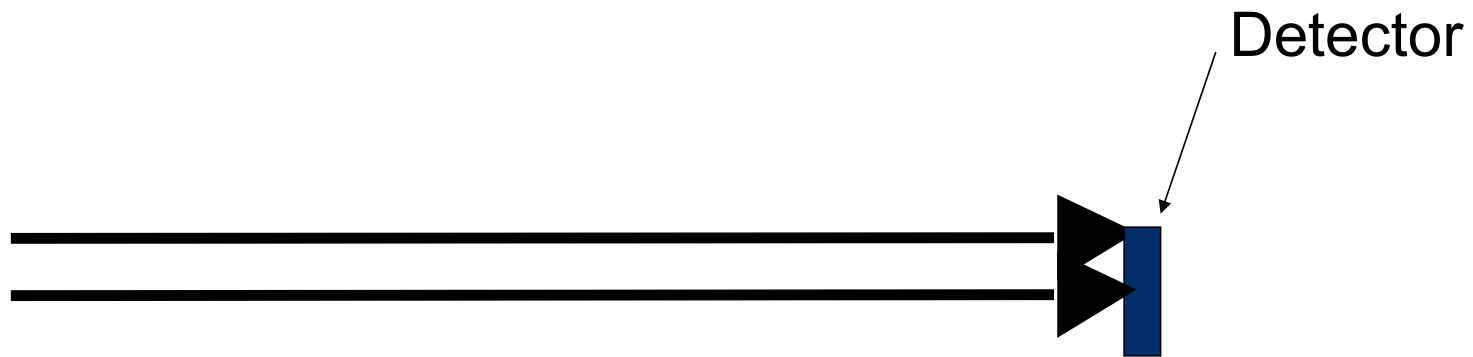
Sphere Used with a Radiometer/Photometer

The integrating sphere is used as a non-imaging optic to achieve the desired collection geometry

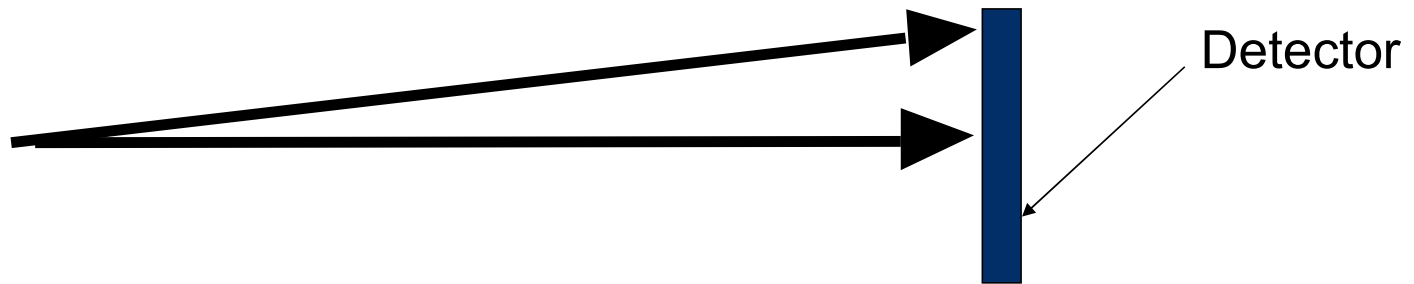
Advantage: geometry

**Disadvantage: signal level
(sometimes this is an advantage)**

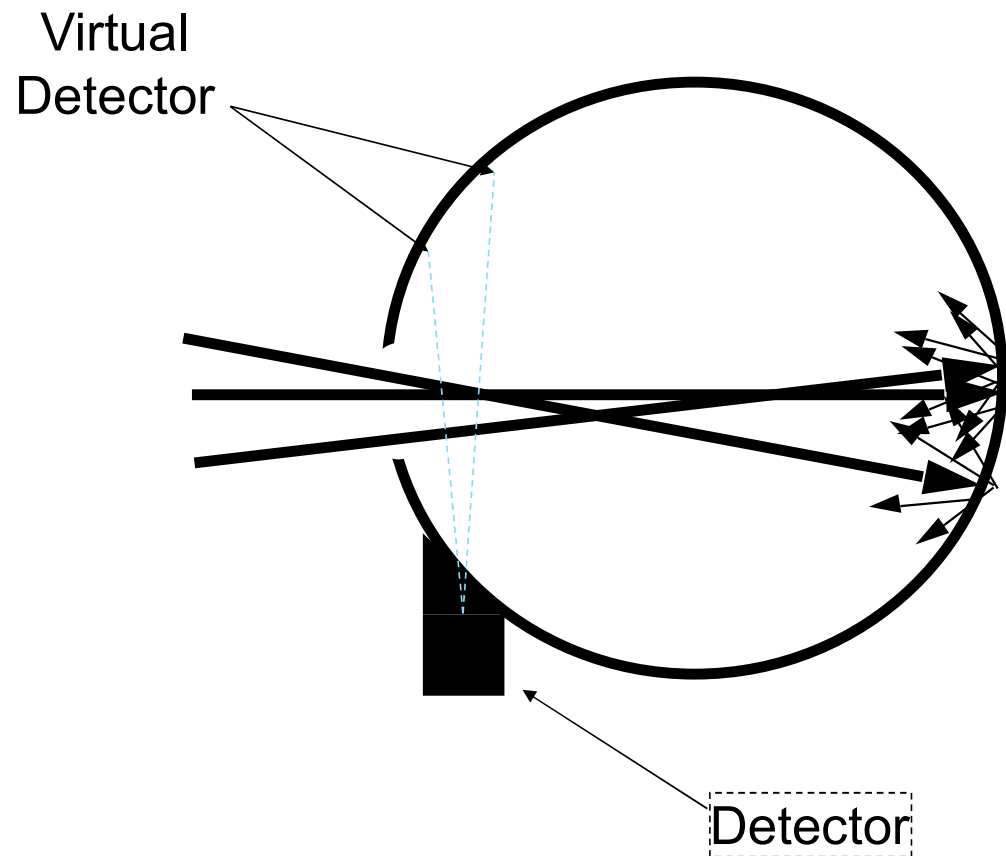
Classic Laser Power Meter – Detector - Spatial



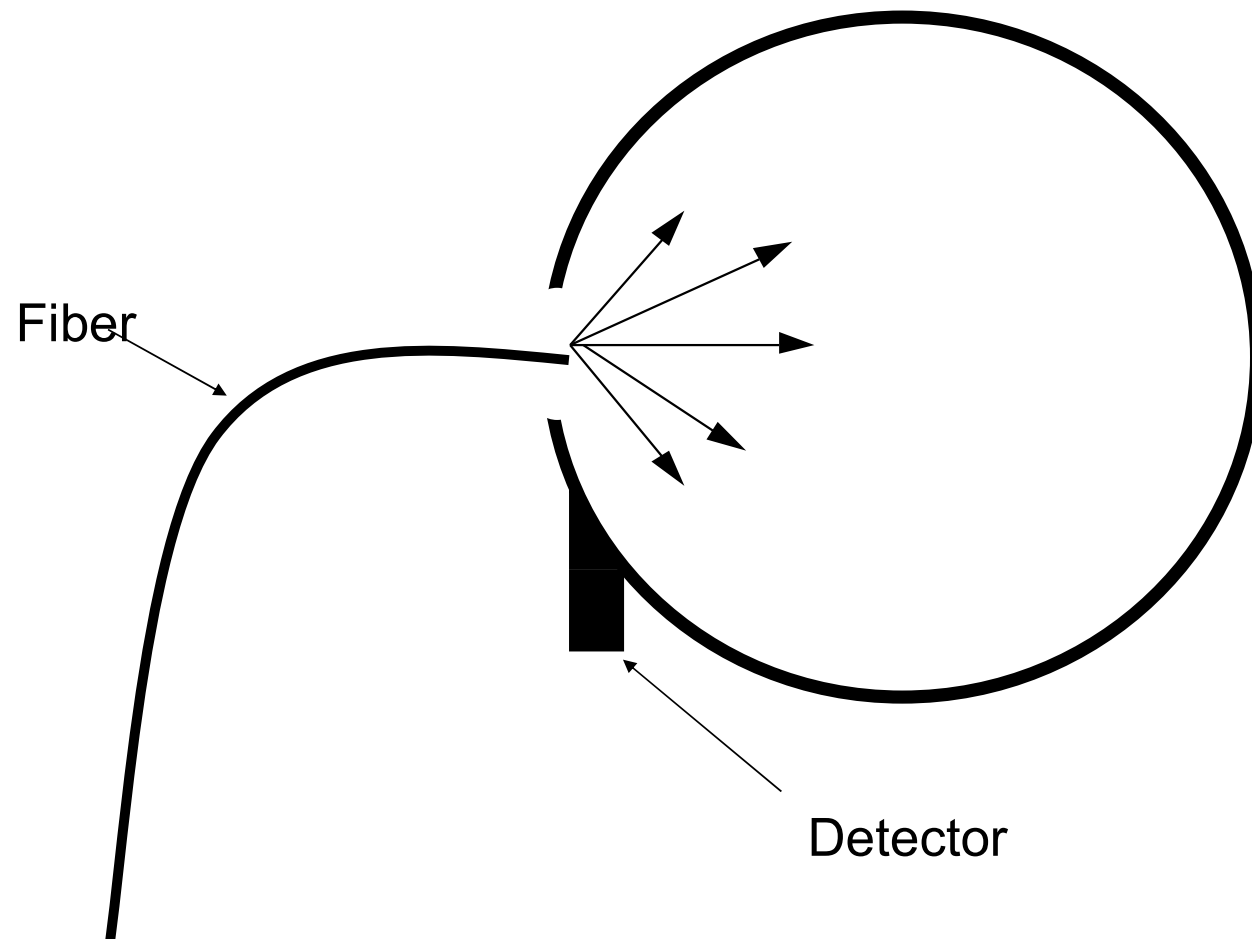
Classic Laser Power Meter – Detector - Geometric



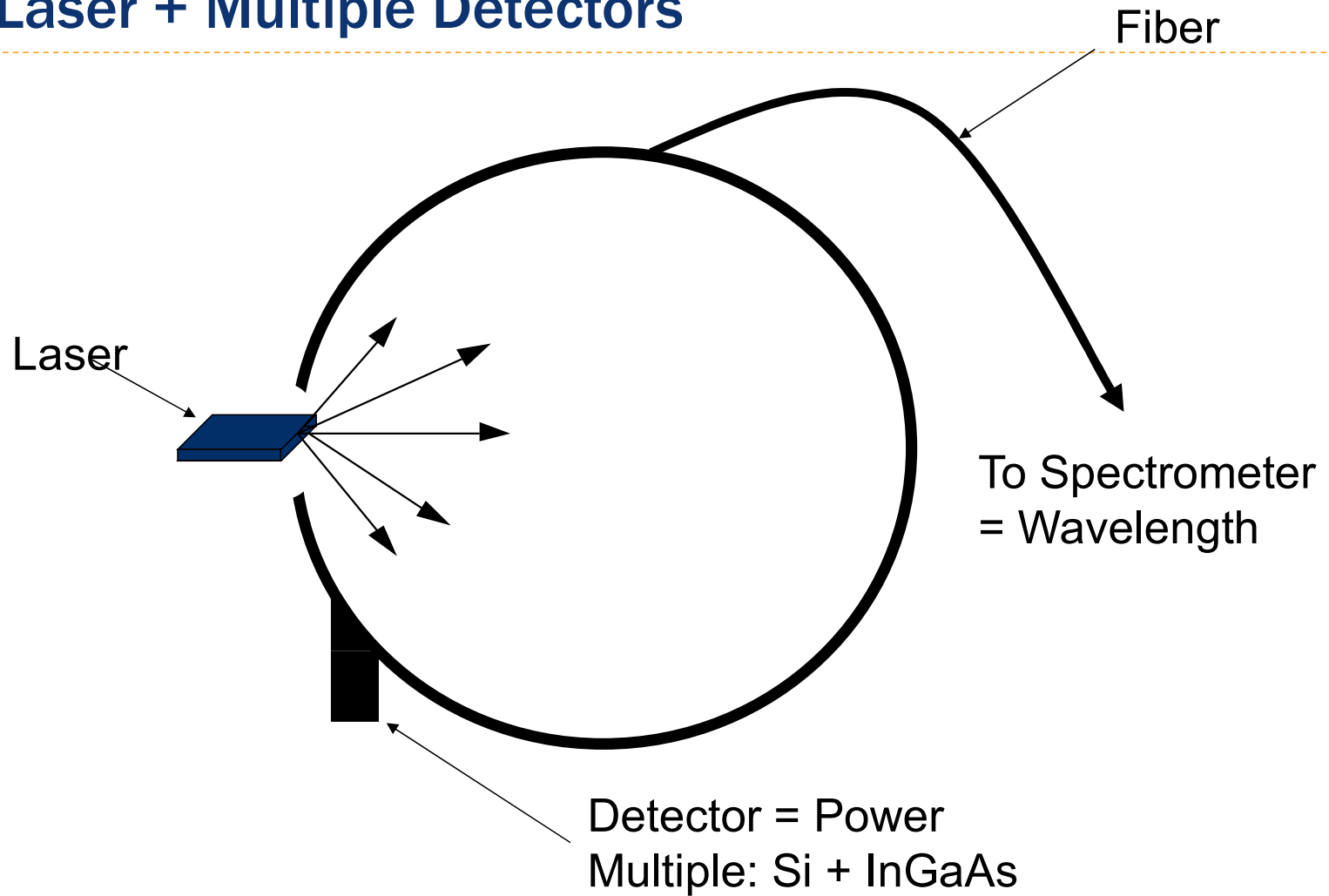
Laser Power Meter - Sphere



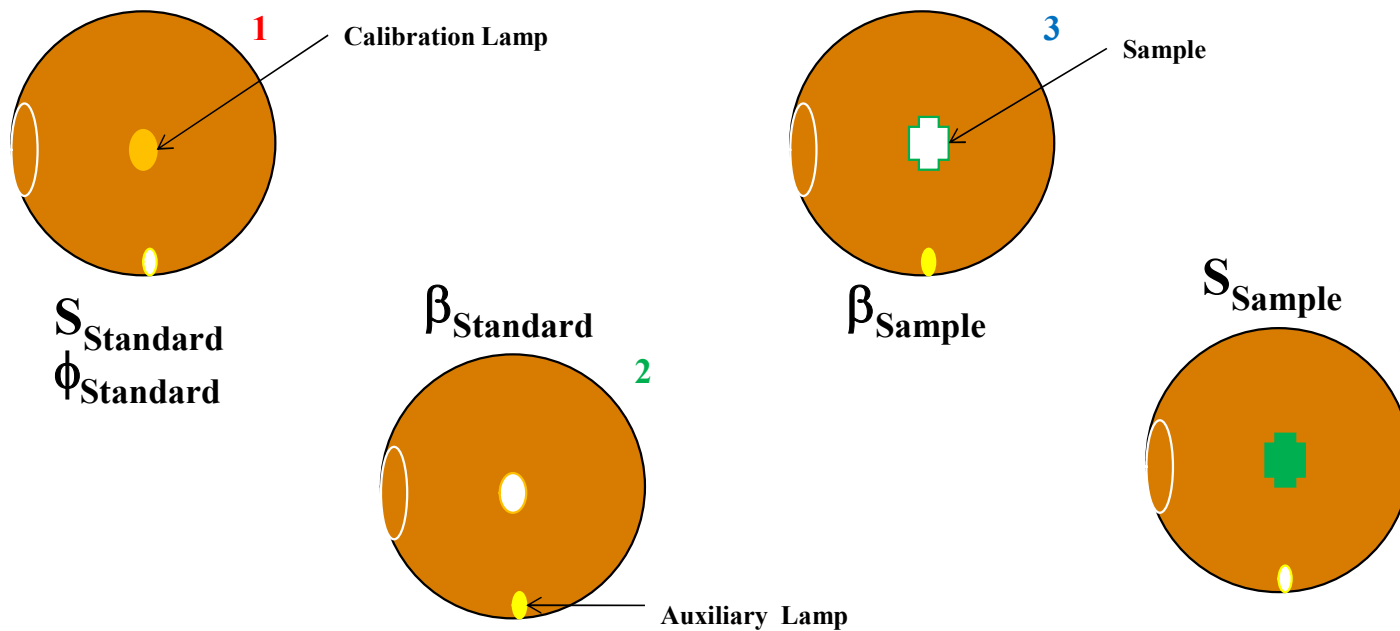
Fiber Input Laser



Diode Laser + Multiple Detectors

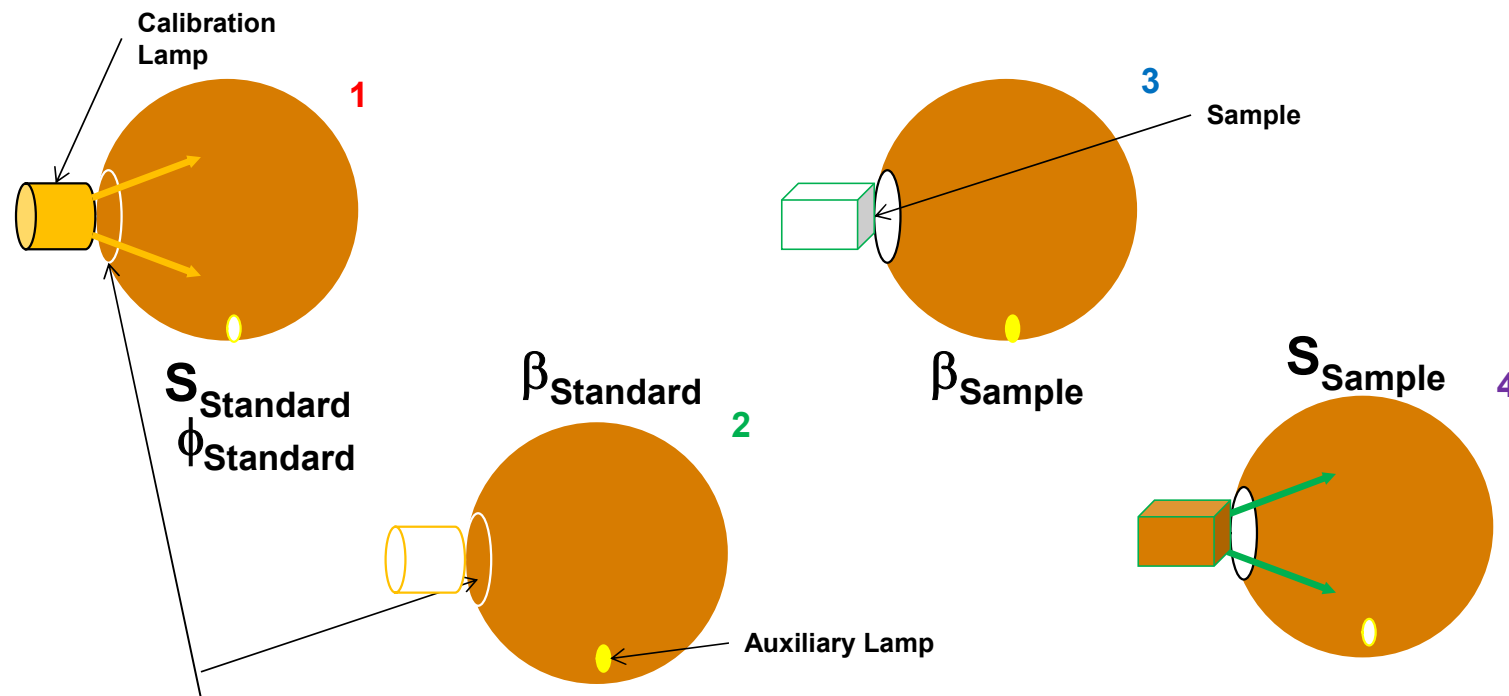


Lamp/Source Measurement - Internal



$$\phi_{\text{Sample}}(\lambda) = \frac{S_{\text{Sample}}^4(\lambda)}{S_{\text{Standard}}^1(\lambda)} * \frac{\beta_{\text{Standard}}^2(\lambda)}{\beta_{\text{Sample}}^3(\lambda)} * \phi_{\text{Standard}}^1(\lambda)$$

Lamp/Source Measurement - External

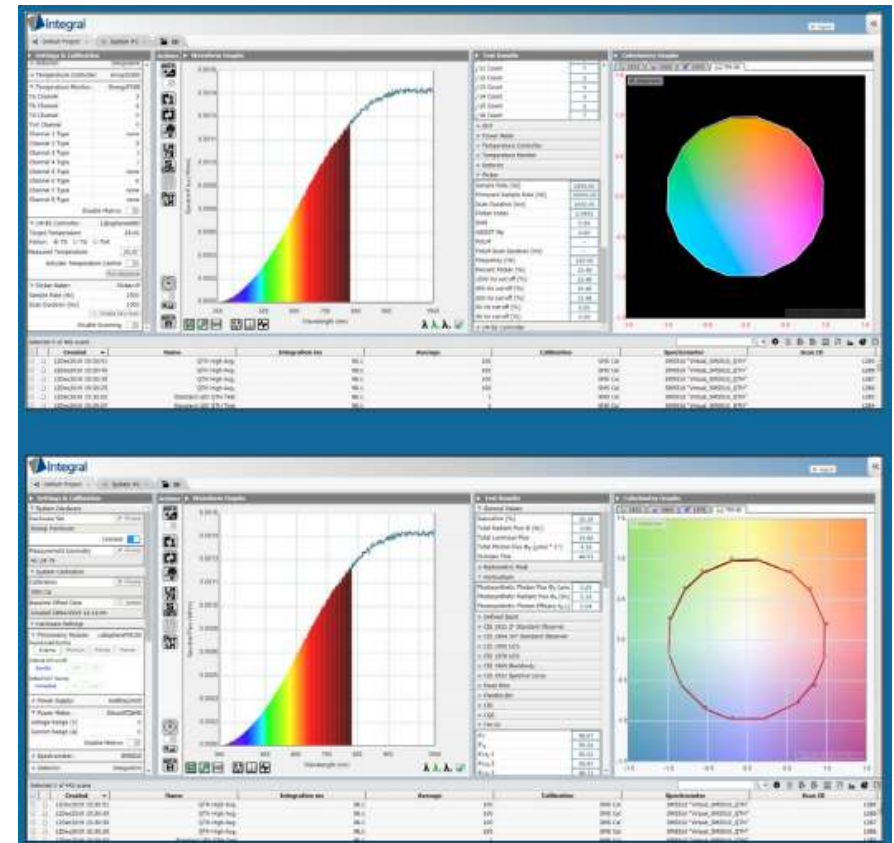


**Plug for
external
port**

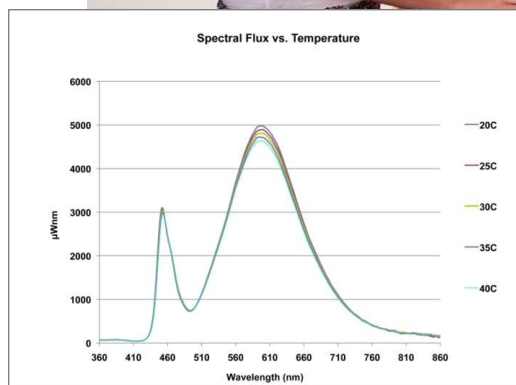
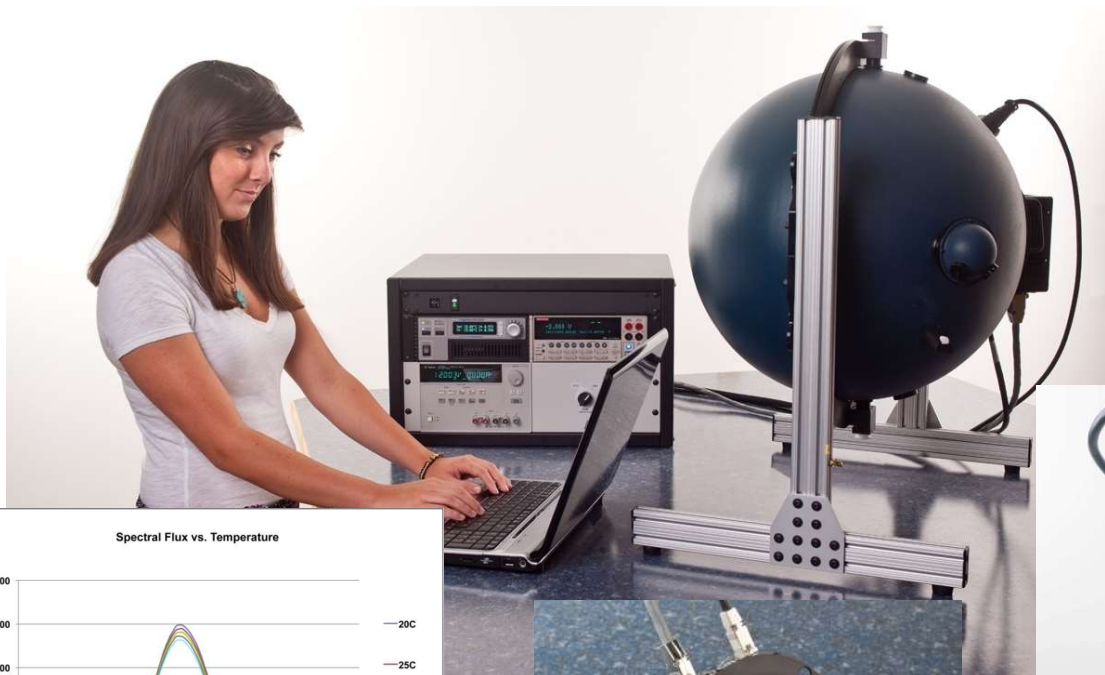
$$\phi_{\text{Sample}}(\lambda) = \frac{S_{\text{Sample}}^4(\lambda)}{S_{\text{Standard}}^1(\lambda)} * \frac{\beta_{\text{Standard}}^2(\lambda)}{\beta_{\text{Sample}}^3(\lambda)} * \phi_{\text{Standard}}^1(\lambda)$$

Spectral vs. Photometric Lamp Measurement

- Color temperature (correlated color temperature)
- Chromaticity
- Color rendering index
- Color Quality System Metrics (NIST)
- Dominant wavelength and purity (for LEDs)
- Optical Characterization with Thermal Control
- Electrical Performance



Lamp/Source – Optical, Electrical and Thermal Characterization



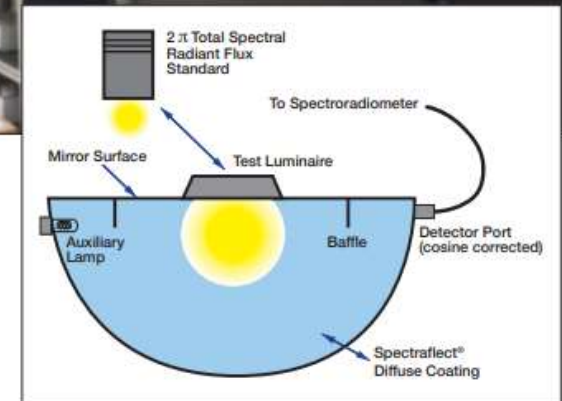
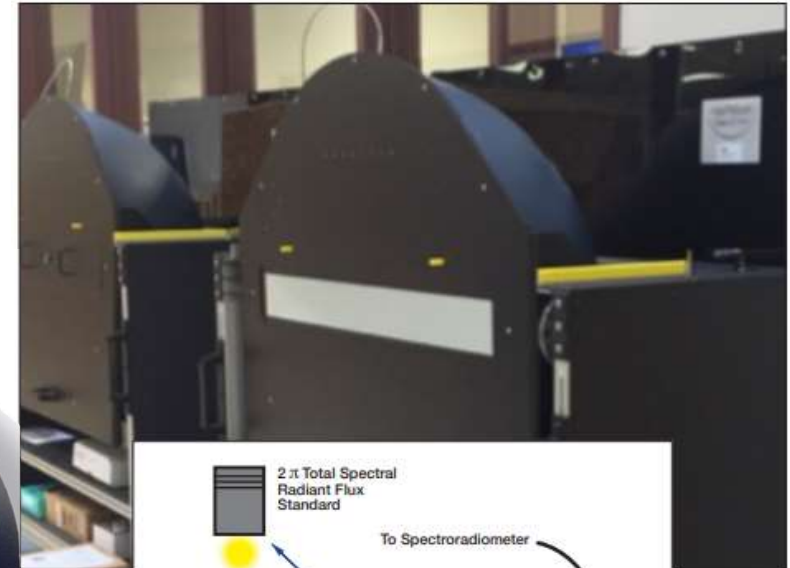
Complete Luminaire AC/DC & Thermal Characterization



LM-82
Ambient
Thermal
Sphere
Test



AC/DC Variable
Impedance System



Production Half-Moon "Sphere"

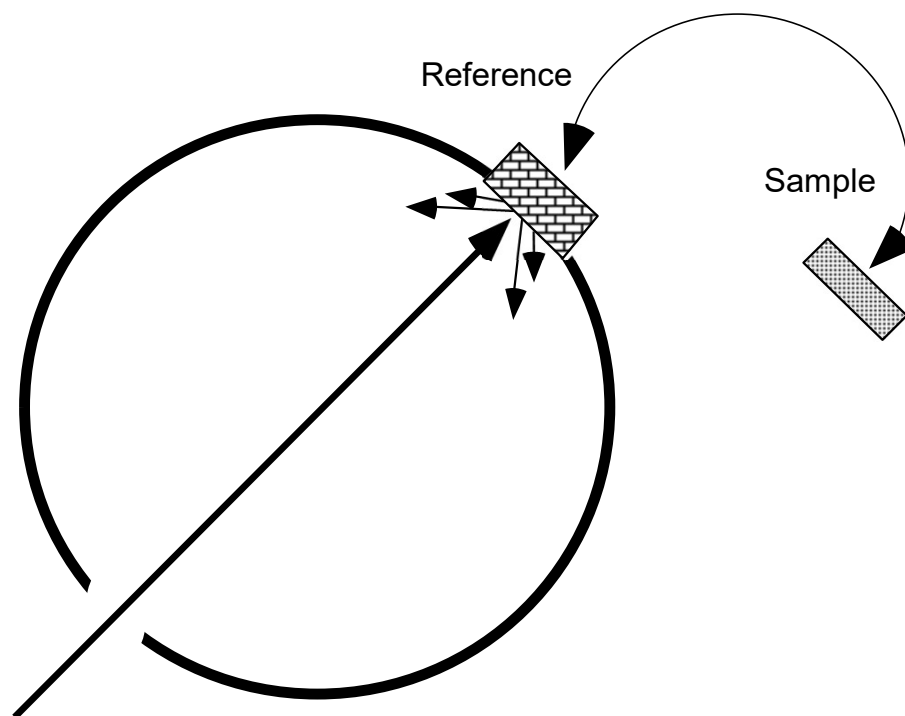
— Uses of Integrating Spheres —

Radiometers/photometers

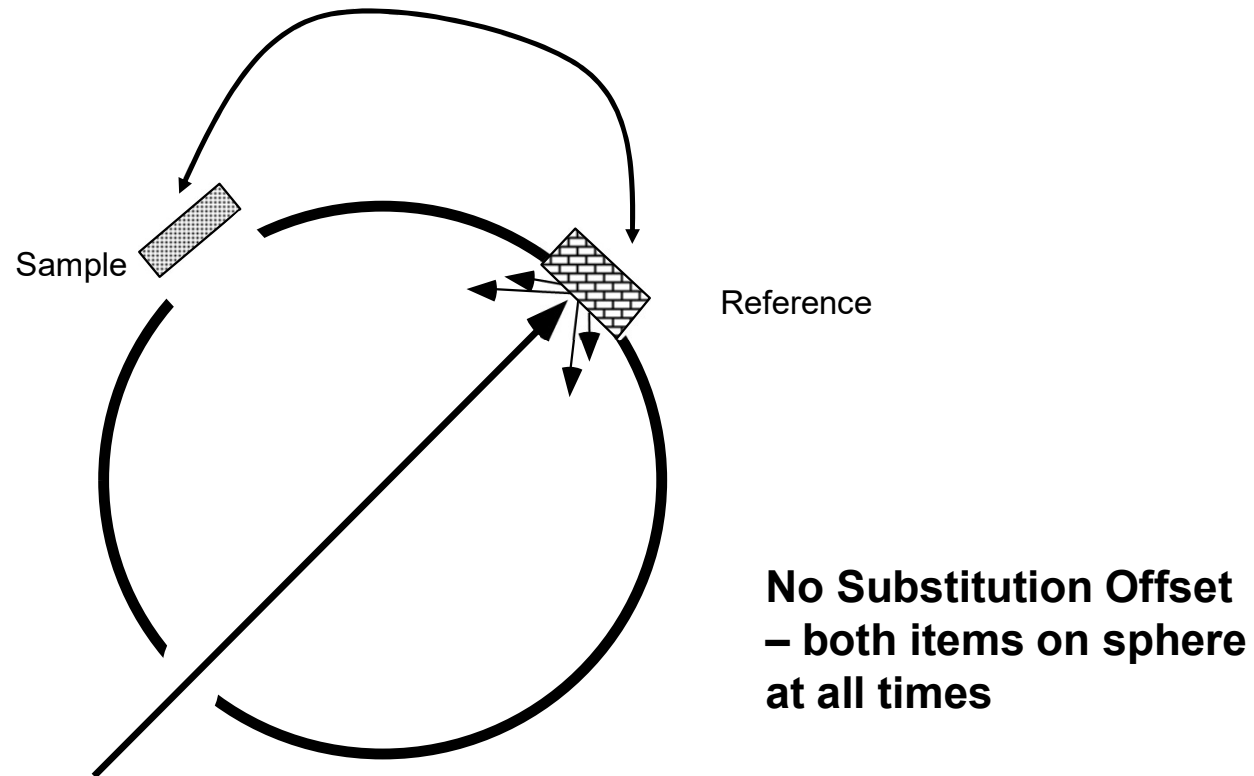
Reflectance/transmittance measurements

Uniform source

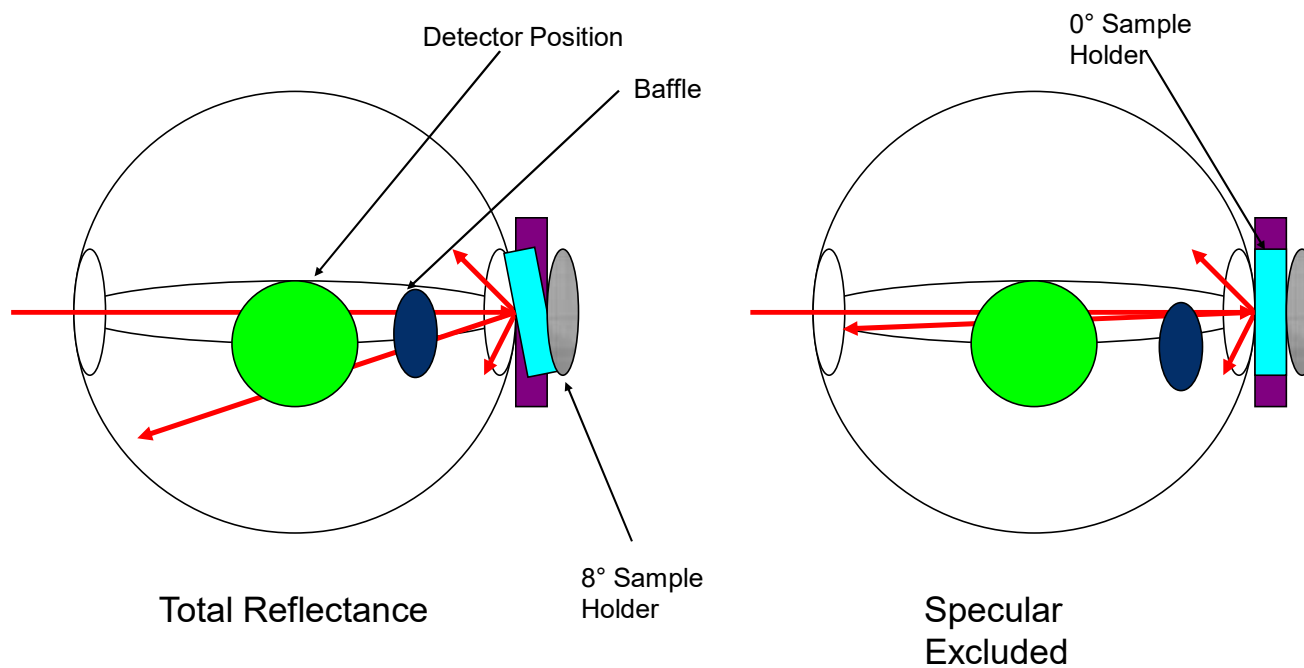
Substitution Method for Reflectance Measurement



Comparison Method for Reflectance Measurement

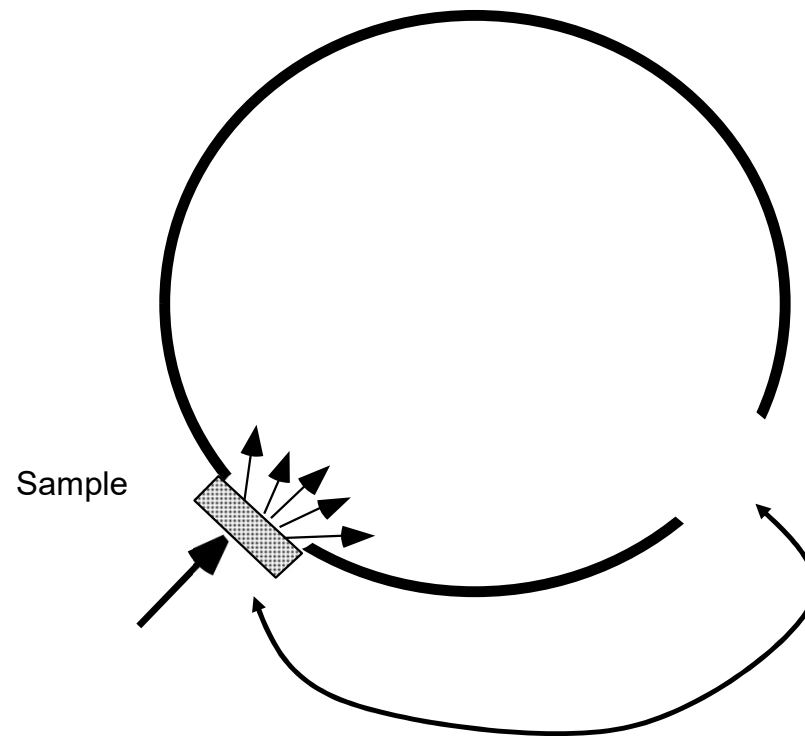


8°/D Hemispherical Reflectance Anatomy

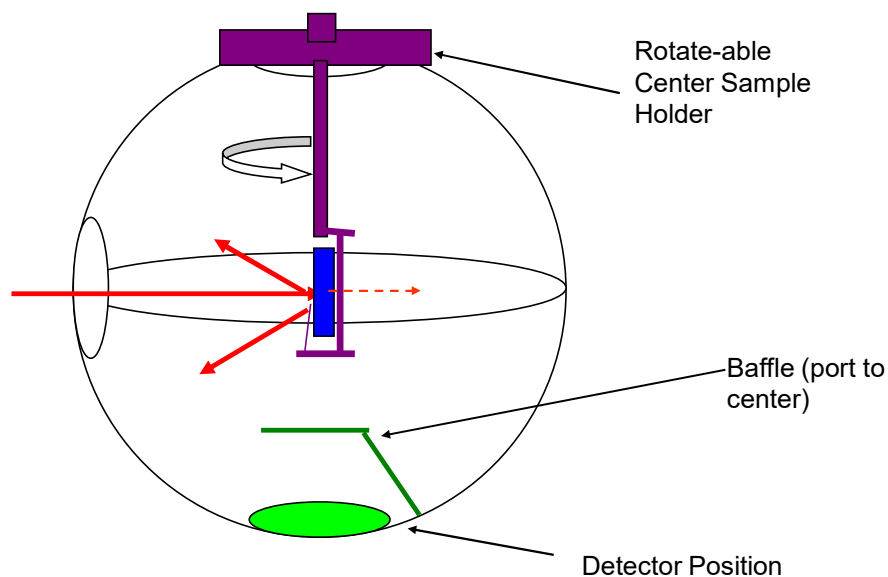


Can also be done using “absolute reference” of the sphere wall

Transmittance Measurement



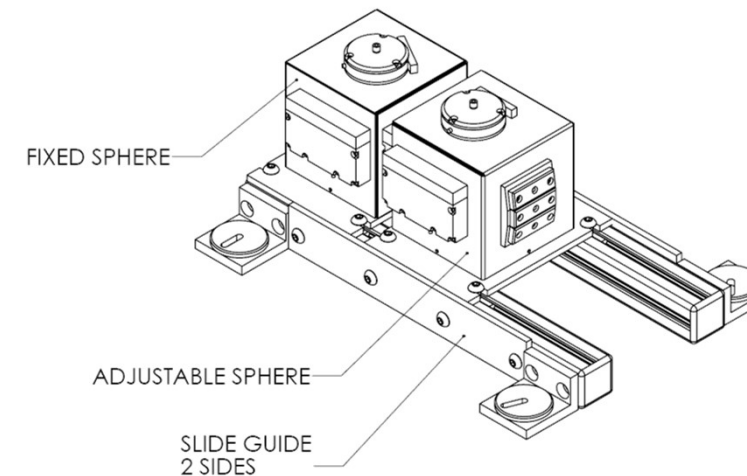
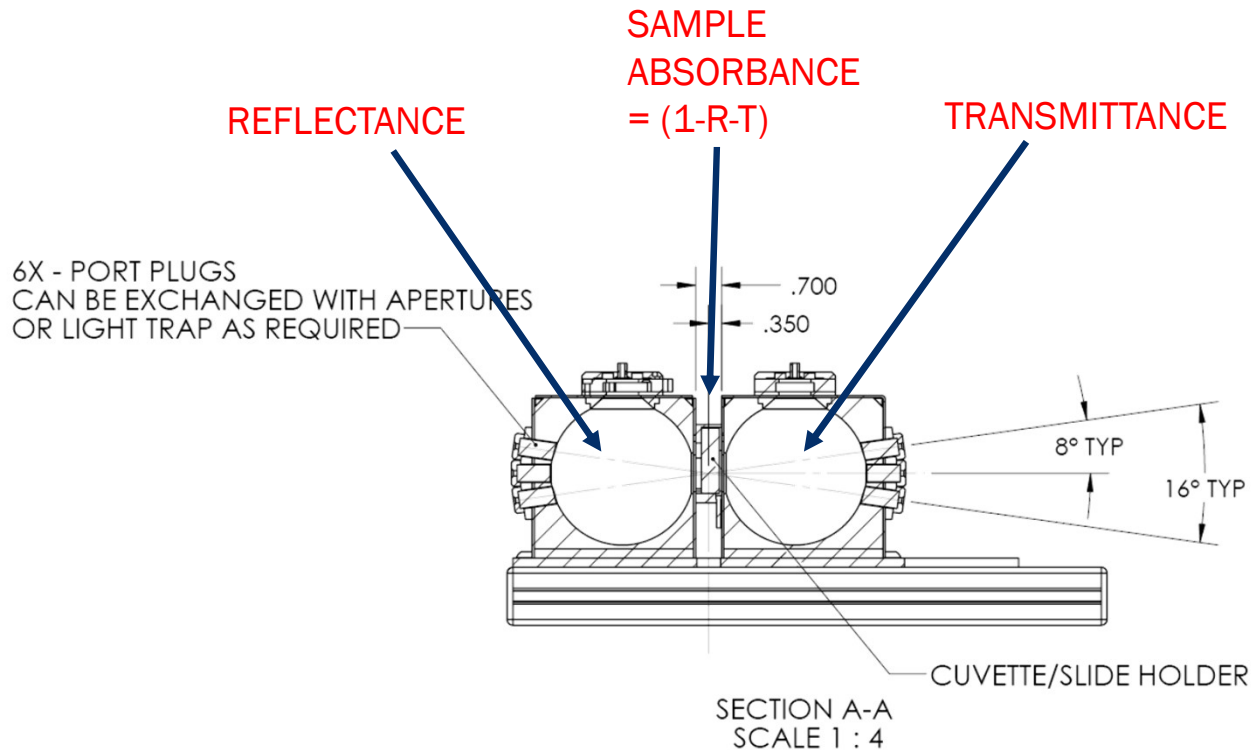
Center Mounted Anatomy



MULTI-ANGLE & “TRANS-FLECTANCE”:
 $(1-R-T-A)=0$

- ▶ Variable Angle
- ▶ Quantum Efficiency Measurements for Phosphors/Fluors (IQE/EQE)
- ▶ Transflectance – BE CAREFUL
 - ▶ Very hard to do absolute.

RTA Double Sphere – Reflectance-Transmittance-Absorbance



- ▶ Also can be used for IQE/EQE for phosphors
- ▶ Possible to get absolute values (still difficult)

— Uses of Integrating Spheres —

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Reflectance/transmittance measurements

Uniform source

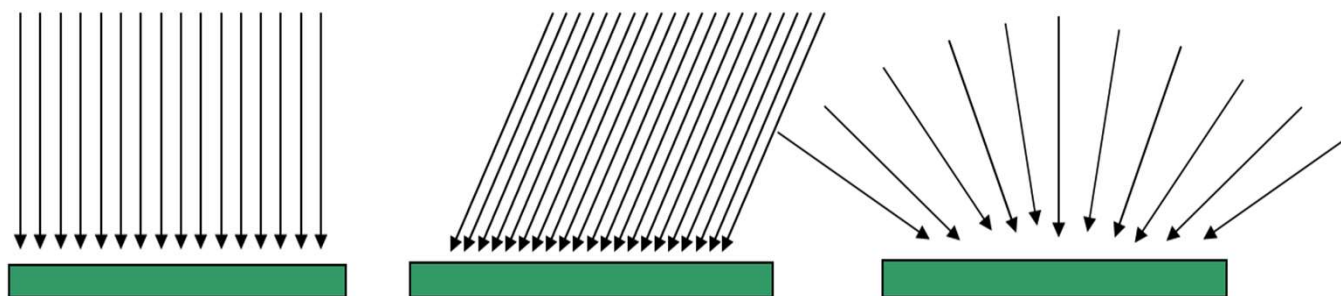
Uniform Source Sphere Overview

Workshop Agenda (All times in MDT)

- ▶ 0730-0840 Sphere Theory and Applications (Durell)
- ▶ 0840-0910 Uniform Source Tutorial (Durell)
- ▶ 0910-0920 Sphere Calibrations (Durell)
- ▶ 0920-0930 (Virtual) Coffee Break
- ▶ 0930-1010 Considerations for Uniform Source Specifications (Scharpf)
- ▶ 1010-1020 Commercial considerations (Scharpf)
- ▶ 1020-1040 NASA GLAMR Case Study (Brendan McAndrew, NASA GSFC)
- ▶ 1040-1050 If time permits: Uniform Source Case Studies (Durell)

Radiometry - Irradiance

► Irradiance/Illuminance

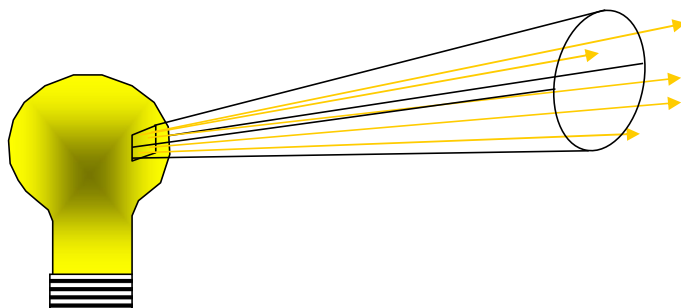


UNITS: W/m^2 - lux (lumens/ m^2) - $\text{ph/m}^2/\text{s}$

Any bare detector or bare FPA (no lens) is sensitive to irradiance

Radiometry - Radiance

► Radiance/Luminance

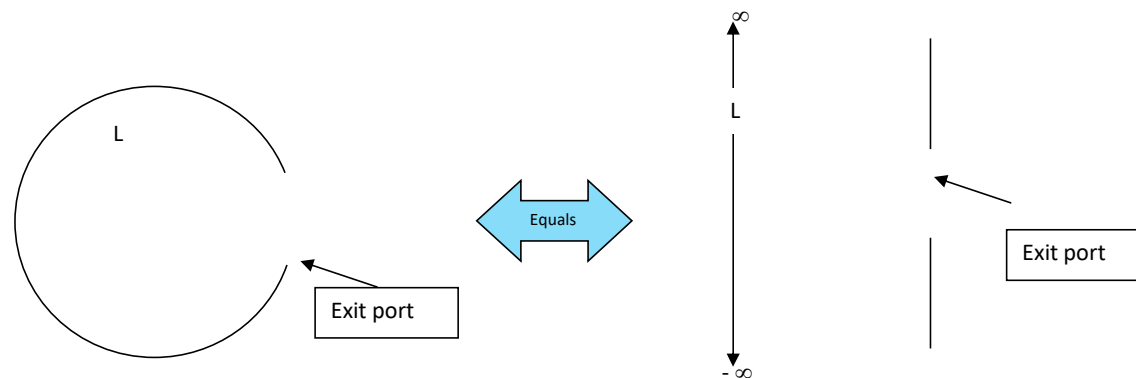


UNITS: $\text{W/m}^2/\text{sr}$ - cd/m^2 - $\text{ph/s/m}^2/\text{sr}$

Any detector with lens is sensitive to radiance

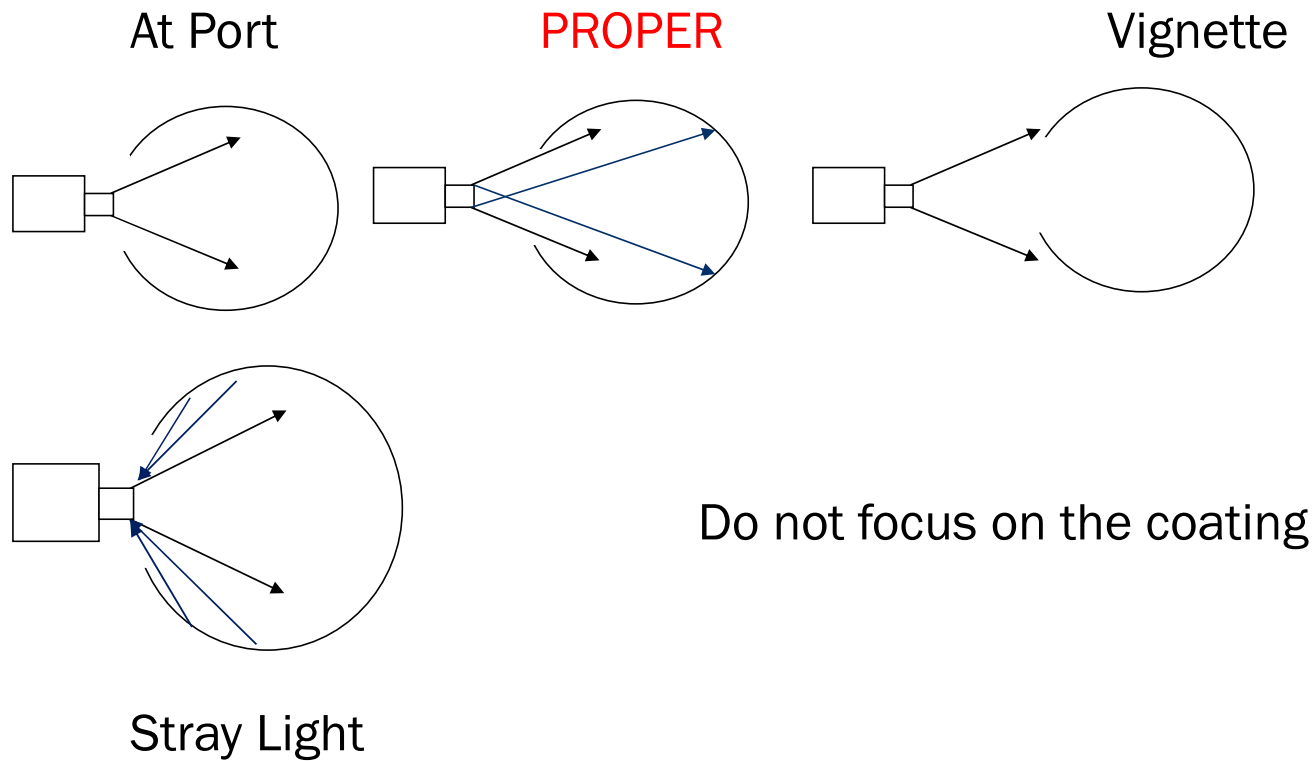
Sphere as a Lambertian Field

- ▶ Radiance is constant whatever the distance to the sphere is.



- ▶ A good working model of an integrating sphere is to consider the port to be a hole in a wall, and, at a totally arbitrary distance behind it, another wall of infinite extent

Proper FOV/Focus with a Sphere



Sphere Radiance Measurements



As far as possible from the sphere to avoid stray light without vignetting

There is no need to focus at the entrance port of the sphere

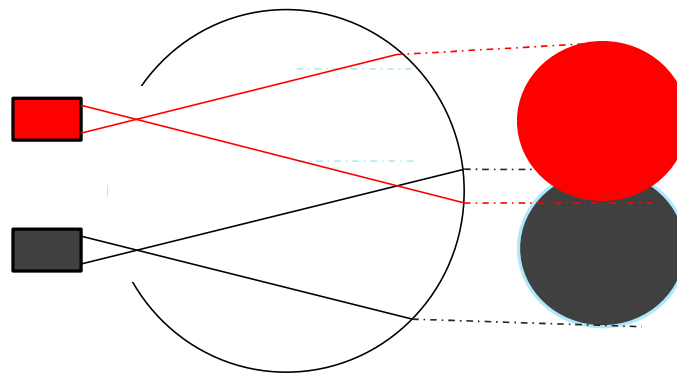
It is better not to focus on the sphere wall (granularity of coating)

The sphere diameter has to be 3 times the sphere port for good uniformity

Definition of Radiance Uniformity

- ▶ Labsphere's standard way of measuring uniformity

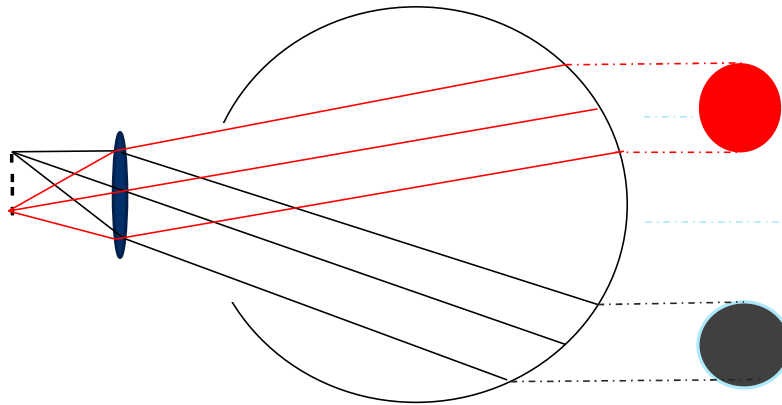
Luminance meter focussed at the entrance port



- ▶ The uniformity is measured as the difference in sphere's radiance between the red spot and the grey spot.
- ▶ Typically normalized to center of the port.
- ▶ Translate in X-Y or Angular

Radiance Uniformity Definition by Optical System

- ▶ Uniformity pixel by pixel - For example

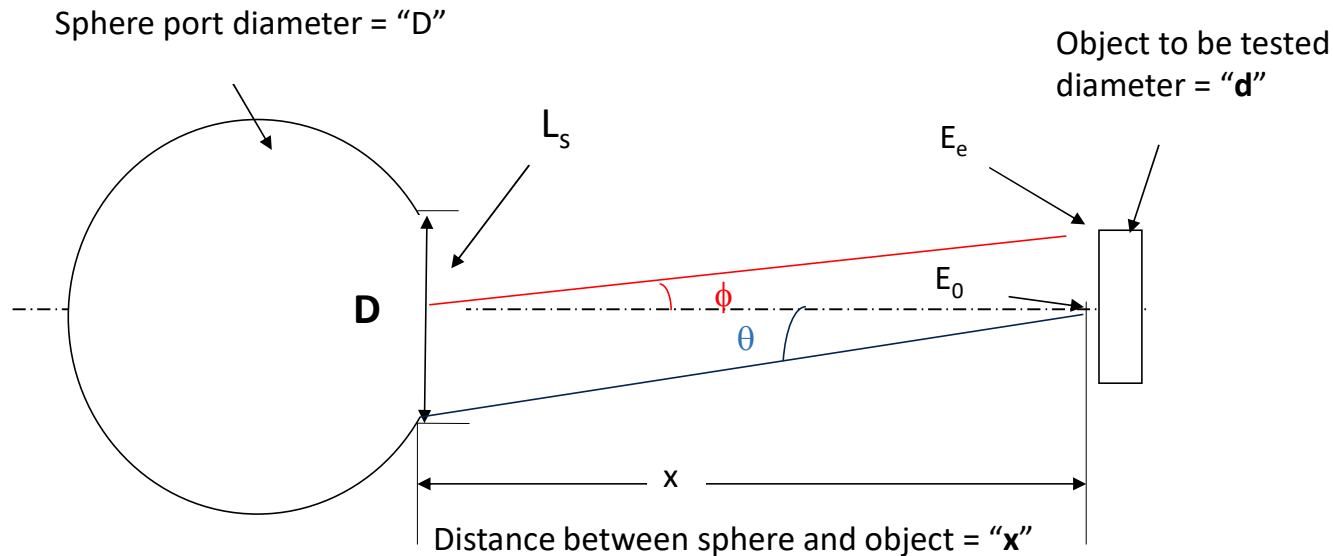


In case of uniformity of <98% both definitions will lead to similar uniformity.

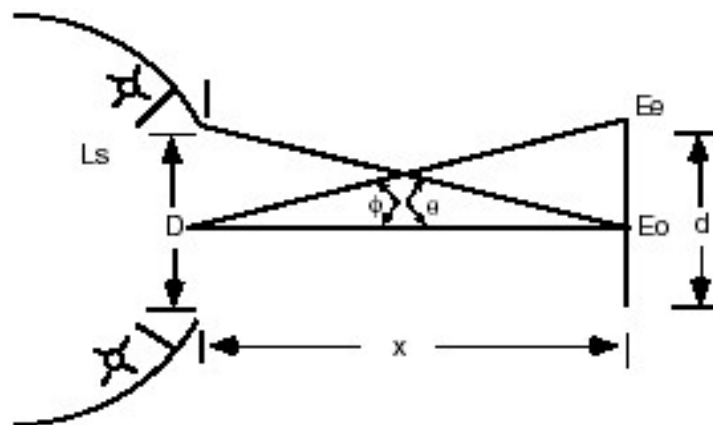
For uniformity >98%, measure uniformity as defined by optical system under test.

Irradiance with a Sphere

- Size of Port (D), Size of Sensor (d), Distance between Sensor and Port (x).



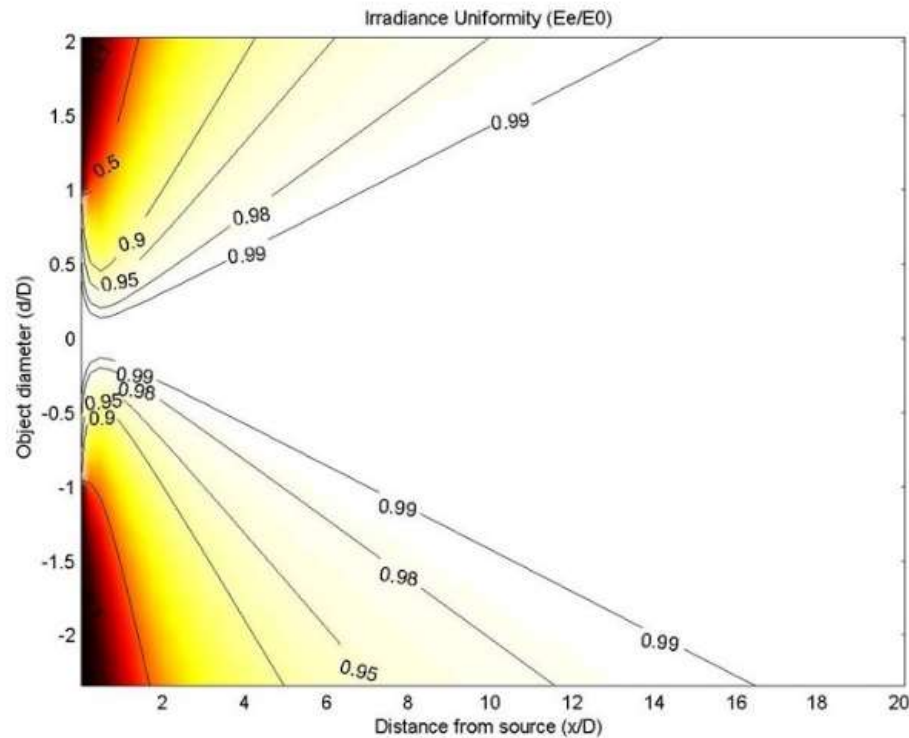
Irradiance Uniformity: d/D and x/D



Object Diameter d/D	Irradiance Uniformity (E_e/E_o) Distance from Source (x/D)												
	0.00	0.10	0.20	0.25	0.50	0.75	1.00	1.50	2.00	2.50	3.00	5.00	10.00
0.1	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00
0.2	1.00	1.00	0.99	0.99	0.98	0.98	0.99	0.99	1.00	1.00	1.00	1.00	1.00
0.3	1.00	0.99	0.98	0.97	0.96	0.96	0.97	0.98	0.99	0.99	1.00	1.00	1.00
0.4	1.00	0.99	0.96	0.94	0.92	0.93	0.95	0.97	0.98	0.99	0.99	1.00	1.00
0.5	1.00	0.97	0.92	0.90	0.88	0.90	0.92	0.96	0.97	0.98	0.99	1.00	1.00
0.6	1.00	0.95	0.88	0.85	0.82	0.86	0.89	0.94	0.96	0.97	0.98	0.99	1.00
0.7	1.00	0.92	0.81	0.78	0.76	0.81	0.86	0.92	0.95	0.96	0.97	0.99	1.00
0.8	1.00	0.84	0.72	0.69	0.70	0.76	0.82	0.89	0.93	0.95	0.97	0.99	1.00
0.9	1.00	0.70	0.60	0.59	0.62	0.71	0.78	0.87	0.92	0.94	0.96	0.98	1.00
$\sin^2 \theta$	1.000	0.962	0.862	0.800	0.500	0.308	0.200	0.100	0.059	0.038	0.027	0.010	0.002
$\pi \sin^2 \theta$	3.142	3.021	3.708	2.513	1.571	0.967	0.628	0.314	0.185	0.121	0.085	0.031	0.008

Note: Boundary lines delineate regions of 98%, 95%, and 90% irradiance uniformity

Irradiance Ratios: d/D and x/D

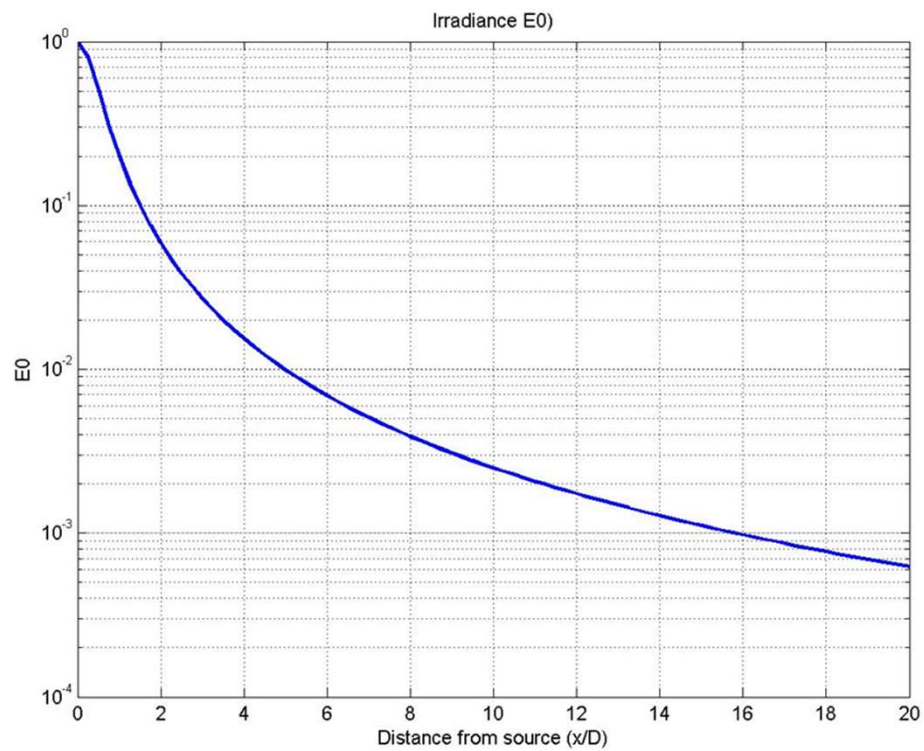


Irradiance is very uniform at sphere port, then degrades with distance.

Uniformity returns as distance increases (point source)

At distance, uniformity is proportional to the \cos^4 of the small angle (δ)

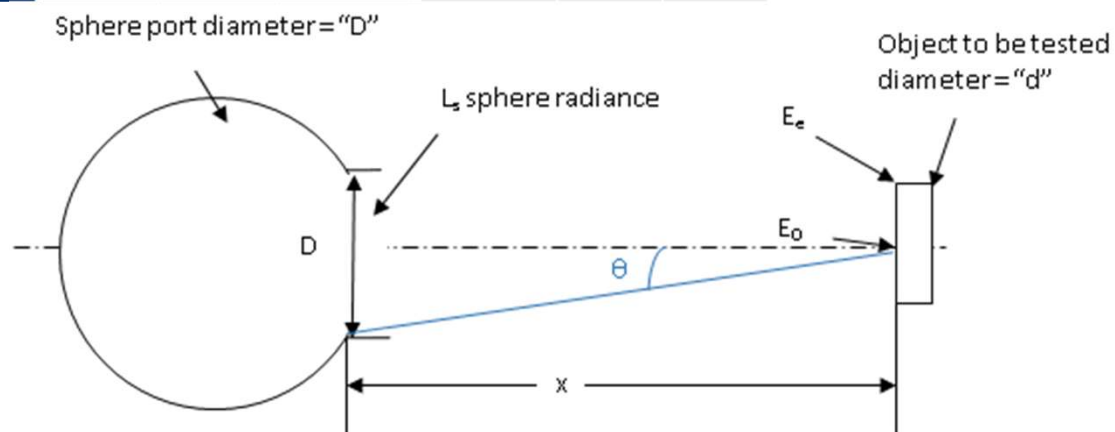
Irradiance Decrease with Distance



Irradiance Decrease with Distance

	θ					
angle (°)	1.8	3.6	7.2	14.5	30	45
N.A.	0.03	0.06	0.13	0.25	0.5	0.71
f/#	16	8	4	2	1	0.71
$\pi.\sin^2\theta$	0.001	0.004	0.016	0.063	0.25	0.50

$$E_0 = \pi.L_s.\sin^2\theta$$



Irradiance and FOV (f/#)

When testing a detector for flat fielding or response, one wants certainly to use the same FOV as the one the detector will see when mounted in the camera.

The way to define a system with a sphere is:

- ▶ Define the uniformity needed on the detector
- ▶ Calculate the distance needed to get this uniformity using the \cos^4 rule
- ▶ When the distance is defined, then the FOV will determine the size of the port needed on the sphere

As an example :

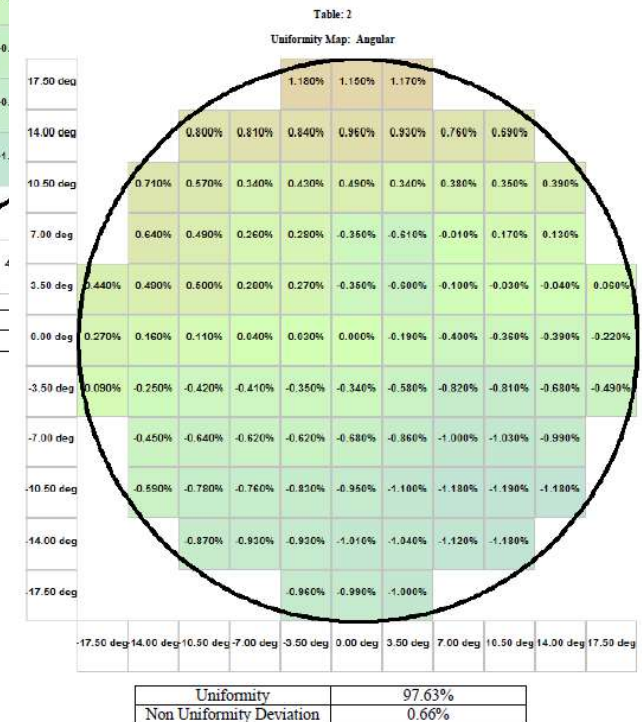
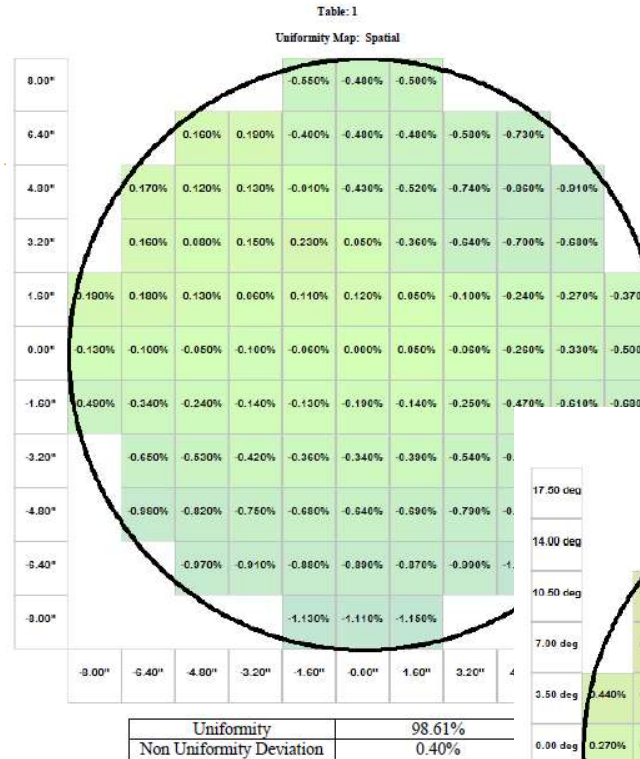
Detector: 13mm diagonal – FOV : f/2 - requested irradiance uniformity : 98%

- ▶ Using the \cos^4 law angle should be 5.7° and the distance should be 65mm
- ▶ f/# of 2 means that the sphere port dia should be 33mm

Sphere vs. a Target: Why?

Main reasons:

- ▶ Uniformity:
 - ▶ Spatial and Angular (10cm port shown)
- ▶ Dynamic range (>100dB)
- ▶ Mix of sources (Solar, QTH, Laser)
- ▶ Monitoring of light levels and absolute measurements with known uncertainty
- ▶ Spheres are depolarized
- ▶ Low Uncertainty Calibration for Downwelling* / Upwelling Sensors



Uniformity & Level of a Target

The uniformity in radiance will depend on the uniformity in irradiance of the source projected at the target. OK for small targets or large distances....not OK for short distance or large targets.

Examples:

Lamp @ 50cm and 10cm Target

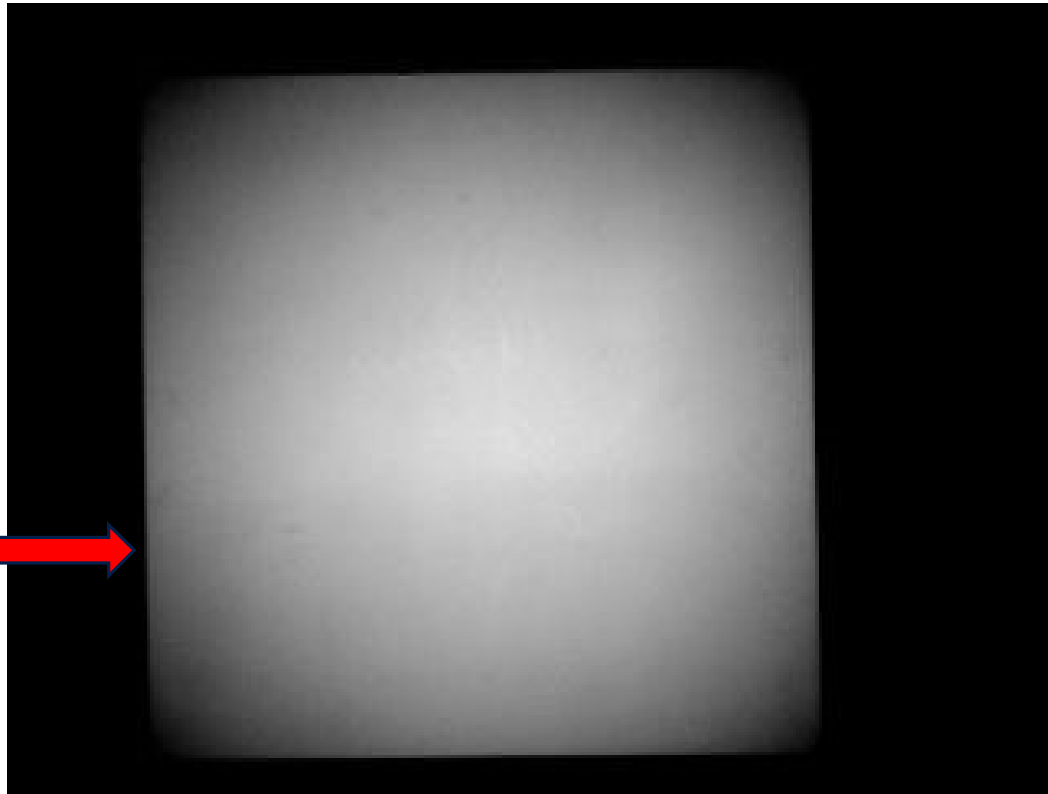
Irradiance $\sim \cos^3$

Uniformity $\sim \pm 1.5\%$ (97%)

Lamp @ 50cm and 30cm Target

Irradiance $\sim \cos^3$

Uniformity $\sim \pm 12\%$ (86%)



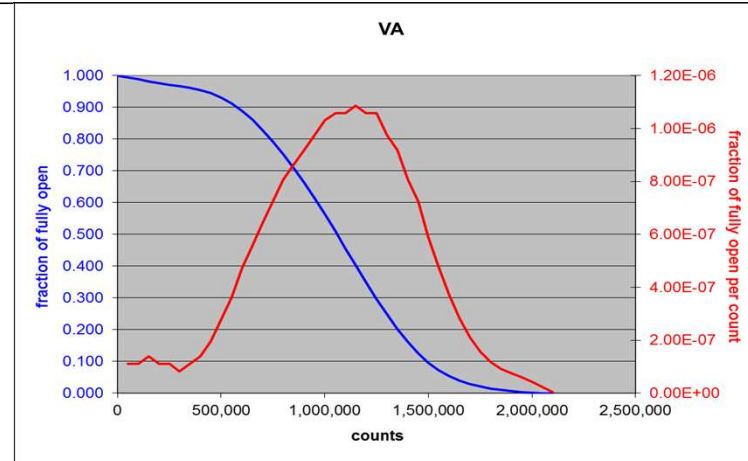
Spheres: Dynamic Range (DR)

► Units:

dB : $20 \cdot \log_{10}(\text{DR})$

bits : $\log_2(\text{DR})$

decades : $\log_{10}(\text{DR})$

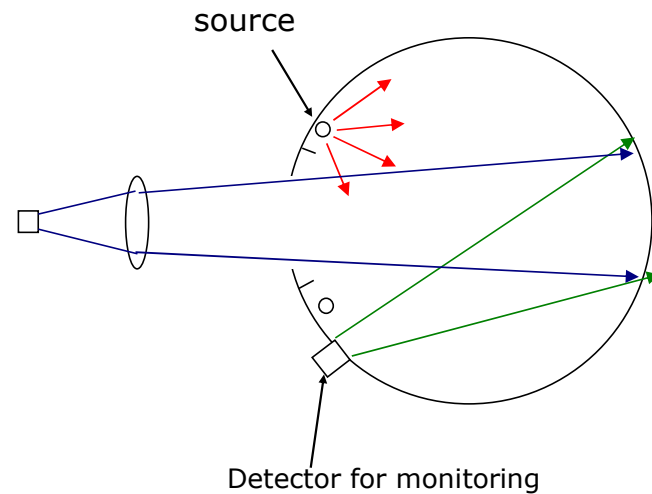


Dynamic range with target using combination of grey target and distance to the target: **0-40dB**

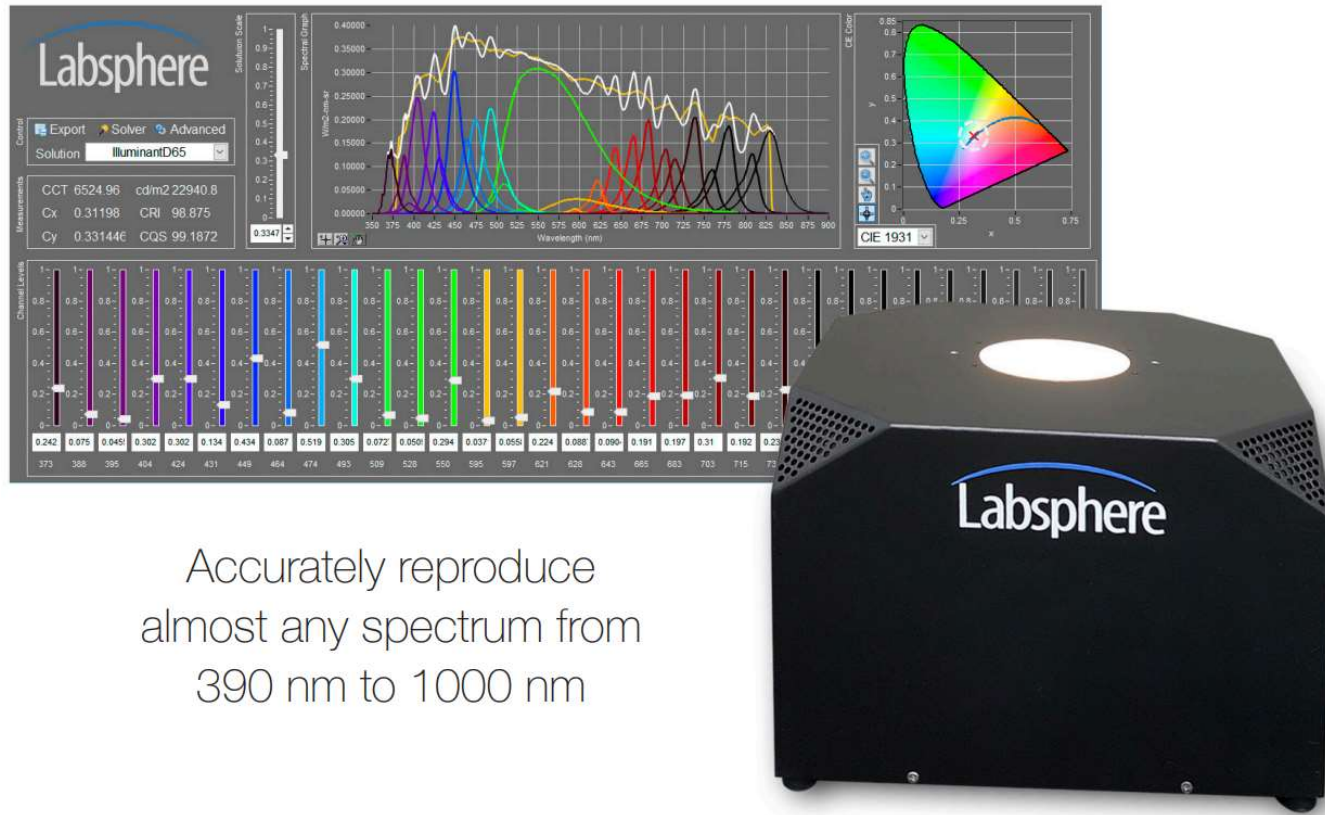
Dynamic range with a sphere system: **40-160dB+**

Sphere: Monitoring & Absolute Measurements with Known Uncertainty

Detector on the sphere can be calibrated to reflect the radiance or irradiance delivered by the sphere



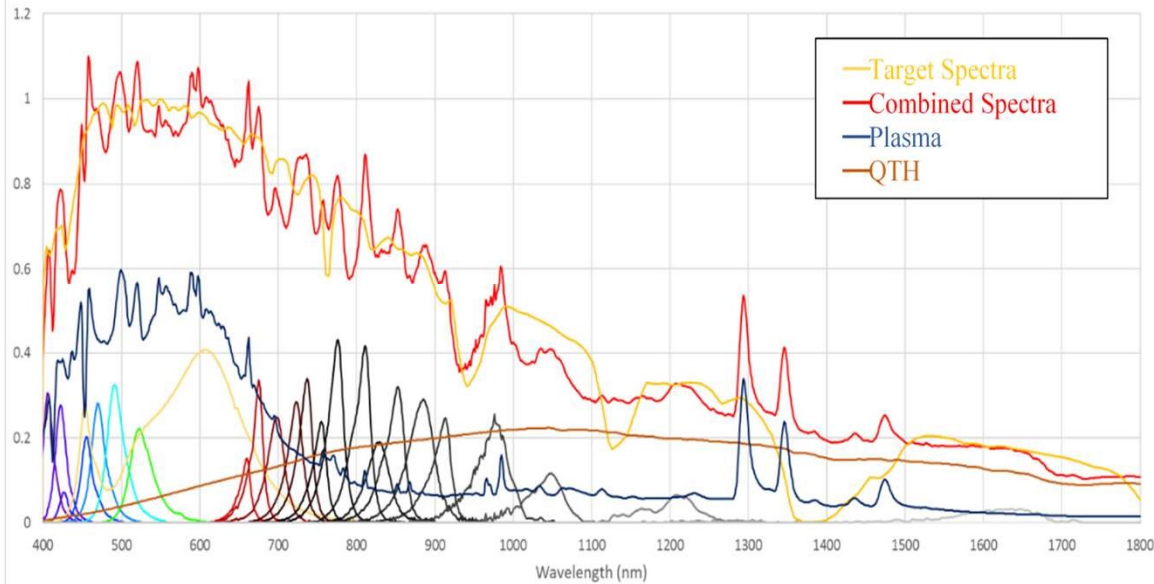
Spheres - Creating Light Mixing or Tuneable Sources



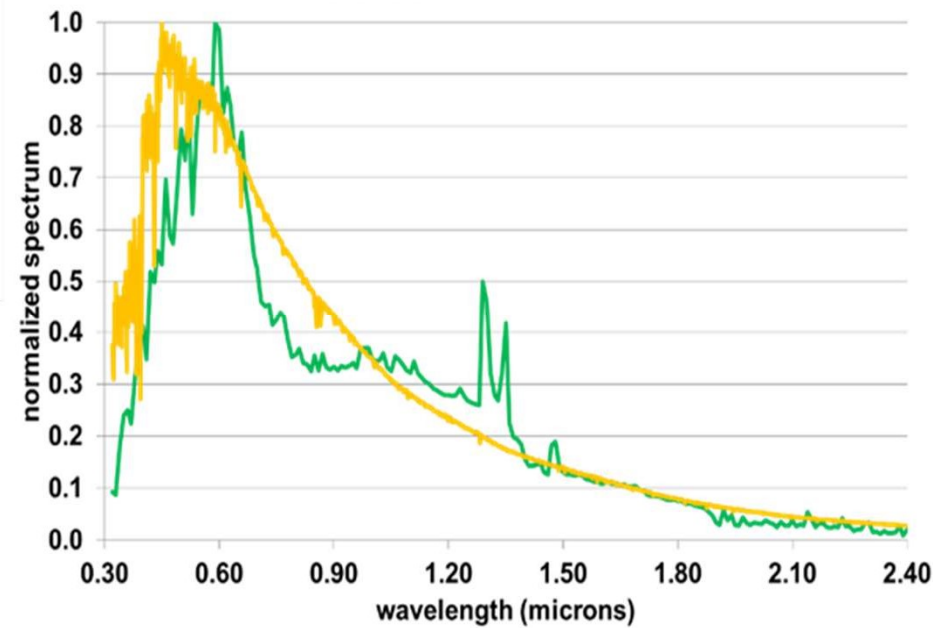
- ▶ Large Arrays of LEDs
 - ▶ Provide high radiance in spheres
- ▶ Spectral Shaping for Tunability Systems
 - ▶ Independent control and flux integration
 - ▶ Global optimization using spectral fit objective functions provide match to target spectra
 - ▶ Can emulate many different sources including broadband through the visible and NIR

Combining Broadband and Other sources – Solar examples

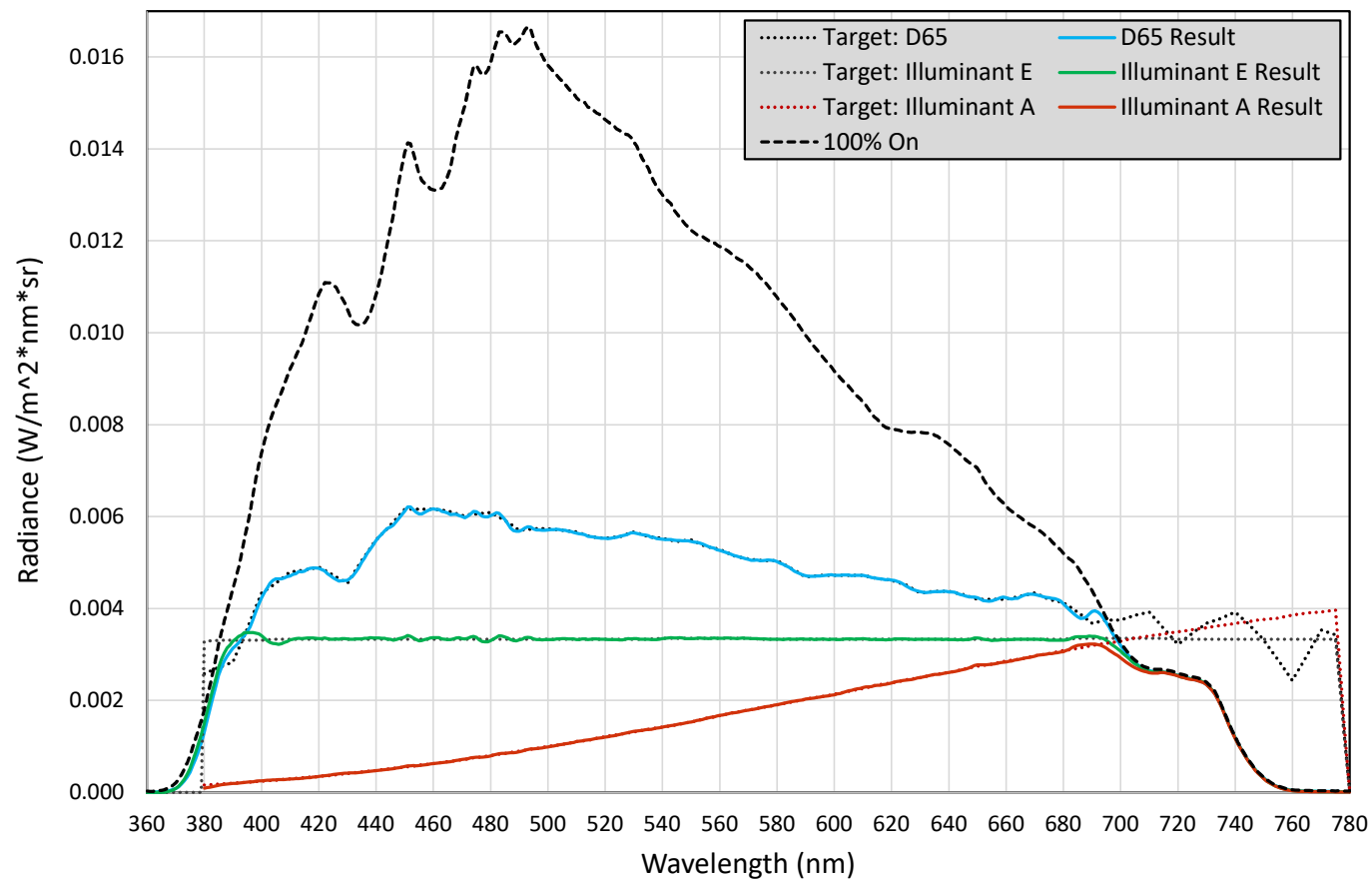
BlueSky



PEL-250 and QTH vs. AM0



Polychromator: Standard Illuminants matching



Calibration of Integrating Spheres

Workshop Agenda (All times in MDT)

- ▶ 0730-0840 Sphere Theory and Applications (Durell)
- ▶ 0840-0910 Uniform Source Tutorial (Durell)
- ▶ 0910-0920 Sphere Calibrations (Durell)
- ▶ 0920-0930 (Virtual) Coffee Break
- ▶ 0930-1010 Considerations for Uniform Source Specifications (Scharpf)
- ▶ 1010-1020 Commercial considerations (Scharpf)
- ▶ 1020-1040 NASA GLAMR Case Study (Brendan McAndrew, NASA GSFC)
- ▶ 1040-1050 If time permits: Uniform Source Case Studies (Durell)

Sphere Calibrations

The reflectance of the sphere cannot be known with low enough uncertainty to calculate throughput accurately enough for calibration.

Therefore, all sphere calibrations are SOURCE BASED calibrations.

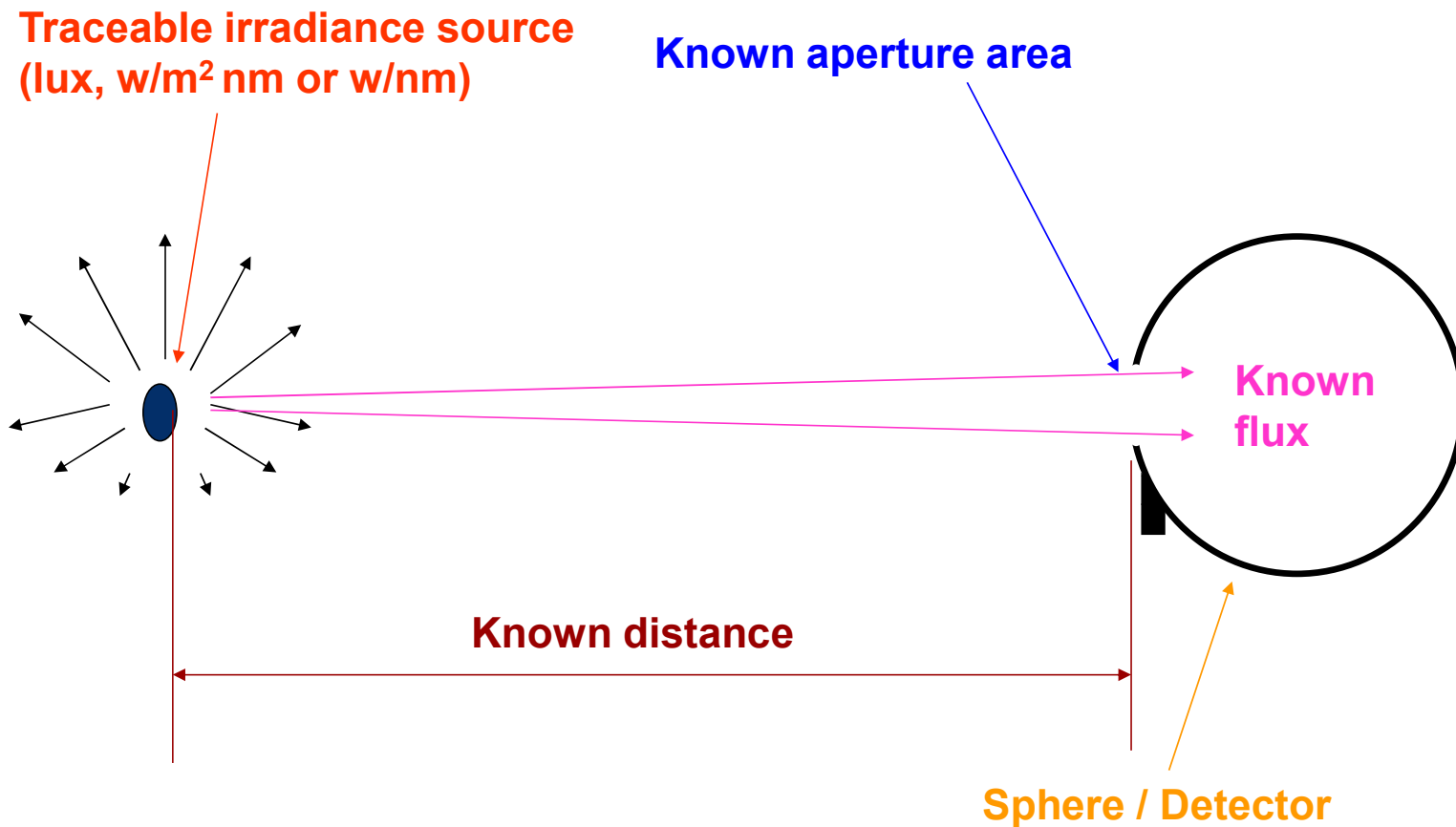
Calibration of Spheres

Radiometers/photometers

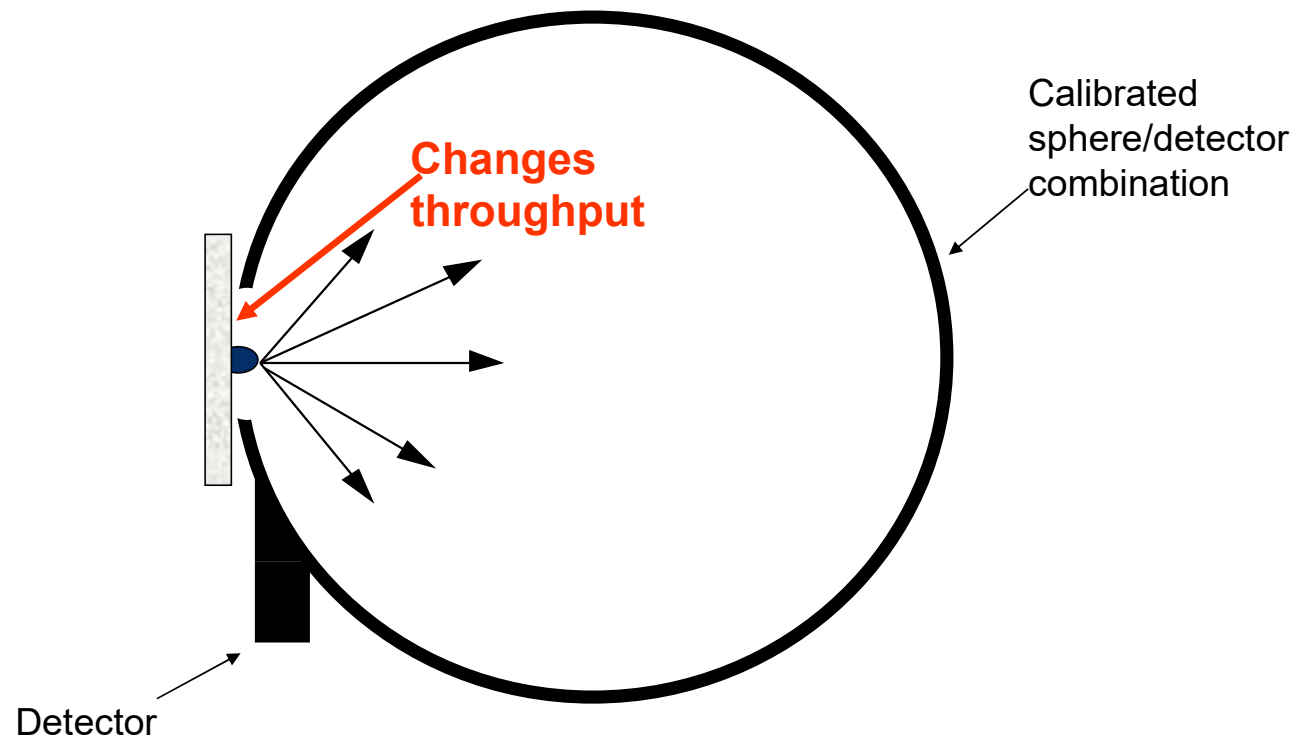
Reflectance/transmittance measurements

Uniform source

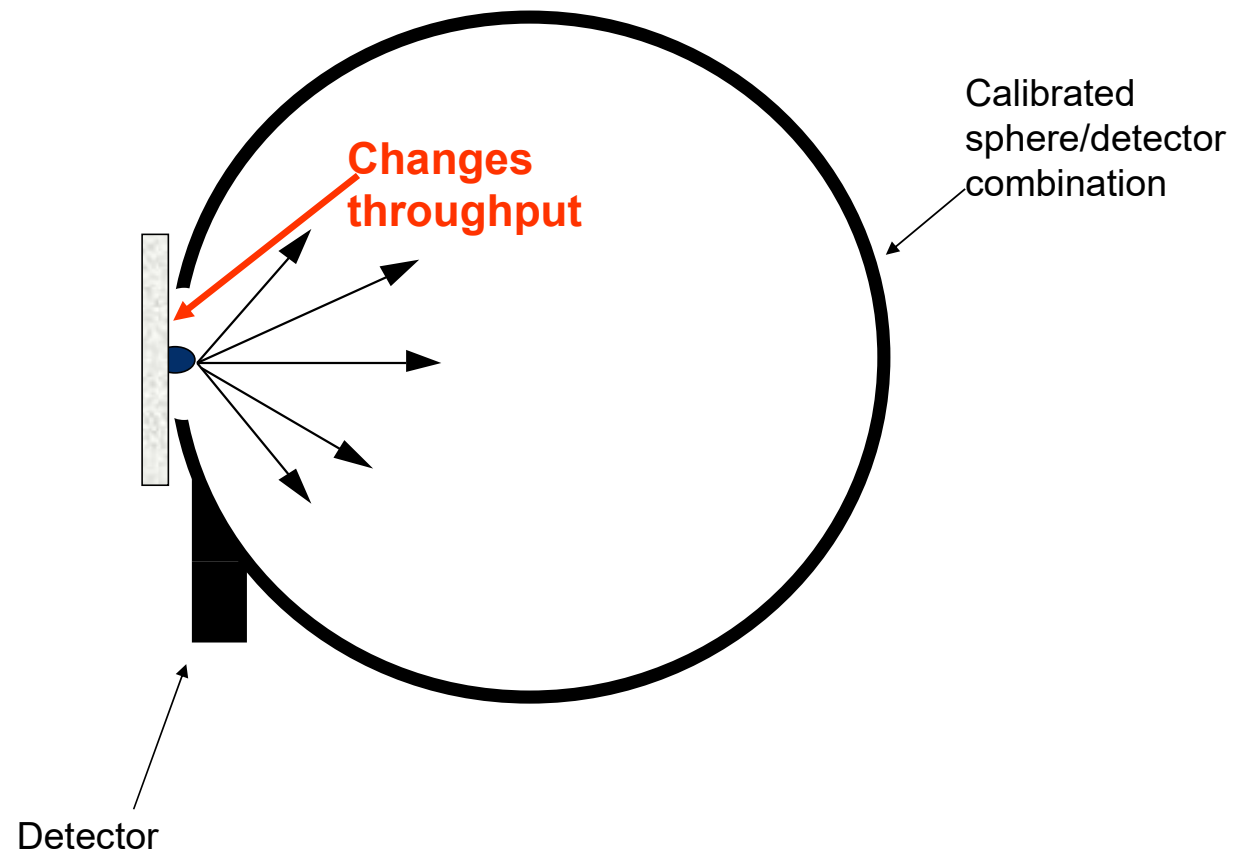
Calibration of Radiometers/Photometers/Laser Power



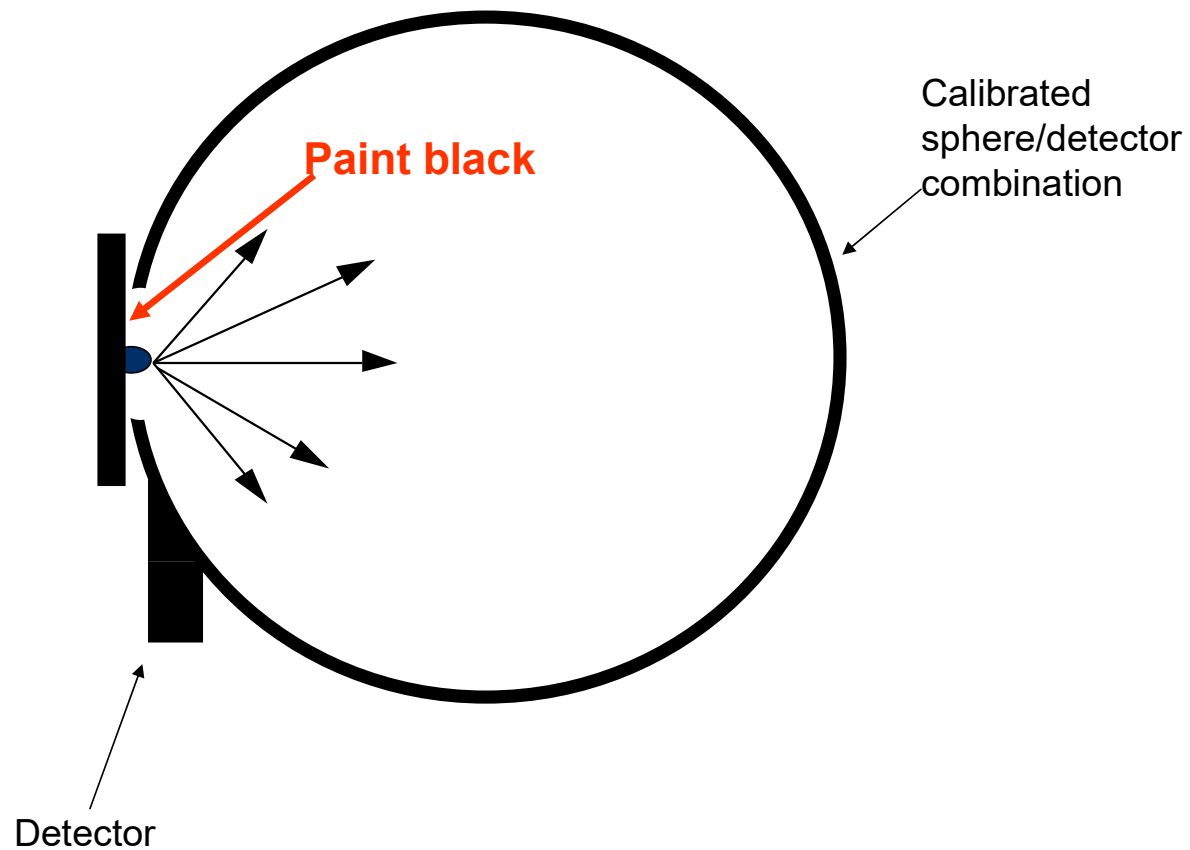
LED / Laser Substitution Error



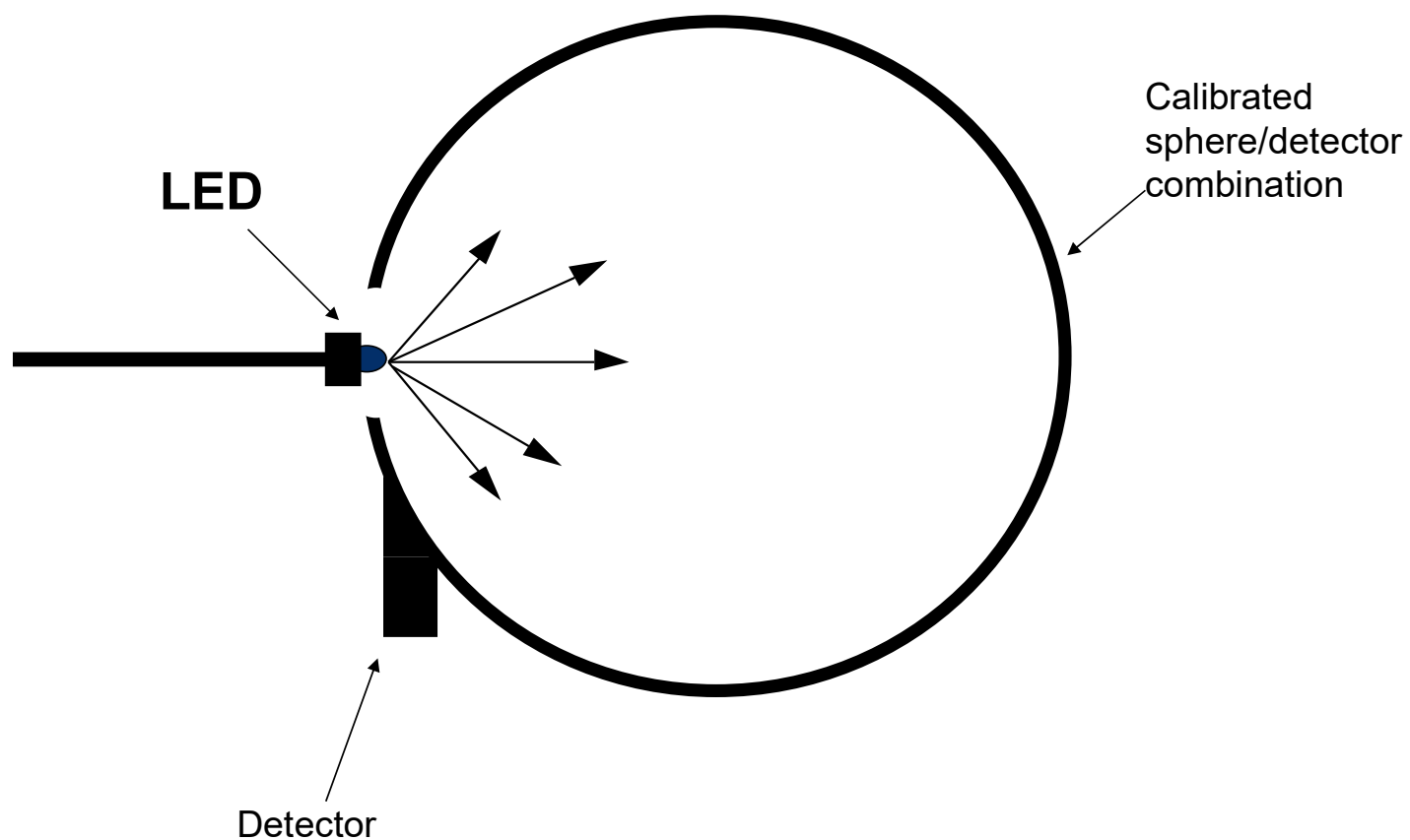
LED / Laser Substitution Error



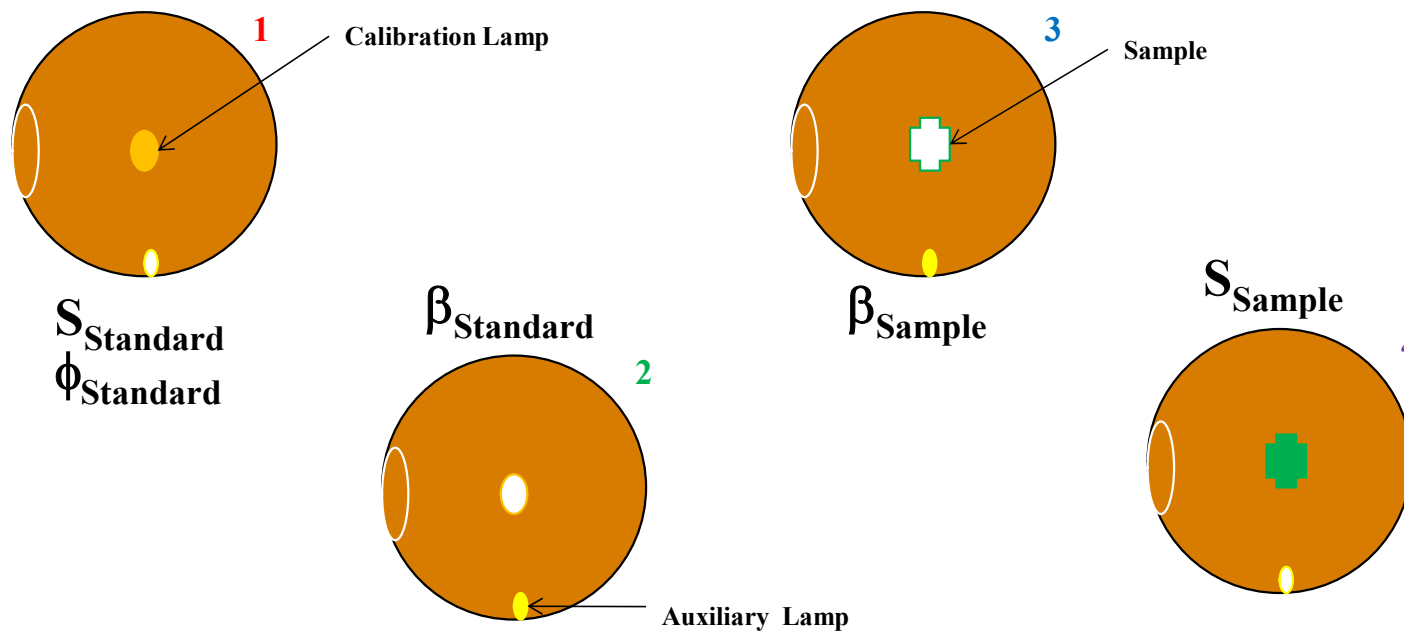
LED / Laser Substitution Error



LED / Laser Substitution Error



Internal/External Lamp Measurement Calibration



$$\phi_{\text{Sample}}(\lambda) = \frac{S_{\text{Sample}}^4(\lambda)}{S_{\text{Standard}}^1(\lambda)} * \frac{\beta_{\text{Standard}}^2(\lambda)}{\beta_{\text{Sample}}^3(\lambda)} * \phi_{\text{Standard}}^1(\lambda)$$

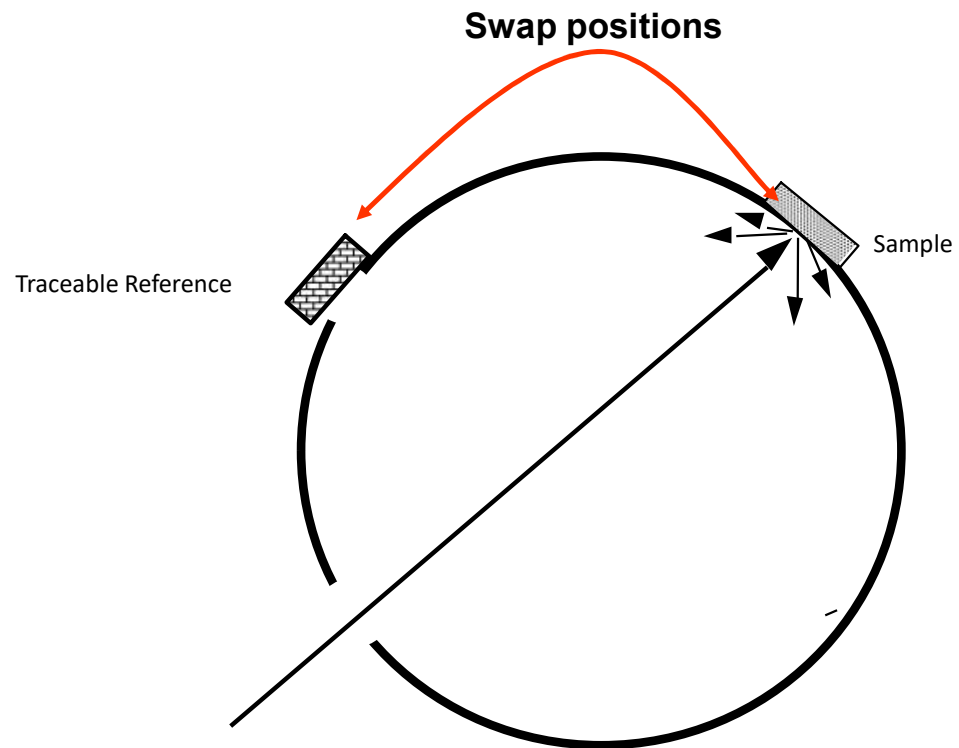
Sphere Calibration

Radiometers/photometers

Reflectance/transmittance measurements

Uniform source

Reflectance Calibration



**Both Sample Stay on
Sphere during each
measurement – no
substitution error.**

Sphere Calibration

Radiometers/photometers

Reflectance/transmittance measurements

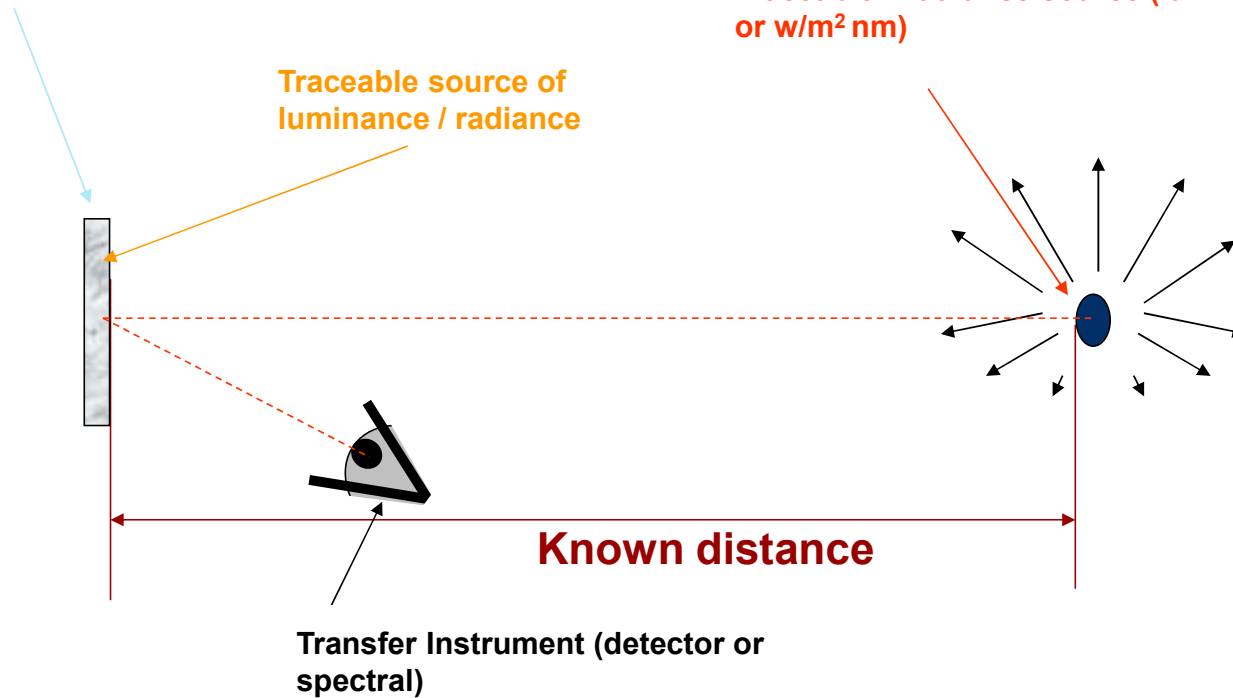
Uniform source

Uniform Source Calibration

Traceable reflectance factor
(Lambertian Target)

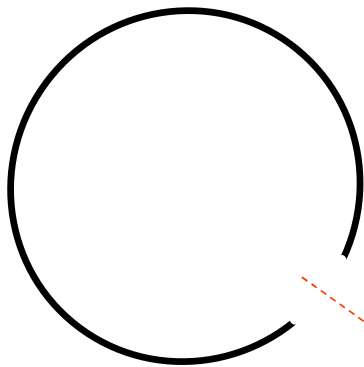
Traceable source of
luminance / radiance

Traceable irradiance source (lux
or $\text{W/m}^2 \text{ nm}$)

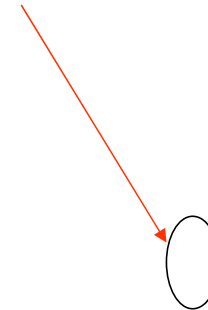


Uniform Source Calibration

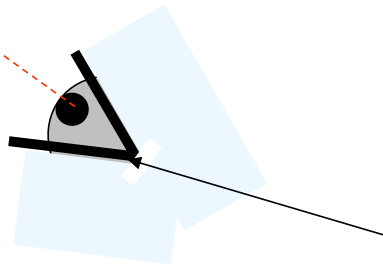
**Transfer calibration
to sphere source**



**Traceable irradiance
source (lux or $\text{W/m}^2 \text{ nm}$)
OFF**

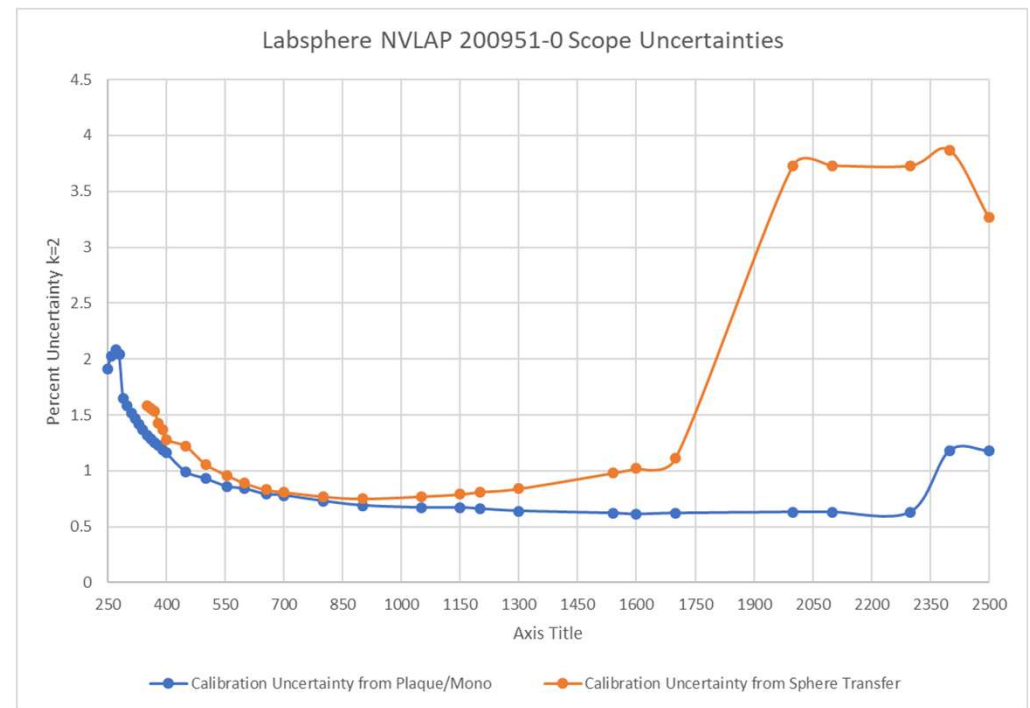


**Transfer Instrument
(detector or spectral)**



Traceability for Integrating Sphere Calibration Source

- Begins with SI Units and the National Metrology Institutes
 - Transfer from NIST primary irradiance source off calibrated Lambertian plaque to monochromator detector
- Increases in NMI accuracy improves uncertainty across industry/EO community
 - NIST recently added (2018) 2500 nm, extends our capability
- Traceability chain to NIST - <1% relative uncertainty 555 – 1600 nm



Uniform Source Case Studies

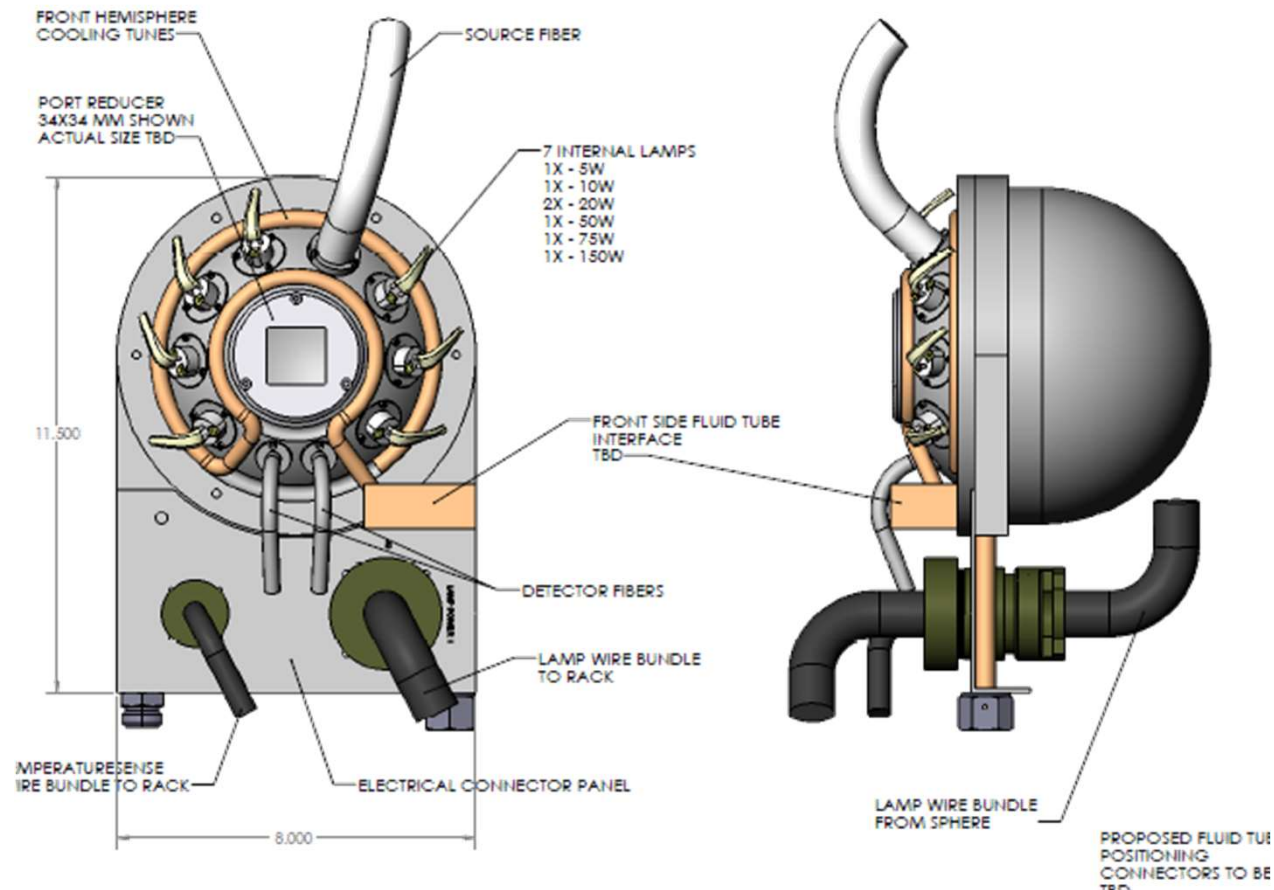
(If time permits...)

Landsat 8 & 9 OLI Calibration System



- ▶ 100% QTH
- ▶ >160dB Dynamic Range
- ▶ Extraterrestrial Sunlight Levels to Night Vision.
- ▶ Spectral and Band Monitoring
- ▶ >98% Uniformity over 8 decades.
- ▶ 1% variation in Uniformity at each level
- ▶ Water-Cooled

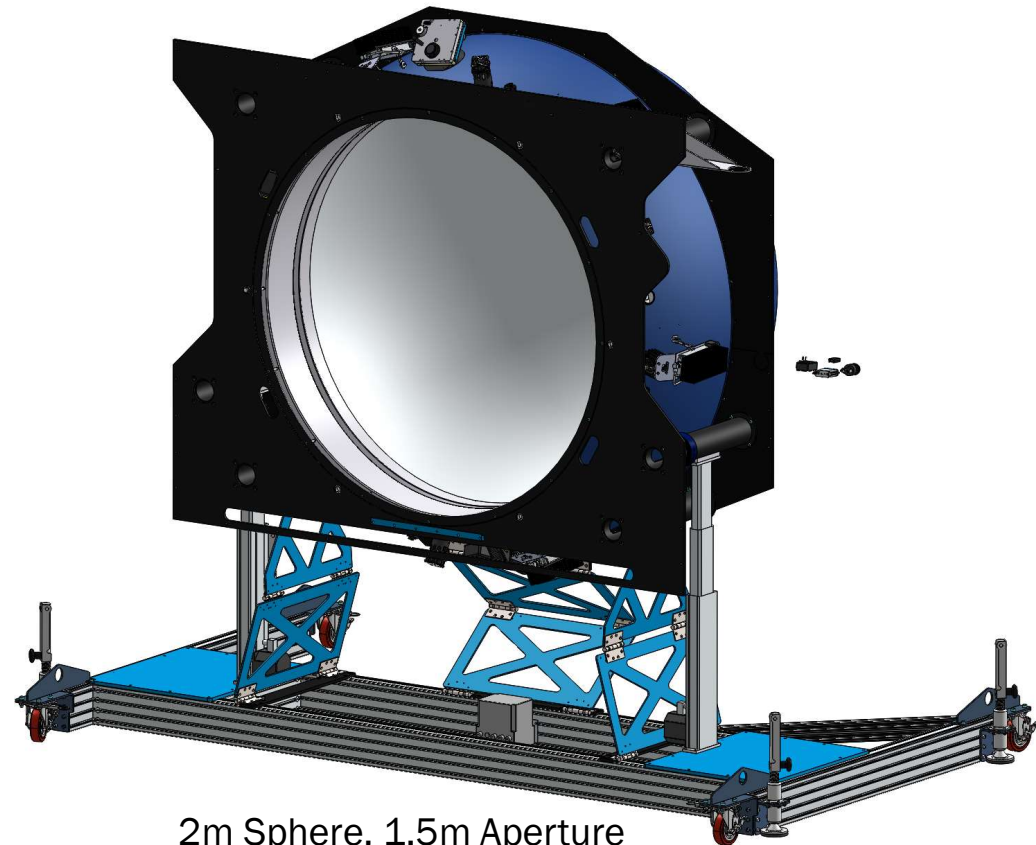
Water cooled, vacuum-ready, variable output source – OLI 8/9



Japan & India – 2m Next Generation Satellite Calibrators

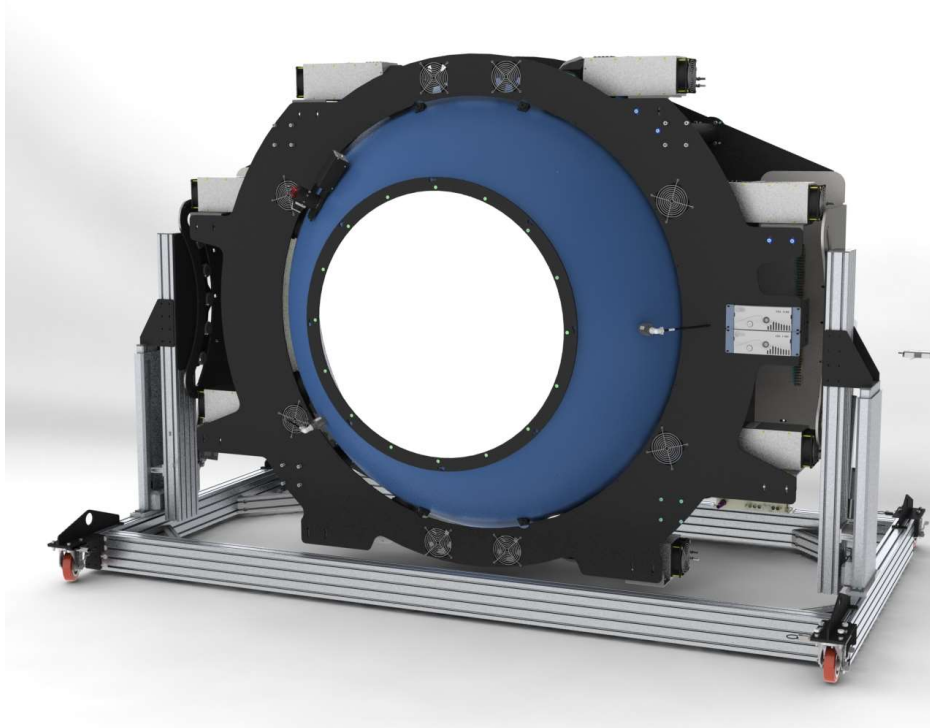


2m Sphere, 1.2m Aperture QTH

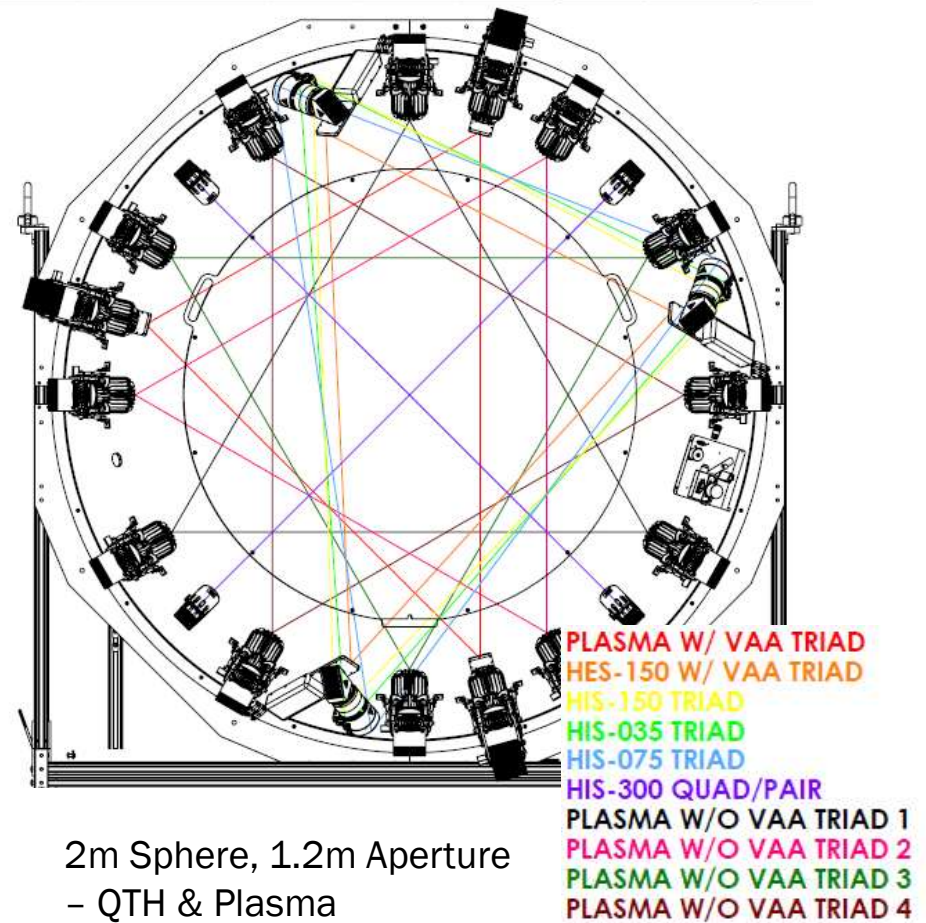


2m Sphere, 1.5m Aperture
Plasma, Laser and QTH

China & Korea – Next Generation

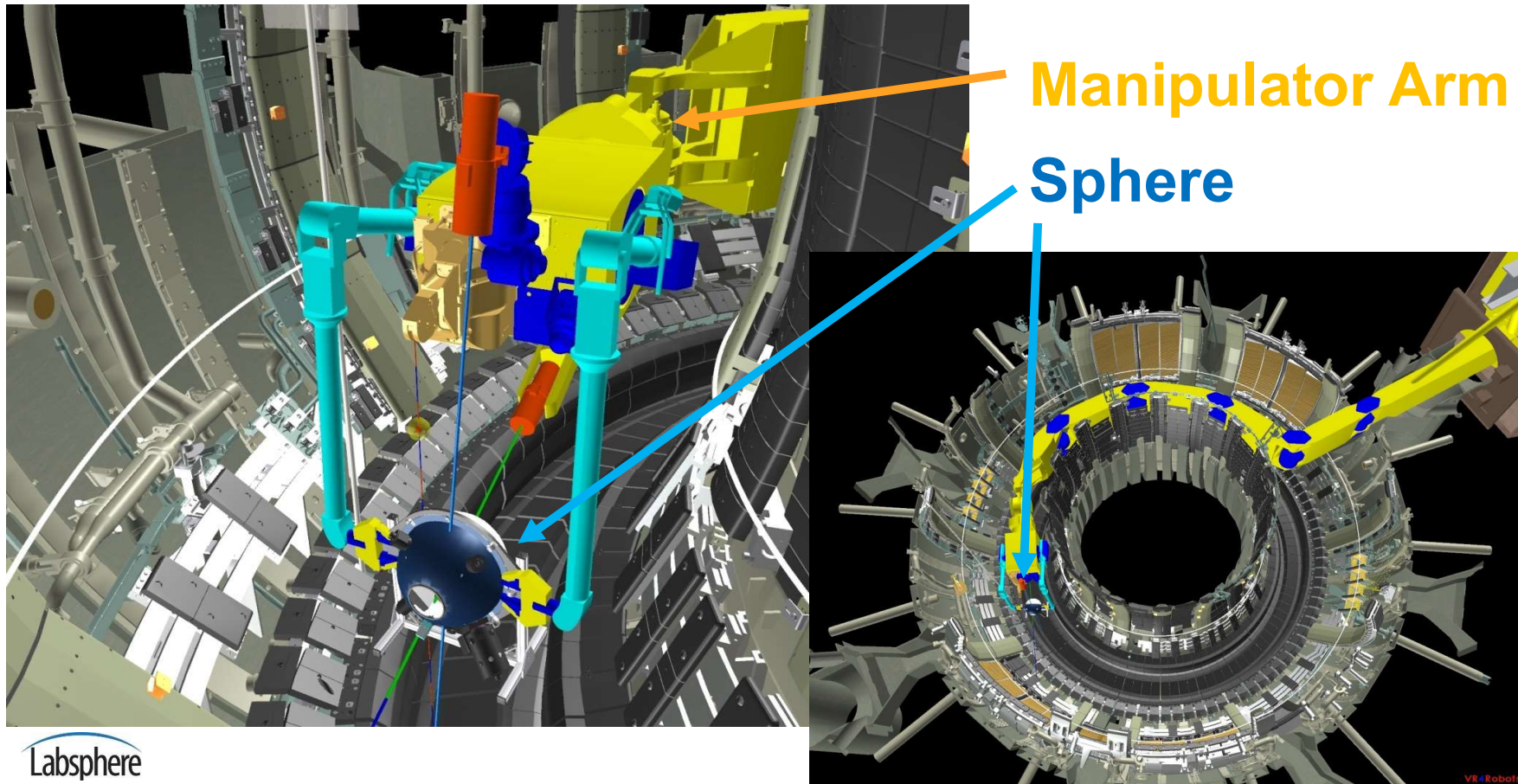


2m Sphere, 1.2m Aperture – QTH & Xenon



2m Sphere, 1.2m Aperture
– QTH & Plasma

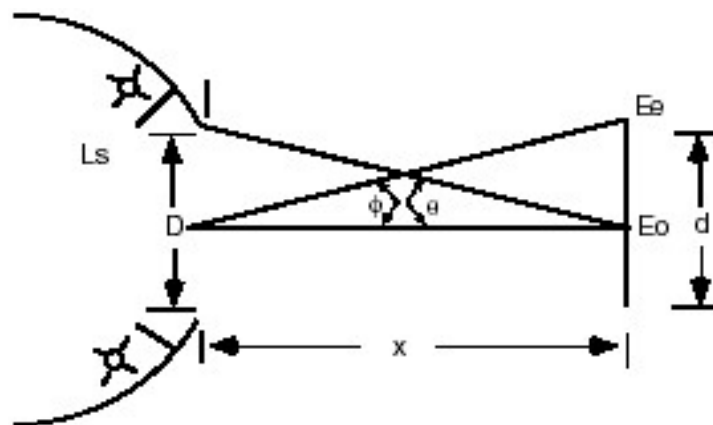
Joint European Torus (JET) – Calibration Sphere



VIRTUAL COFFEE BREAK

(10 Minutes)

Irradiance Uniformity: d/D and x/D



Object Diameter d/D	Irradiance Uniformity (E_e/E_o) Distance from Source (x/D)												
	0.00	0.10	0.20	0.25	0.50	0.75	1.00	1.50	2.00	2.50	3.00	5.00	10.00
0.1	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00
0.2	1.00	1.00	0.99	0.99	0.98	0.98	0.99	0.99	1.00	1.00	1.00	1.00	1.00
0.3	1.00	0.99	0.98	0.97	0.96	0.96	0.97	0.98	0.99	0.99	1.00	1.00	1.00
0.4	1.00	0.99	0.96	0.94	0.92	0.93	0.95	0.97	0.98	0.99	0.99	1.00	1.00
0.5	1.00	0.97	0.92	0.90	0.88	0.90	0.92	0.96	0.97	0.98	0.99	1.00	1.00
0.6	1.00	0.95	0.88	0.85	0.82	0.86	0.89	0.94	0.96	0.97	0.98	0.99	1.00
0.7	1.00	0.92	0.81	0.78	0.76	0.81	0.86	0.92	0.95	0.96	0.97	0.99	1.00
0.8	1.00	0.84	0.72	0.69	0.70	0.76	0.82	0.89	0.93	0.95	0.97	0.99	1.00
0.9	1.00	0.70	0.60	0.59	0.62	0.71	0.78	0.87	0.92	0.94	0.96	0.98	1.00
$\sin^2 \theta$	1.000	0.962	0.862	0.800	0.500	0.308	0.200	0.100	0.059	0.038	0.027	0.010	0.002
$\pi \sin^2 \theta$	3.142	3.021	3.708	2.513	1.571	0.967	0.628	0.314	0.185	0.121	0.085	0.031	0.008

Note: Boundary lines delineate regions of 98%, 95%, and 90% irradiance uniformity

Performance Considerations for Uniform Source Specifications

Workshop Agenda (All times in MDT)

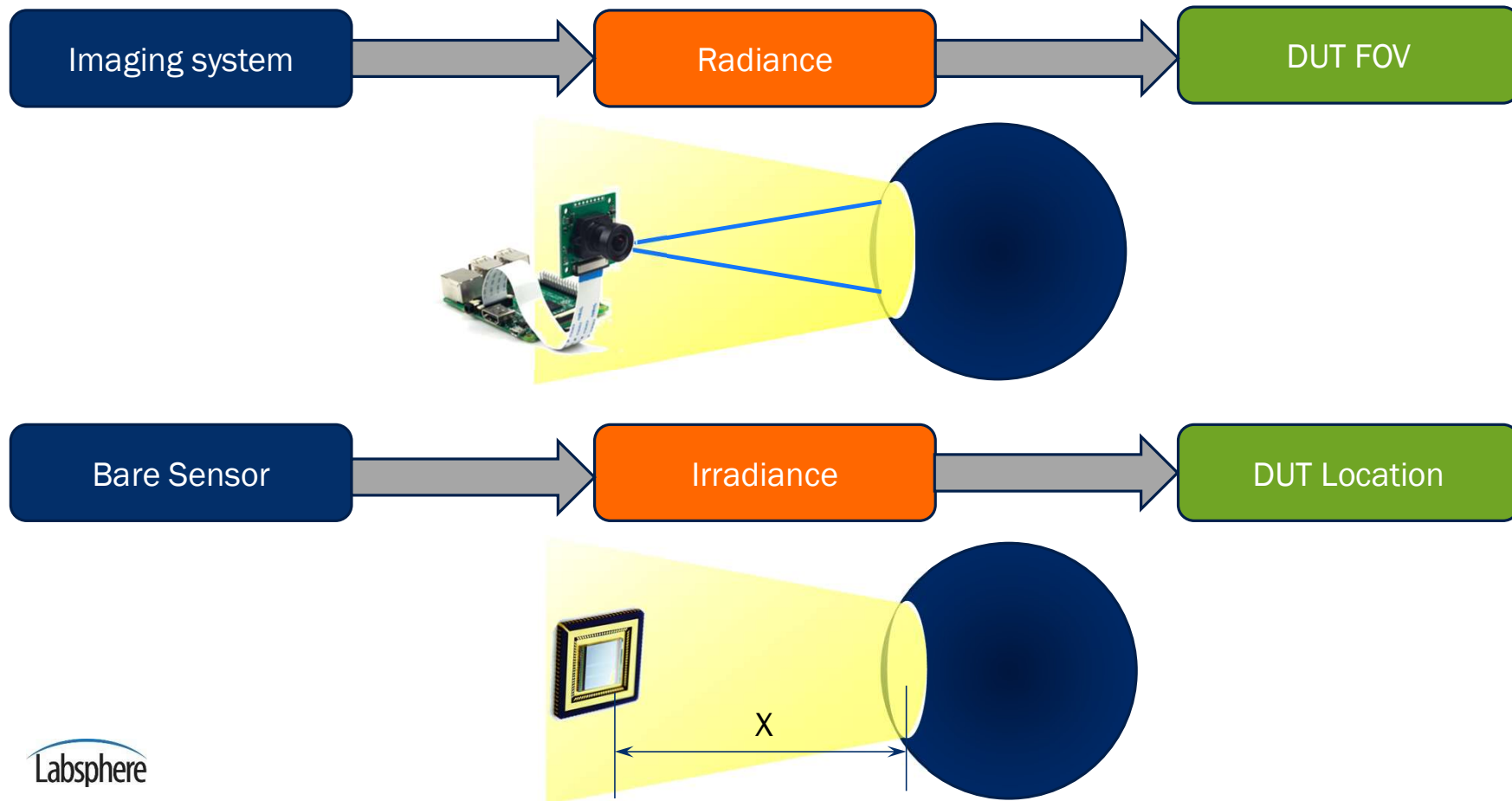
- ▶ 0730-0840 Sphere Theory and Applications (Durell)
- ▶ 0840-0910 Uniform Source Tutorial (Durell)
- ▶ 0910-0920 Sphere Calibrations (Durell)
- ▶ 0920-0930 (Virtual) Coffee Break
- ▶ **0930-1010 Considerations for Uniform Source Specifications (Scharpf)**
- ▶ 1010-1020 Commercial considerations (Scharpf)
- ▶ 1020-1040 NASA GLAMR Case Study (Brendan McAndrew, NASA GSFC)
- ▶ 1040-1050 If time permits: Uniform Source Case Studies (Durell)

Performance Considerations for Uniform Source Specifications

- ▶ Imaging v. Sensor Applications
- ▶ Size requirements
- ▶ Uniformity
- ▶ Output levels
 - ▶ Adjustability
 - ▶ Min/Max
- ▶ Spectral requirements
 - ▶ In-band
 - ▶ Spectral shape
 - ▶ Color temperature
- ▶ Stability
- ▶ Accuracy/Uncertainty

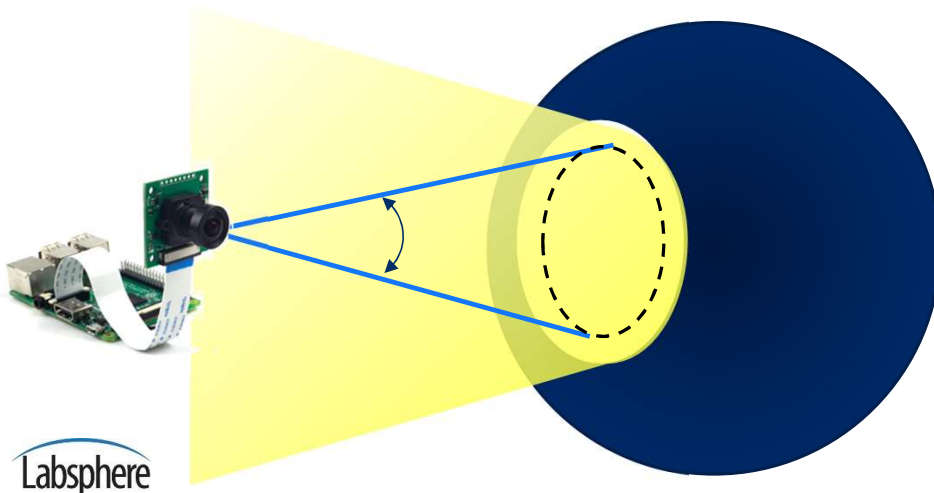


DUT: Imaging Device or Bare Sensor?



Sphere Design for Imaging Device

- ▶ Port dia. Is based on FOV
 - ▶ Determine DUT location
 - ▶ Calculate dia at sphere location
 - ▶ FOV set to < 90% of port Dia.
- ▶ Use Radiance Requirement to determine Flux



Design Steps

Define FOV

Calculate Exit Port
Dia.

Define Sphere Dia
with $f < 5\%$

Calculate Required
Flux, ϕ_i

$$L = \frac{\phi_i}{\pi A_s} \frac{\rho_0}{1 - \rho_0(1 - f)}$$

Sphere Design for Bare Sensor

► Define Irradiance at DUT Location

► Iterate on D_{sphere} , D_{port}

► Constraints:

- $f < 5\%$
- Uniformity at sensor

► Calculate Required Flux

Object Diameter a/D	0.09	0.10	0.20	0.25	0.50	0.75	1.00	1.50	2.00	2.50	3.00	5.00	10.00
0.1	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00
0.2	1.00	1.00	0.99	0.99	0.98	0.98	0.99	0.99	1.00	1.00	1.00	1.00	1.00
0.3	1.00	0.99	0.98	0.97	0.96	0.96	0.97	0.98	0.99	1.00	1.00	1.00	1.00
0.4	1.00	0.99	0.96	0.94	0.92	0.93	0.95	0.97	0.98	0.99	1.00	1.00	1.00
0.5	1.00	0.97	0.92	0.90	0.88	0.90	0.92	0.96	0.97	0.98	0.99	1.00	1.00
0.6	1.00	0.95	0.88	0.85	0.82	0.86	0.89	0.94	0.96	0.97	0.98	0.99	1.00
0.7	1.00	0.93	0.81	0.78	0.76	0.81	0.86	0.92	0.95	0.96	0.97	0.99	1.00
0.8	1.00	0.84	0.72	0.69	0.70	0.76	0.82	0.89	0.93	0.95	0.97	0.99	1.00
0.9	1.00	0.70	0.60	0.59	0.62	0.71	0.78	0.87	0.92	0.94	0.96	0.98	1.00
$\sin^2 \theta$	1.000	0.962	0.862	0.800	0.500	0.308	0.200	0.100	0.059	0.038	0.027	0.010	0.002
$\tau \sin^2 \theta$	3.142	3.021	3.708	2.513	1.571	0.967	0.628	0.314	0.185	0.121	0.085	0.031	0.008

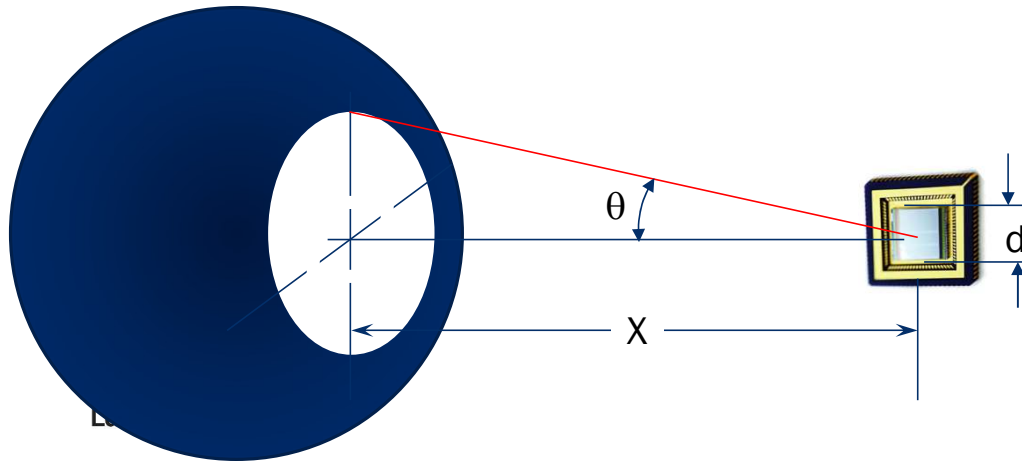
Design Steps

Define Irradiance at DUT

Iterate to calculate port Dia., Sphere Dia

Sphere Dia with $f < 5\%$

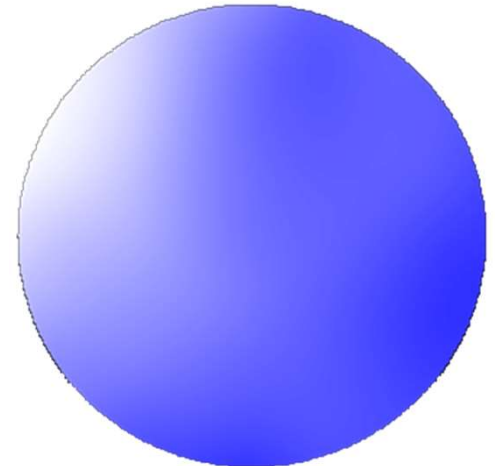
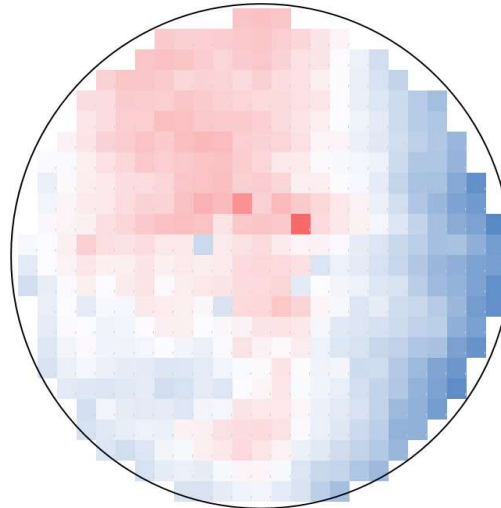
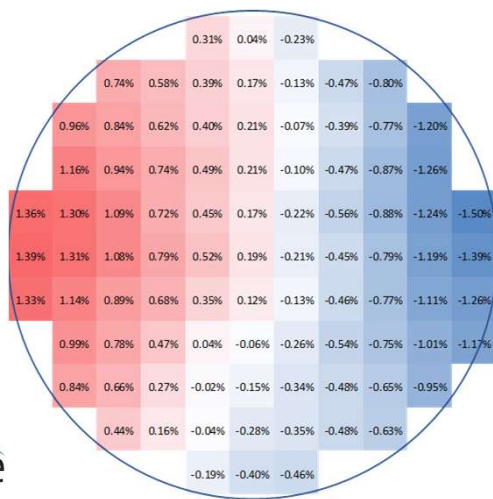
Calculate Required Flux



$$E = \frac{\phi_i}{A_s} \frac{\rho_0}{1 - \rho_0(1 - f)} \sin^2 \theta$$

Uniformity Requirements

- ▶ Define the uniformity calculation
- ▶ Will the uniformity map data be used for correction?
- ▶ Define the required uniformity map resolution
- ▶ Quantify the required uniformity
- ▶ Uniformity for each operating condition?



Quantifying Uniformity

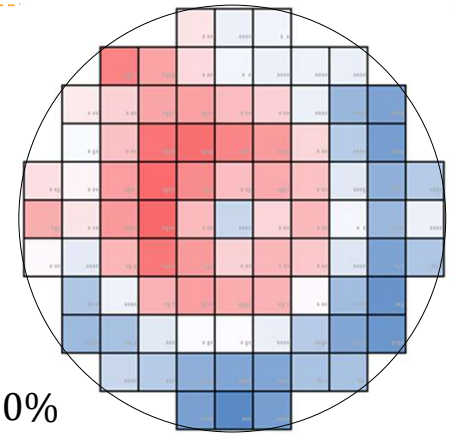
- ▶ Divide source area into sub-elements

1. Max Deviation Method $U_{Max\ Deviation} = \frac{Min}{Max} \times 100\%$

2. Mean Deviation Method $U_{Mean\ Deviation} = 1 - \frac{\left(\frac{Max - Min}{2}\right)}{Mean} \times 100\%$

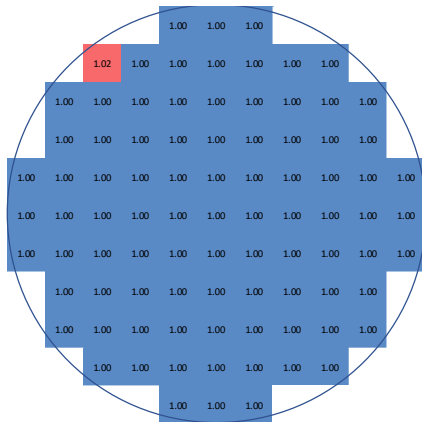
3. Deviation Method $U_{Deviation} = 1 - \frac{(Max - Min)}{Mean} \times 100\%$

4. CoV Method $U_{COV} = \left(1 - \frac{\sigma_L}{\bar{L}}\right) \times 100\%$

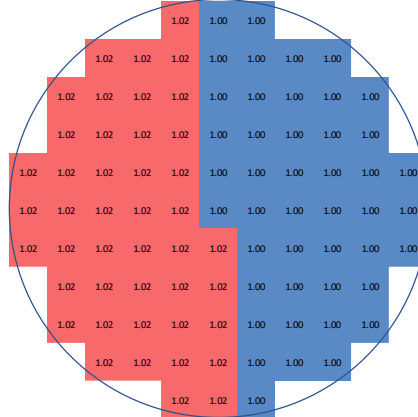


Uniformity Examples

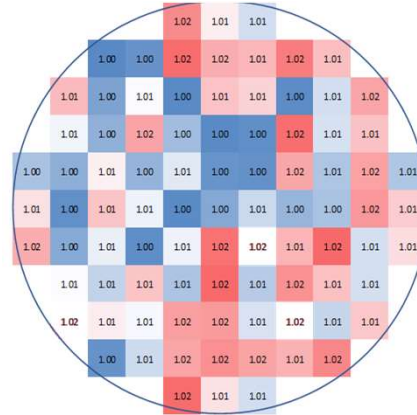
2% Spike



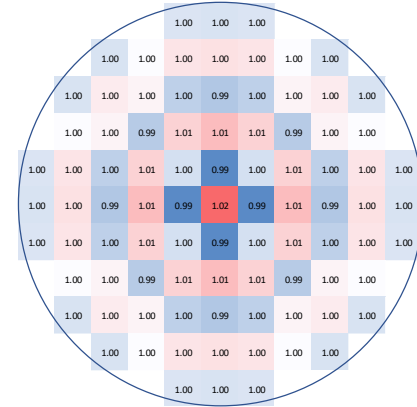
2% Split



2% Random

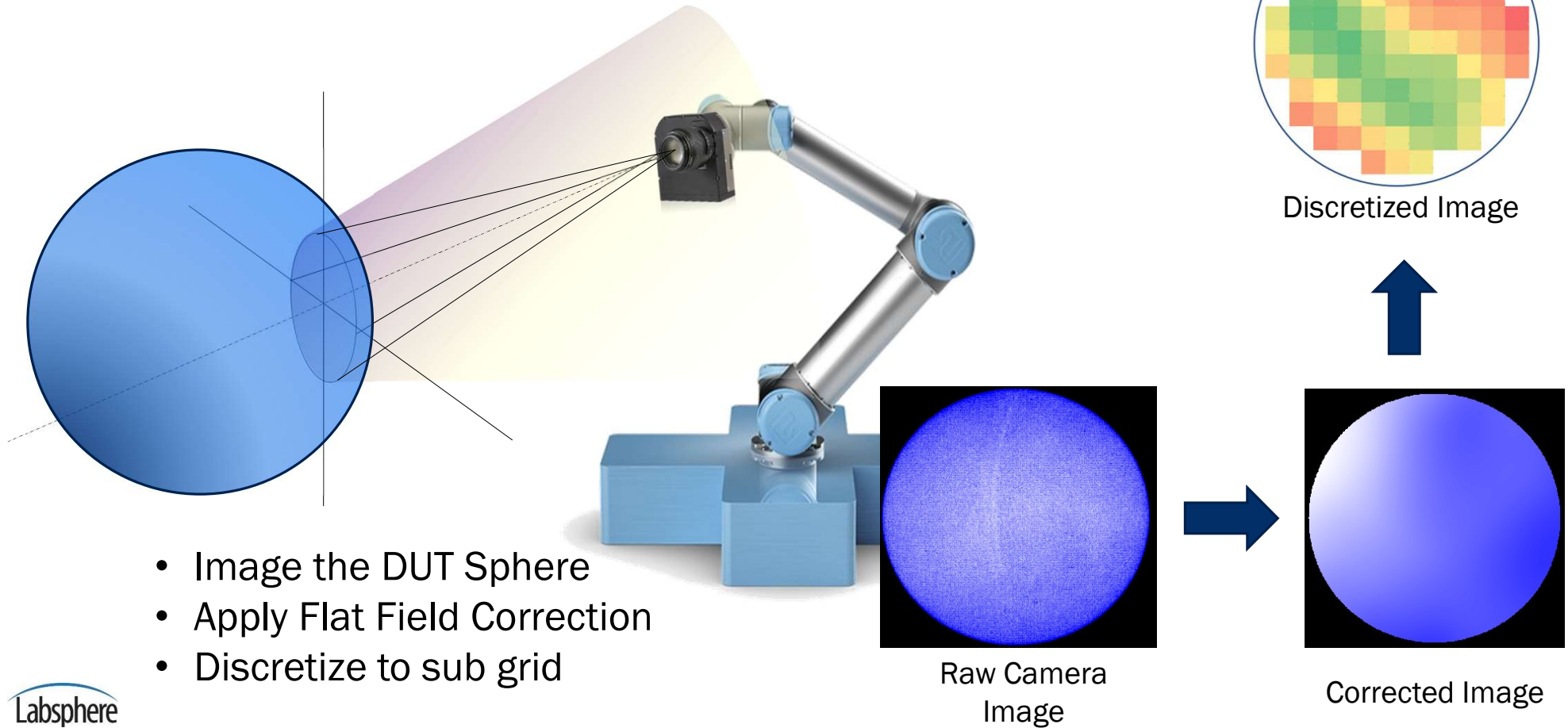


2% Damped

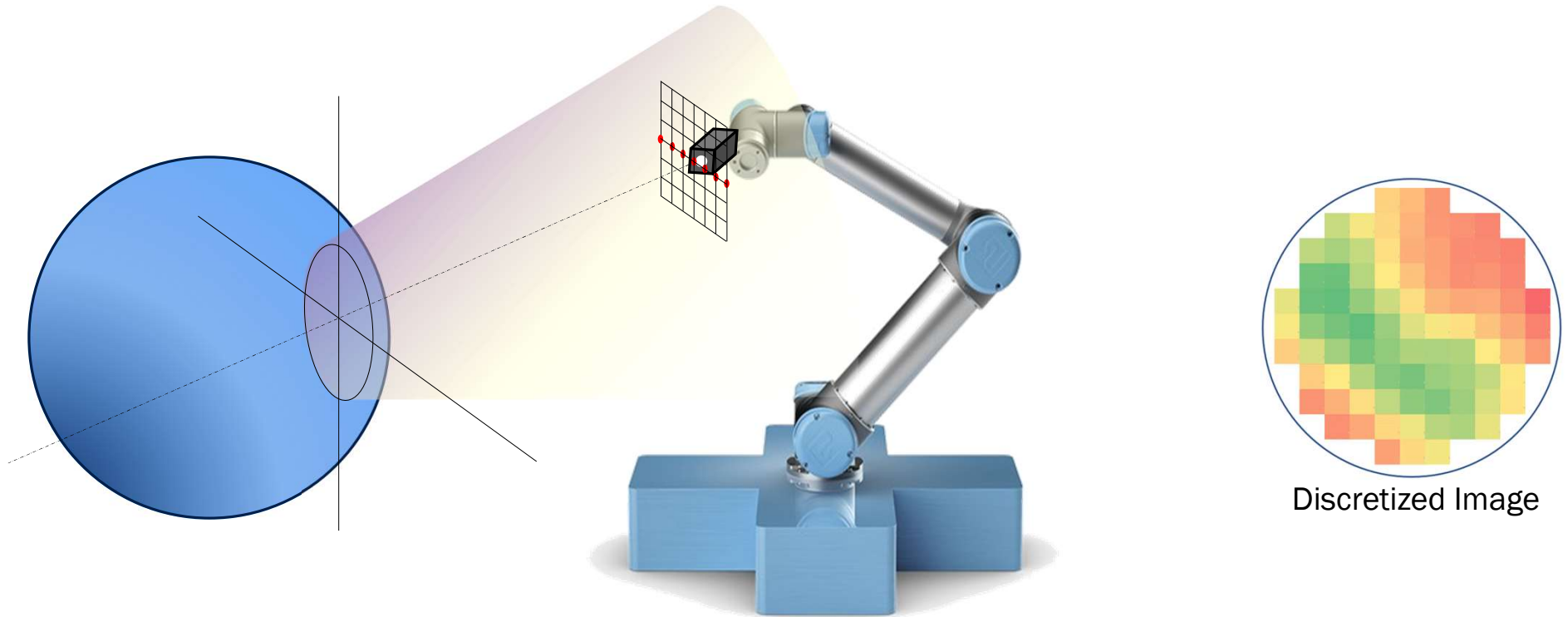


Max Deviation	98.0%	98.0%	98.1%	96.7%	$\frac{L_{min}}{L_{max}}$
Deviation Method	98.0%	98.0%	98.0%	96.7%	$1 - \frac{L_{max} - L_{min}}{L_{mean}}$
Mean Deviation	99.0%	99.0%	99.0%	98.3%	$1 - \frac{(L_{max} - L_{min})/2}{L_{mean}}$
(CoV)	99.8%	99.0%	99.4%	99.5%	$1 - \frac{s_L}{L_{mean}}$

Measuring Radiance/Luminance Uniformity



Measuring Irradiance Uniformity



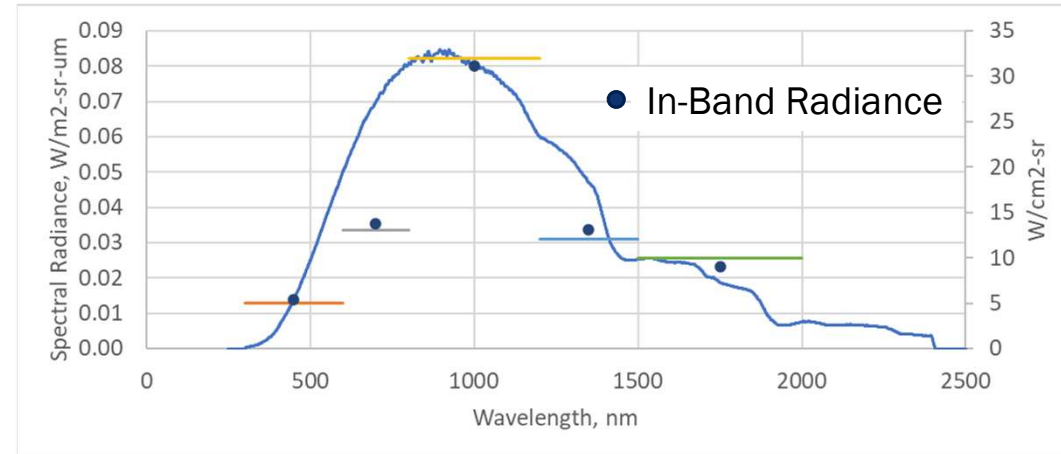
- Define Sensor distance
- Define spacing at sensor location
- Traverse sensor in xy-plane

Defining Sphere Output Requirements

- ▶ Spectral or In-Band?
- ▶ Units
- ▶ Min/Max Levels
- ▶ Dynamic Range
- ▶ Spectral Shape
 - ▶ Blackbody
 - ▶ Smoothness – Peak-peak variation, RMS,
- ▶ Wavelength Range

Defining Sphere Output: In-Band integrated values

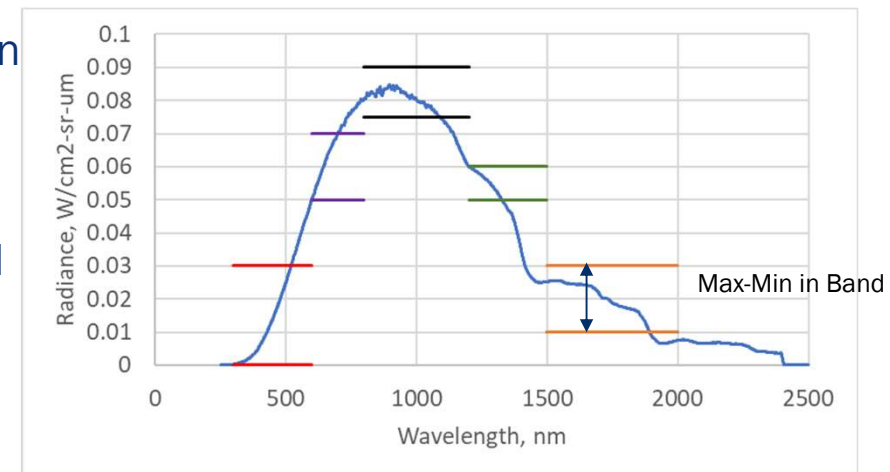
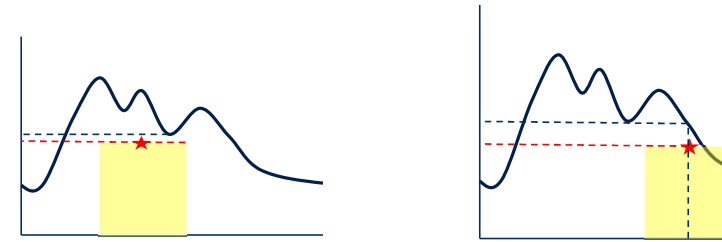
- ▶ Define the bands
 - ▶ Define the units
 - ▶ Radiance: $[\text{W}/\text{m}^2\text{-sr}]$, $[\text{photons}/\text{s}\text{-m}^2\text{-sr}]$
 - ▶ Irradiance $[\text{W}/\text{m}^2]$
- ▶ Define the requirements
 - ▶ All in-band requirements to be met simultaneously?
 - ▶ In-band requirements to be met individually?
 - ▶ Integrated value in band must exceed minimum
 - ▶ Integrated value in band must fall between min and max



Band, nm	Min Radiance, W/cm2-sr
300 - 600	5
600 - 800	13
800 - 1200	32
1200 - 1500	12
1500 - 2000	10

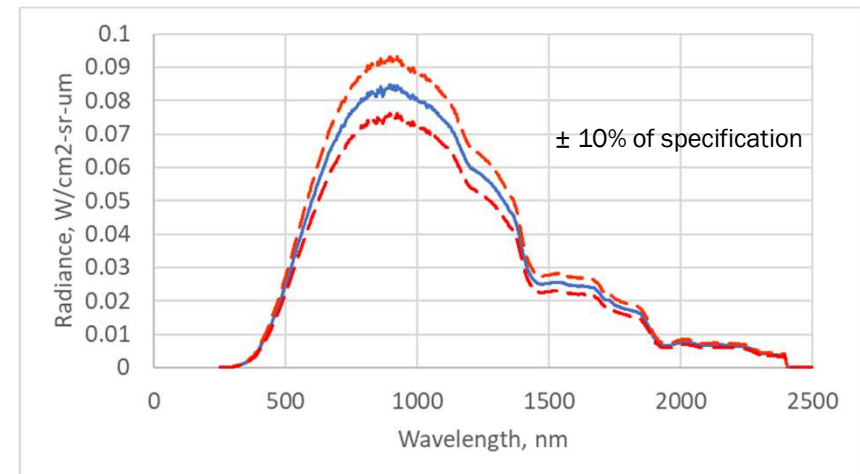
Defining Sphere Output: Spectral Levels

- ▶ Define the Units
 - ▶ Radiance: $[\text{W}/\text{m}^2\text{-sr-}\mu\text{m}]$, $[\text{photons}/\text{s-m}^2\text{-sr-}\mu\text{m}]$
 - ▶ Irradiance $[\text{W}/\text{m}^2\text{-}\mu\text{m}]$
- ▶ Within the Band of interest:
 - ▶ All spectral values to exceed the minimum within band
 - ▶ The level at the center wavelength should exceed the value prescribed for the band
 - ▶ All spectral values to fall between min and max within range
 - ▶ All in-band requirements to be met simultaneously
 - ▶ In-band requirements to be met individually
 - ▶ Value must exceed min at center wavelength in band
- ▶ Can the sphere output filtered?



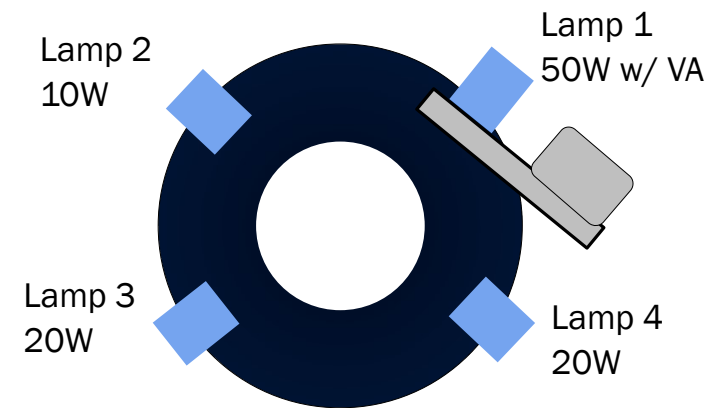
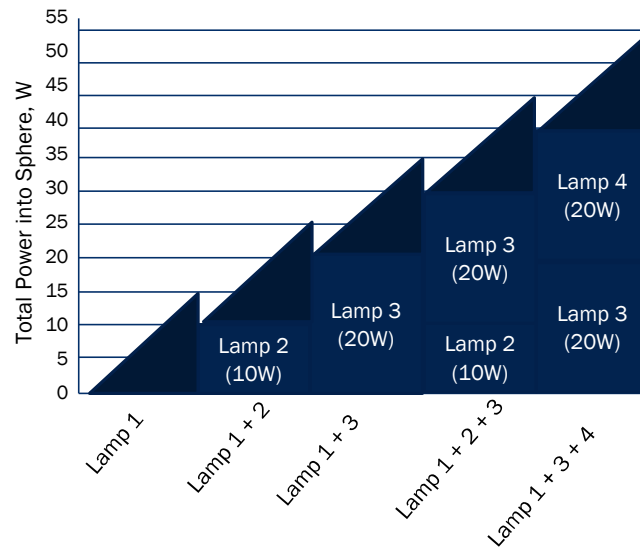
Defining Output Levels: Spectral Shapes

- ▶ Provide a tolerance across the band:
 - ▶ All values to be within $\pm 10\%$ of nominal value within the band.
- ▶ Provide an RMSE value:
 - ▶ The RMSE between the measured and prescribed spectrum shall be $< 5\%$
- ▶ Blackbody curve
 - ▶ Provide CCT
 - ▶ Provide allowable deviation as defined above



Defining Output Levels: Adjustability

- ▶ What is dynamic range of system?
 - ▶ Define the min and max levels
- ▶ Is continuous adjustability required?

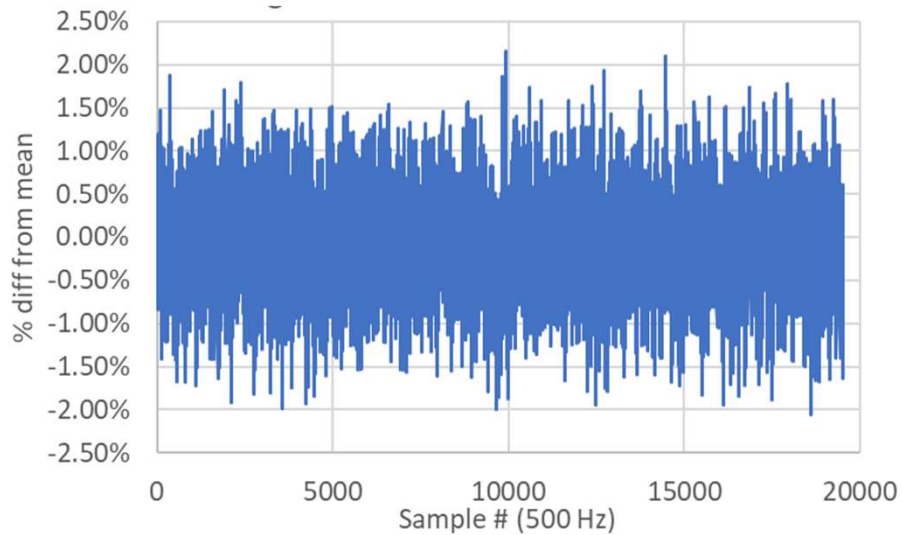


Sphere Output: Defining Required Stability

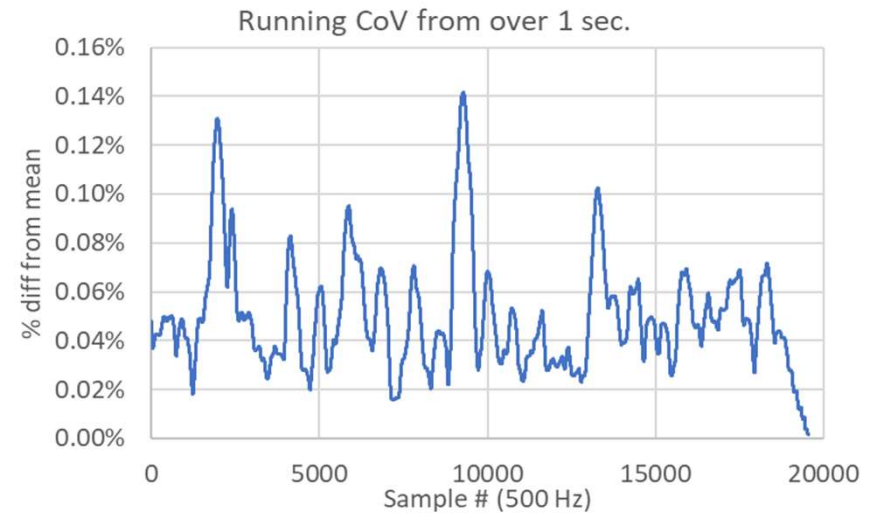
- ▶ Define the use case:
 - ▶ Will it run for hours at one condition?
 - ▶ Sweep through dynamic range?
 - ▶ Is time required to capture output on the order of minutes, hours, days?
- ▶ What is the effect of stability on the DUT measurement?
- ▶ Define the stability requirement
 - ▶ Max allowable peak-peak variation
 - ▶ %RMS over time period (CoV)
- ▶ Short-Term or Long-Term requirements?
- ▶ CCT Stability?
- ▶ Define sampling frequency for system validation testing

Sphere Output: Xe Lamp Stability Example

Peak-Peak $\sim \pm 2\%$



CoV < 0.15%



Sphere Output: Accuracy and Uncertainty

- ▶ Accuracy – Closeness of a measured value to the true value
- ▶ Uncertainty – parameter, associated with the result of a measurement, that characterizes the dispersion of values that could reasonably be attributed to the thing being measured*.
 - ▶ Refers to the measurement at a given instance in time, NOT the instrument.
- ▶ Uncertainty values are provided with the calibration of the system.
 - ▶ Measured spectral radiance
 - ▶ Detector response
 - ▶ Uniformity

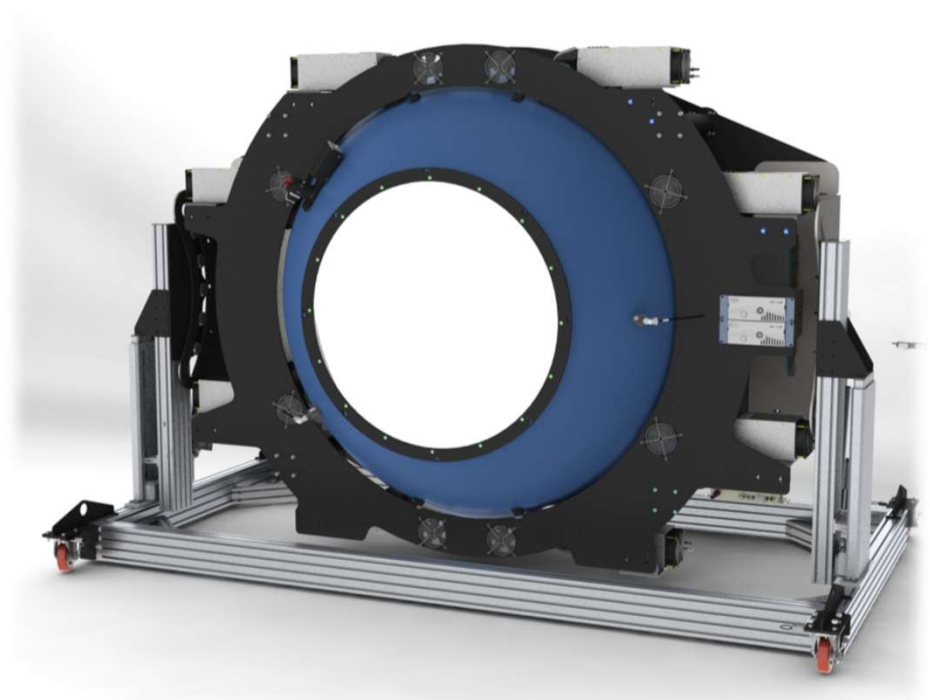
Commercial Considerations for Uniform Source Specifications

Workshop Agenda (All times in MDT)

- ▶ 0730-0840 Sphere Theory and Applications (Durell)
- ▶ 0840-0910 Uniform Source Tutorial (Durell)
- ▶ 0910-0920 Sphere Calibrations (Durell)
- ▶ 0920-0930 (Virtual) Coffee Break
- ▶ 0930-1010 Considerations for Uniform Source Specifications (Scharpf)
- ▶ **1010-1020 Commercial considerations (Scharpf)**
- ▶ 1020-1040 NASA GLAMR Case Study (Brendan McAndrew, NASA GSFC)
- ▶ 1040-1050 If time permits: Uniform Source Case Studies (Durell)

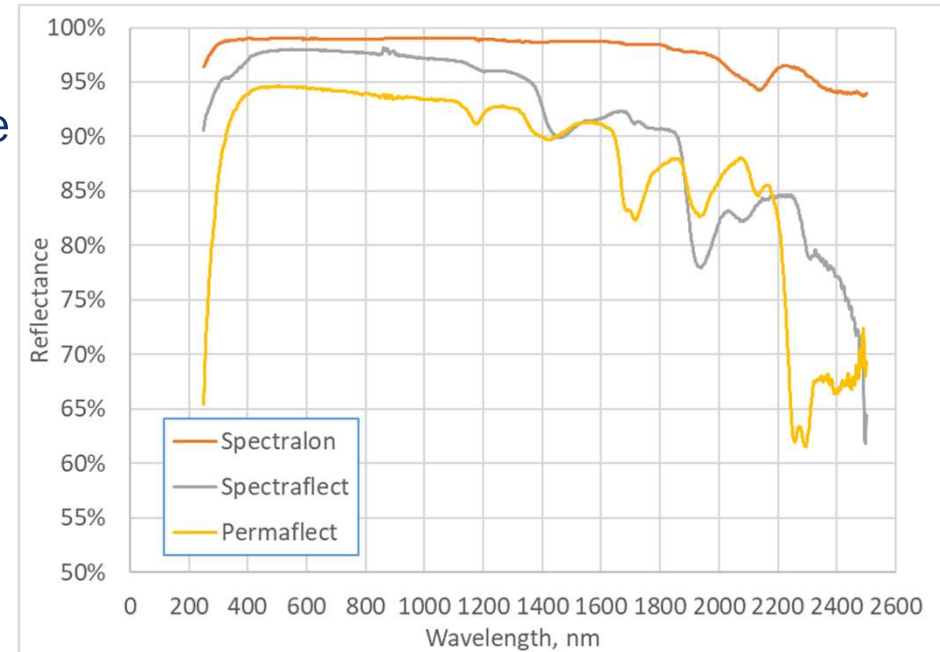
Commercial Considerations

- ▶ Sphere Material
- ▶ Sphere Size
- ▶ Spectral Requirements
- ▶ Source Types
 - ▶ Plasma, Xe, LED, Lasers, QTH, UV/IR
- ▶ Spectral Range
- ▶ Dynamic Range
- ▶ Lead Time
- ▶ Uncertainty
- ▶ Mechanical features
- ▶ Stability and Control
- ▶ Software Modifications
- ▶ Theory v. Practice
- ▶ Thermal Control
- ▶ Environmental



Cost Drivers – Materials

- ▶ Spectralon (machined PTFE)
 - ▶ Needed for UV, and high reflectance in blue
 - ▶ Space applications – vacuum baked
- ▶ Spectraflect (spray coating)
 - ▶ General purpose
 - ▶ Wide spectral range
- ▶ Permaflect
 - ▶ Cleanable
 - ▶ Harsh environments
- ▶ Gold
 - ▶ IR applicaitons

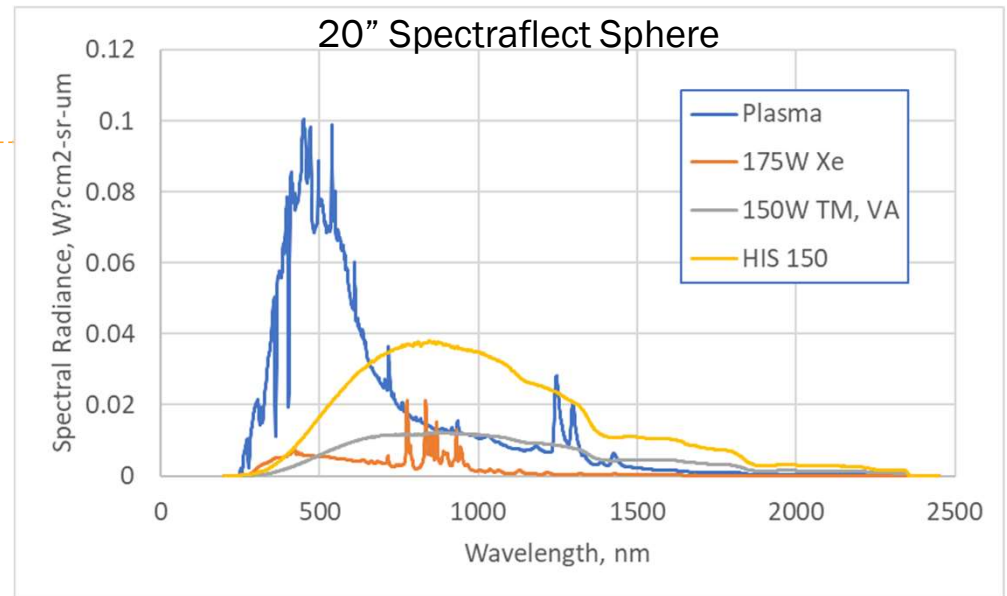


Cost Drivers: Spectral Requirements

- ▶ Spectral Matching
 - ▶ Requires multiple lamp types
 - ▶ Tight specifications may require filters on sources
- ▶ High Blue Content
 - ▶ Multiple plasma
 - ▶ LEDs
- ▶ High NIR (>1200nm)
- ▶ Simultaneously meeting levels in multiple bands

Cost Drivers: Lamp Types

- ▶ Xenon \$\$\$\$
- ▶ Plasma \$\$\$
- ▶ Lasers \$\$ - \$\$\$
 - ▶ May require de-speckler
- ▶ LED \$\$\$
- ▶ External QTH \$\$
- ▶ Internal QTH \$



Cost Considerations

- Each lamp typically requires a dedicated power supply
- High # of lamps:
 - increases electronics rack complexity
 - increases power consumption and complexity
 - May introduce thermal issues and control
- Continuous Adjustability requires multiple lamps

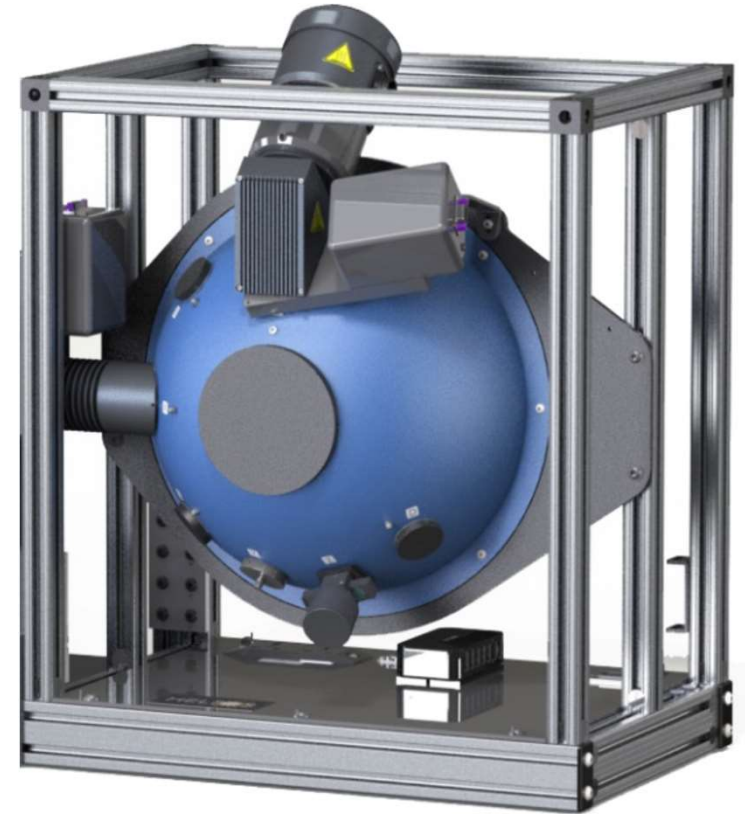
Cost Drivers: Spectral Range

- ▶ Wide ranges may span multiple detector ranges:
 - ▶ Si 320nm – 1100nm
 - ▶ InGaAs 900 – 1700nm, or 700 – 2600nm
- ▶ Filters on detectors for specific bands
 - ▶ Rolloff
 - ▶ Cutoff
 - ▶ Leakage
- ▶ Wide spectral range may require multiple lamp types



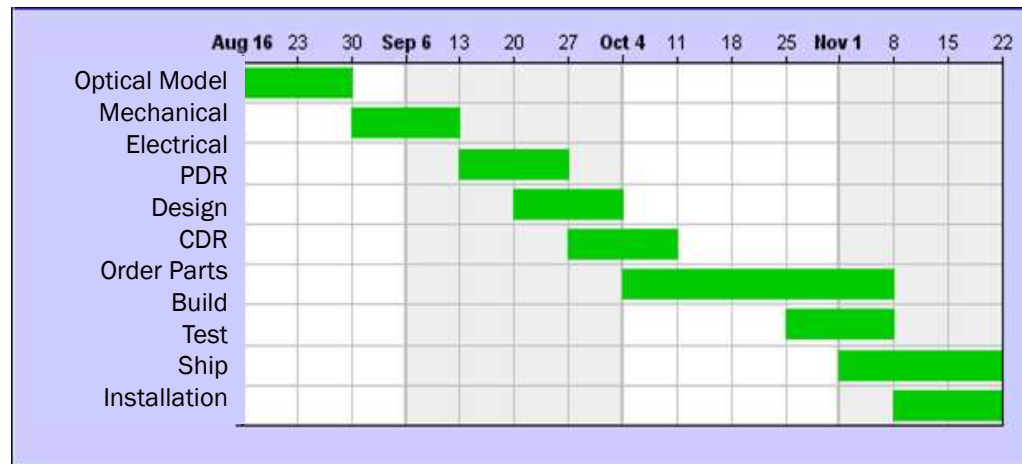
Cost Drivers: Dynamic Range

- ▶ Requires multiple lamps
- ▶ Continuous adjustability
 - ▶ Variable Attenuator (VA) required
- ▶ May require apertures on detectors
 - ▶ May require additional calibrations for each configuration



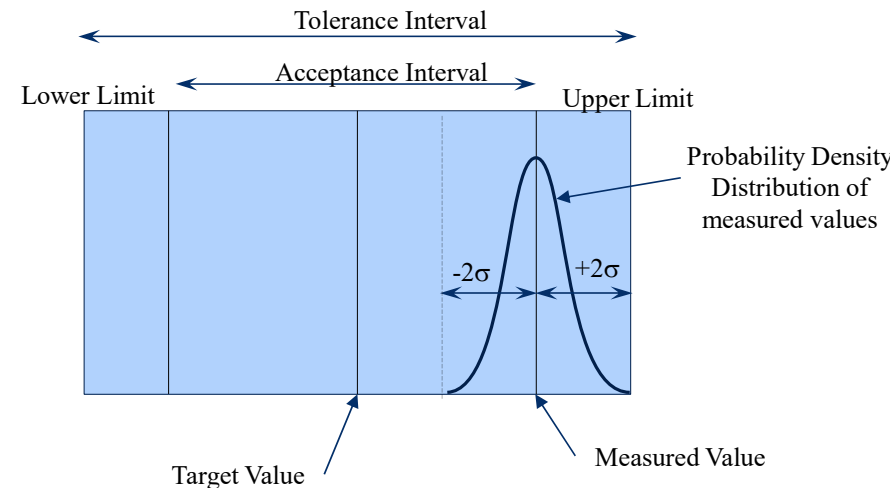
Cost Drivers: Schedule and Lead Time

- ▶ Standard systems – quickest delivery
- ▶ Custom
 - ▶ add time for NRE and custom parts
- ▶ Advanced Custom
 - ▶ NRE, Custom parts, Design Reviews
- ▶ Special components
 - ▶ Gold coating
- ▶ Special calibrations
- ▶ 3rd party components
- ▶ 3rd party calibration
- ▶ Special Filter Orders
- ▶ Shipment: Air/Land
- ▶ Installation and Training
- ▶ Readiness of installation site



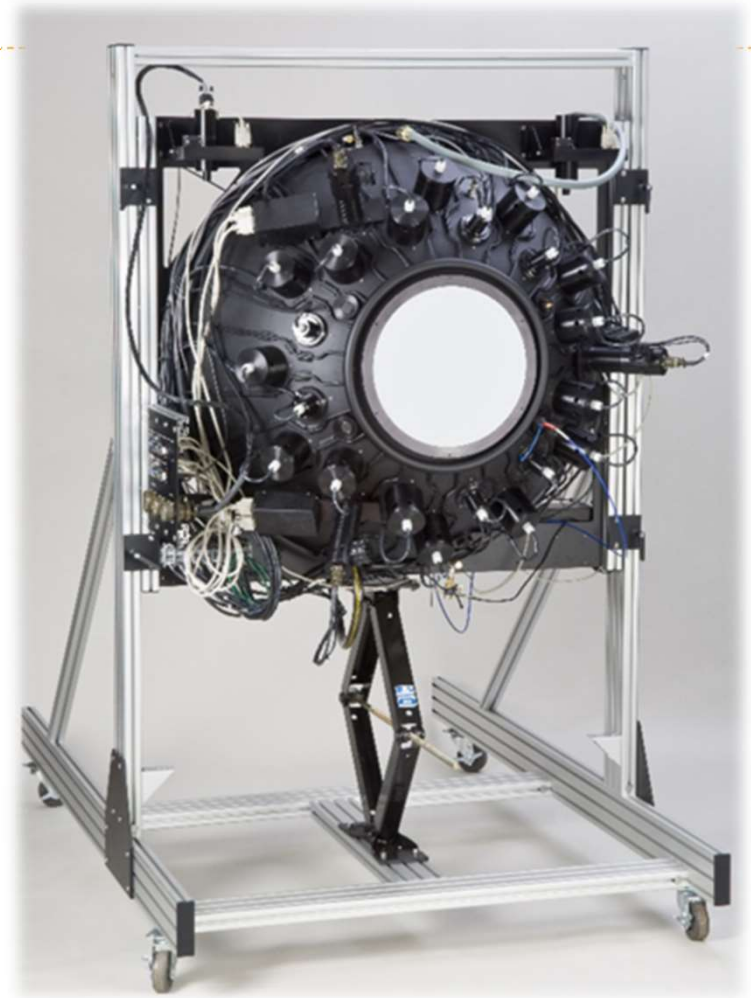
Commercial Considerations: Uncertainty

- ▶ Uncertainty is on the measurement at the time of the measurement
- ▶ Standard Calibrations include uncertainty estimates
- ▶ Custom Calibrations/Measurements
 - ▶ Add ~ 1-2 weeks of NRE for uncertainty
- ▶ New systems and components that require uncertainty
 - ▶ Add ~ 1-4 weeks of NRE for uncertainty
 - ▶ May require additional measurements and characterization of new components



Mechanical Features that Add Cost

- ▶ Height Adjustment
- ▶ Additional Port reducers
- ▶ Rotation
- ▶ Alignment features
- ▶ Shutters
- ▶ Clean Room Requirements
- ▶ Cable Lengths
- ▶ Thermal management
 - ▶ Fans
 - ▶ Insulation
- ▶ Weight Limitations
- ▶ Space Constraints

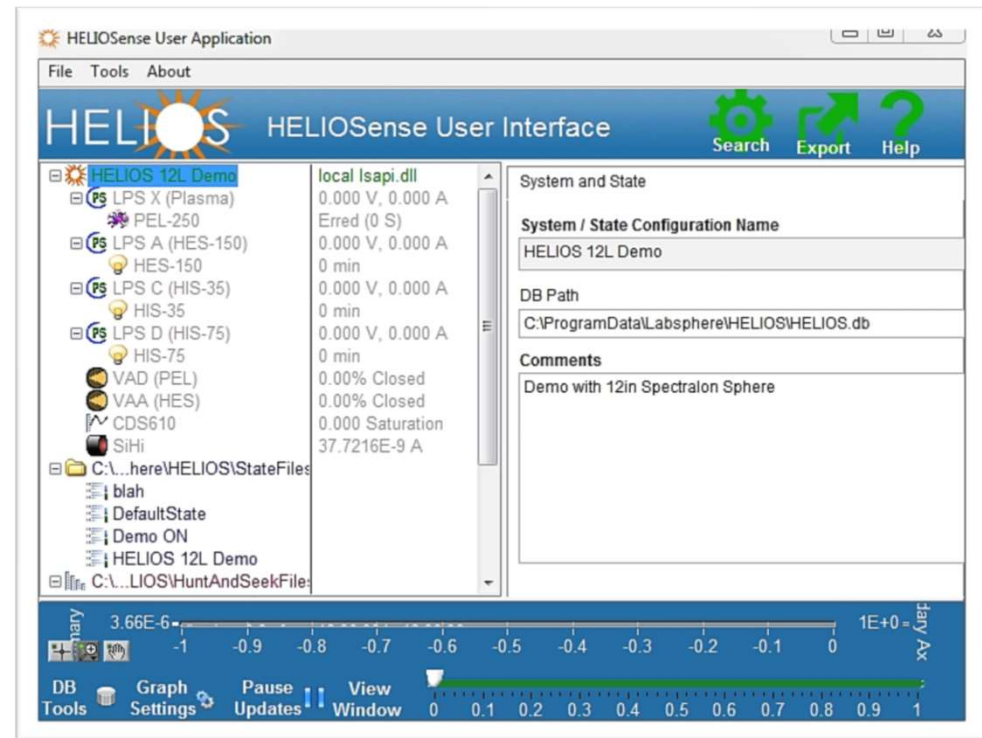


Commercial Considerations: Stability and Control

- ▶ Stability needs to be defined over a time period
- ▶ QTH lamps are very stable ($\sim 0.04\%$ P-P)
- ▶ Plasma Stability
 - ▶ Short term (<1 min) $\pm 0.4\%$ P-P, 0.3% CoV
 - ▶ Long Term (> 1 min) $\pm 0.4\%$ P-P, 0.2% CoV
 - ▶ Long Term ~ 30 min w/ 15 plasma lamps: $< \pm 0.7\%$ P-P, 0.2% CoV
 - ▶ Improved stability with multiple lamps
- ▶ Improved stability over baseline requires additional control

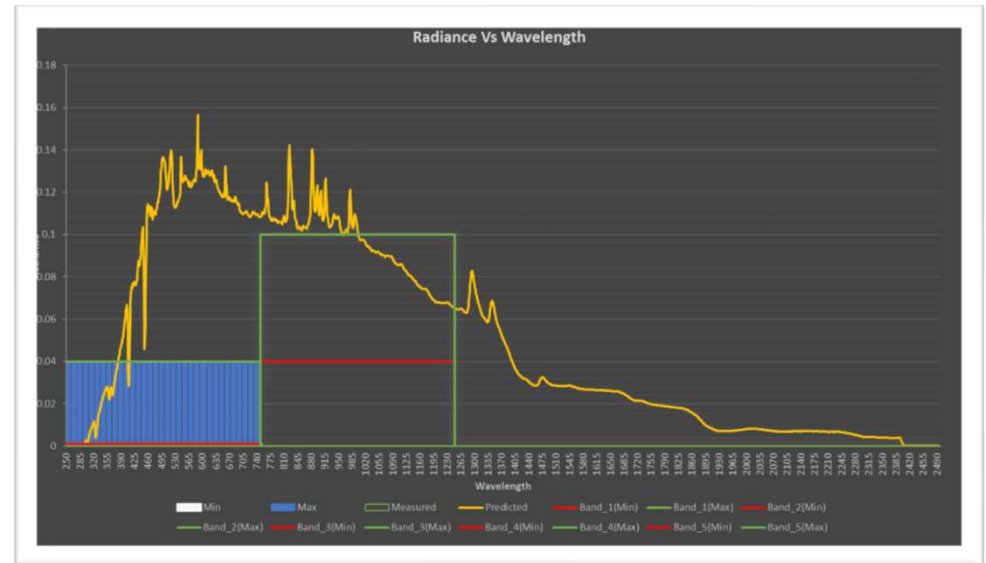
Commercial Considerations: Software

- ▶ SDK available
- ▶ NRE required for:
 - ▶ Addition of new features
 - ▶ Addition of new hardware controls
 - ▶ SDK development assistance
 - ▶ Integration to automated system



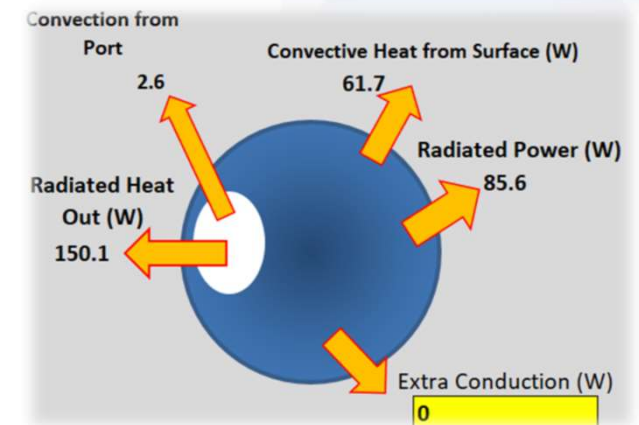
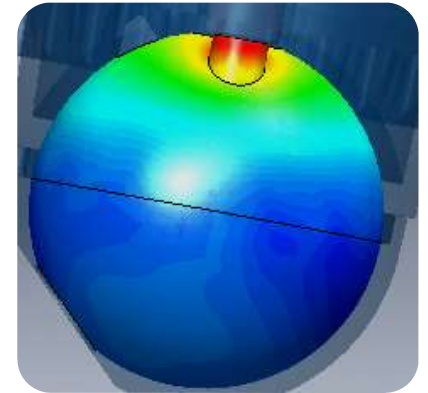
Commercial Considerations: Theory v. Practice

- ▶ QTH Lamp supply is constantly changing
- ▶ LED Specifications and Binning
- ▶ Material variations
- ▶ Machine Tolerances
- ▶ Always deal with design tradeoffs
 - ▶ Prioritize the Requirements



Commercial Considerations: Thermal Control

- ▶ Many lamps turns sphere into an oven
- ▶ Thermal limits on coating:
 - ▶ Spectraflect ~ 100C
 - ▶ Spectralon ~ 400C
- ▶ Labsphere models for bulk temperature of sphere
- ▶ Detailed analysis using CFD
- ▶ Cooling methods
 - ▶ External fans
 - ▶ Directed fans/blowers
 - ▶ Cooled filters
 - ▶ Liquid cooling



Commercial Considerations: Environmental

- ▶ Harsh Environments

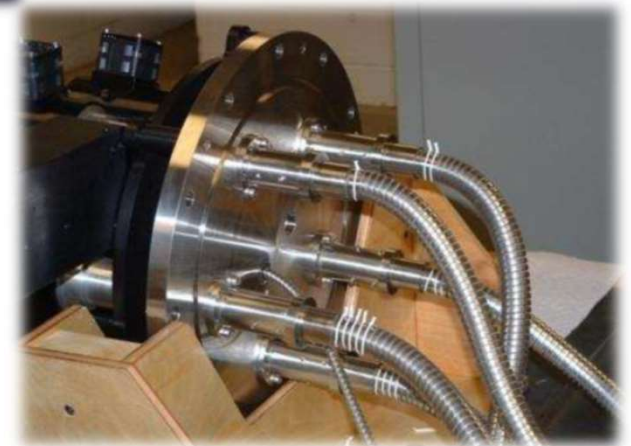
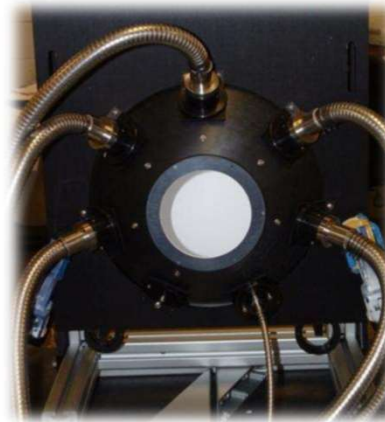
- ▶ Tarmac
- ▶ Flight Lines
- ▶ Desert
- ▶ On-board

- ▶ Clean Rooms

- ▶ Material constraints
- ▶ ISO Class

- ▶ Vacuum

- ▶ Material limitations (outgassing)
- ▶ Instrument and lamp changes
- ▶ Fiber feeds
- ▶ Optical Fibers
- ▶ Bulkhead design



Commercial Considerations: Summary

▶ Cost Adders

- ▶ Custom
- ▶ High output
- ▶ Large spheres
- ▶ UV
- ▶ Thermal management
- ▶ Spectral Monitoring
- ▶ Vacuum or environmental

▶ Complexity

- ▶ Spectral matching
- ▶ Matching multiple spectral ranges
- ▶ Tight specifications
- ▶ Extended range

▶ Cost controls

- ▶ Prioritize the requirements
- ▶ Identify areas for flexibility
- ▶ Use standard product when possible
- ▶ Quantify specs and define calculations prior to design
- ▶ Understand use case

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