

A General Approach to Lifting-Line Theory, Applied to Wings with Sweep

Jackson T. Reid

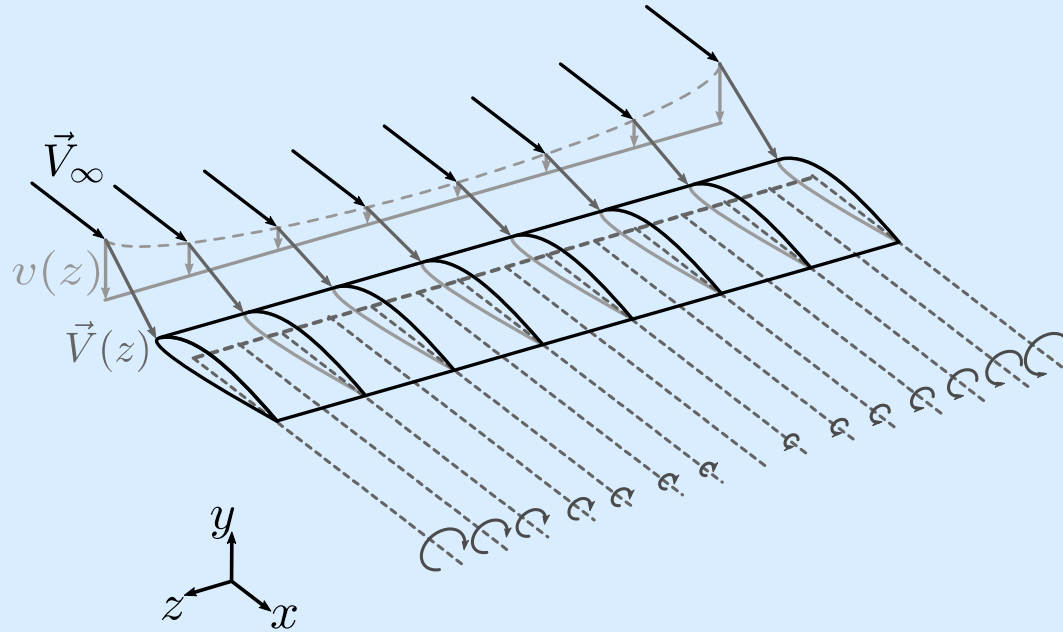
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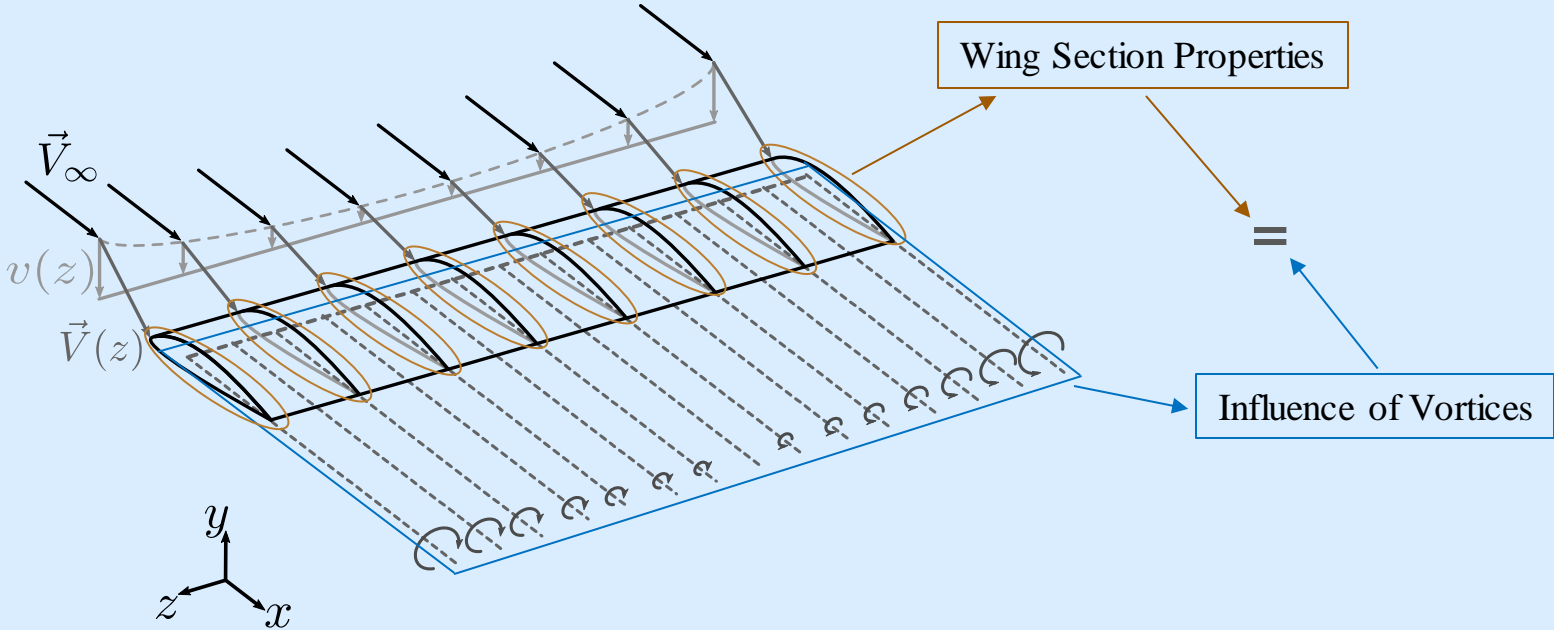
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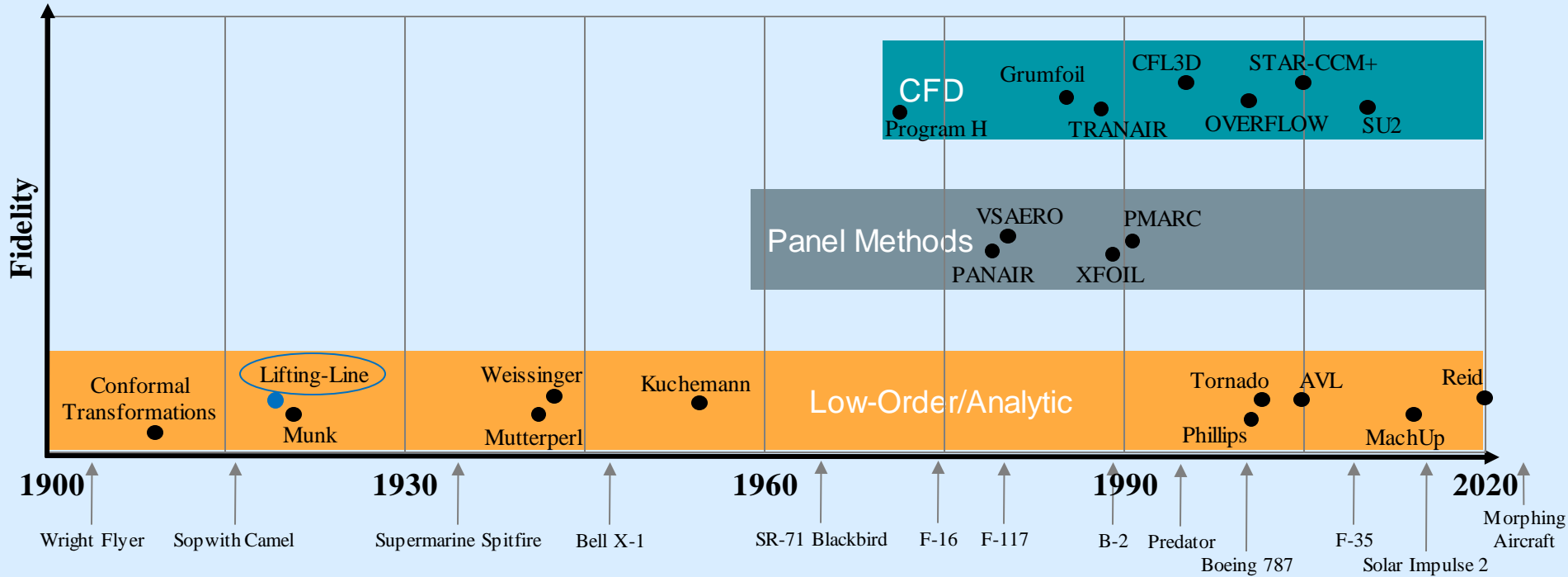
Lifting-Line Theory



Lifting-Line Theory

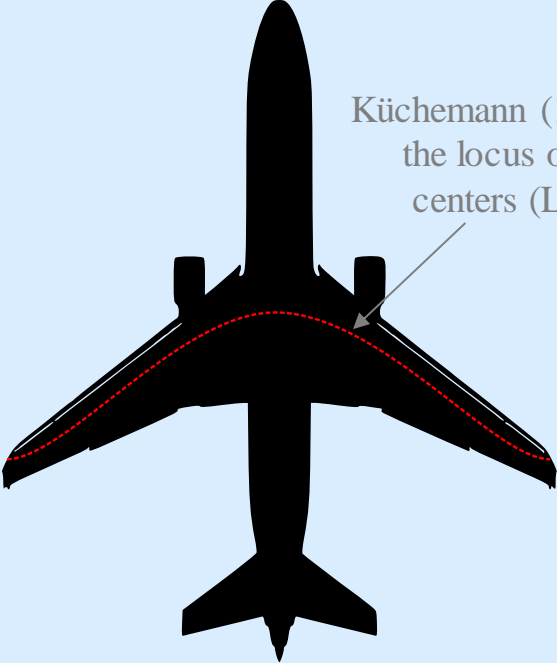
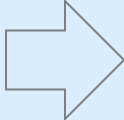
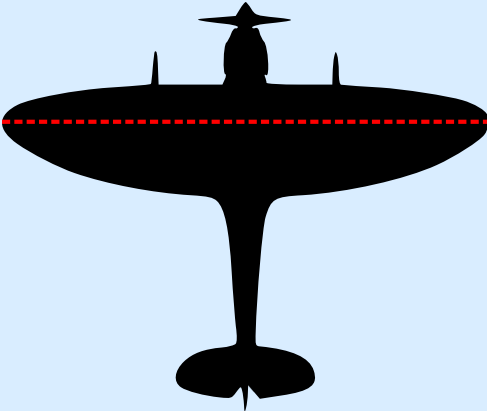


Aerodynamic Tools



Usefulness of Prandtl's Implementation

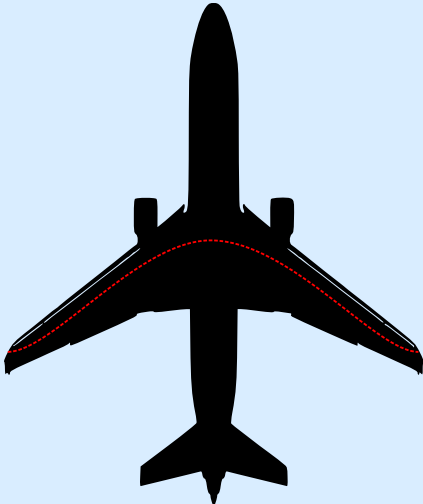
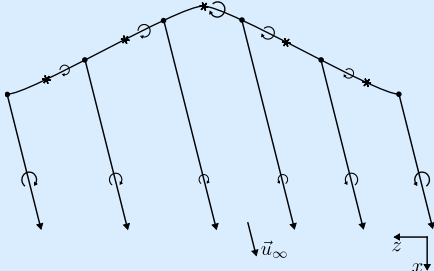
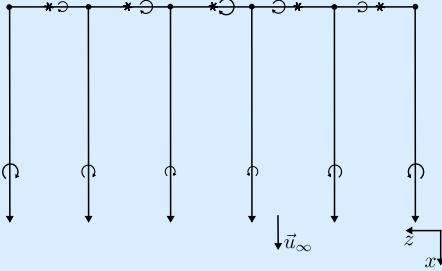
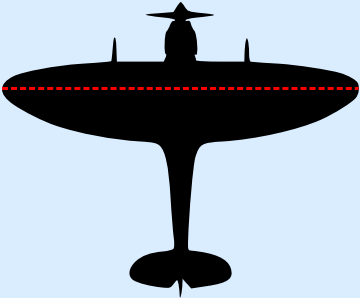
Prandtl's classical implementation was instrumental in the design of aircraft during WWII.



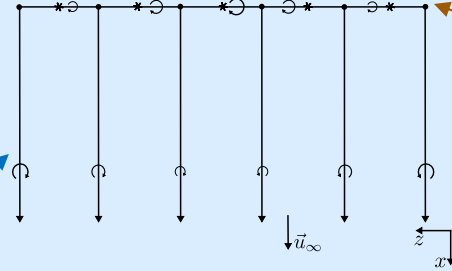
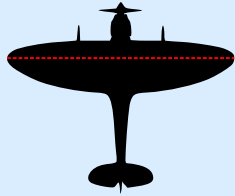
Küchemann (1956) modeled the locus of aerodynamic centers (LAC) for swept wings



Influence of Vortices

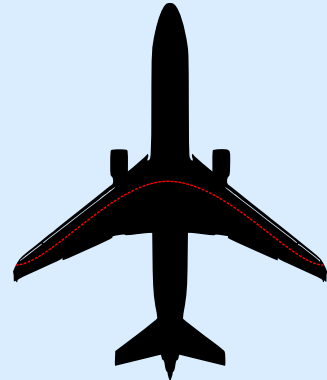
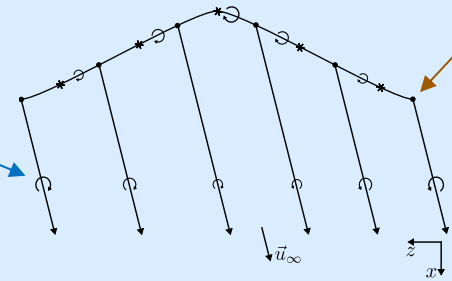


Influence of Vortices

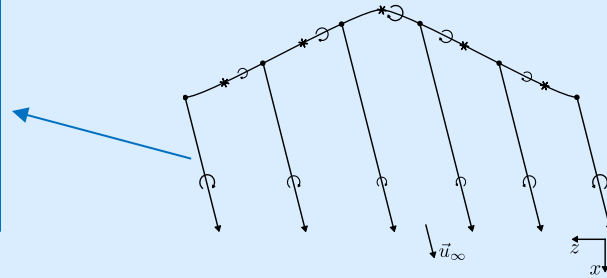
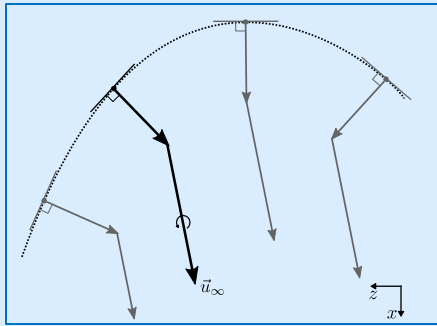


Influence is finite only if the bound vortex has **no curvature**

Influence is finite only if the trailing vortices are **perpendicular** to locus of aerodynamic centers

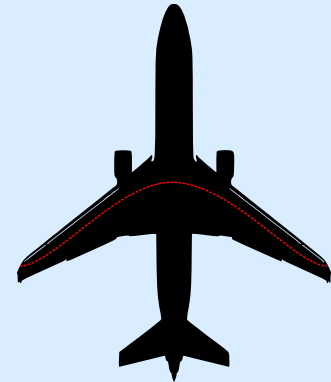


Influence of Vortices

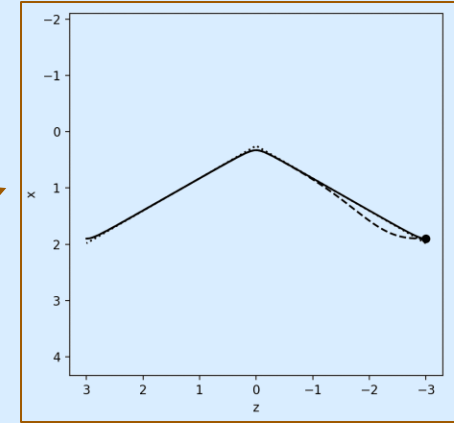
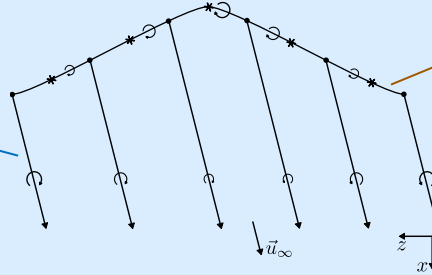
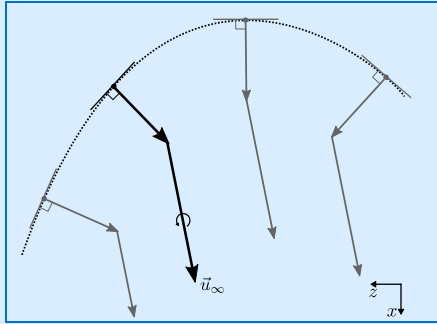


Jointed Trailing Vortices:

- Finite vortex segment perpendicular to LAC
- Semi-infinite vortex aligned with freestream



Influence of Vortices



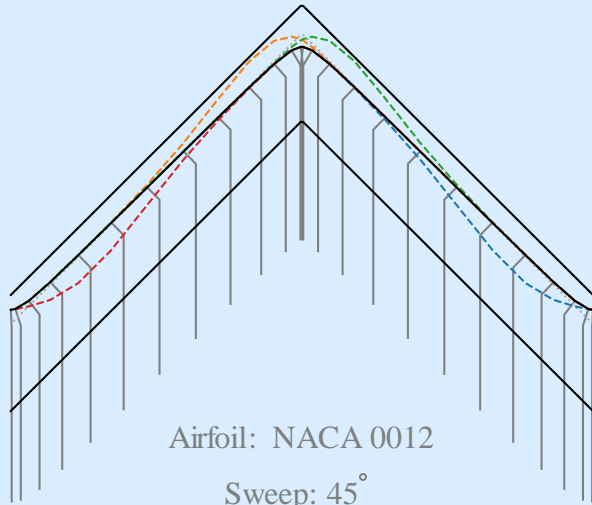
Jointed Trailing Vortices:

- Finite vortex segment perpendicular to LAC
- Semi-infinite vortex aligned with freestream

Effective Loci of Aerodynamic Centers:

- No concavity at control point
- Blend between tangent line and original LAC

General Implementation Accuracy



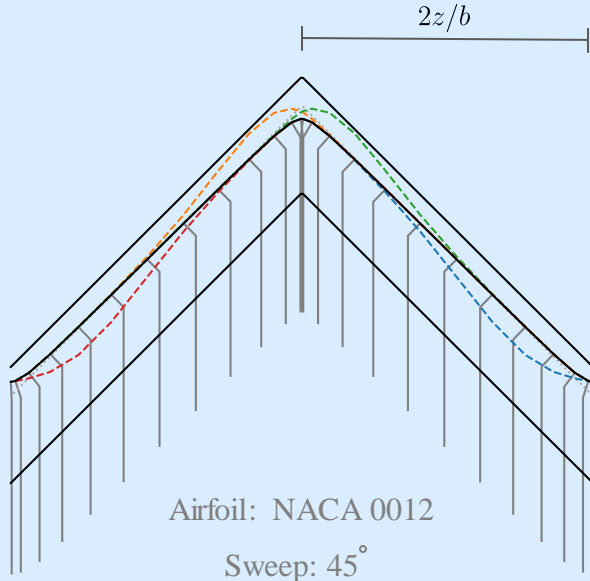
Airfoil: NACA 0012

Sweep: 45°

Aspect Ratio: 5

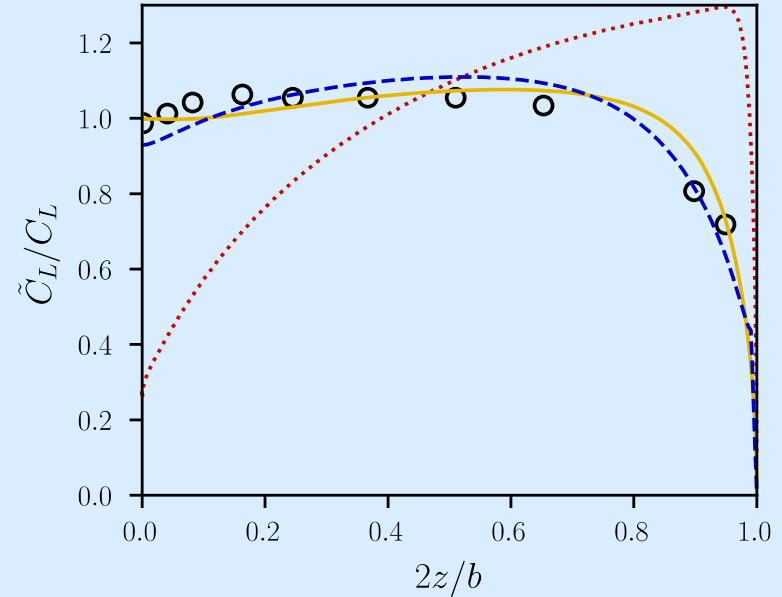
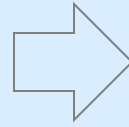
Taper Ratio: 1

General Implementation Accuracy



Aspect Ratio: 5

Taper Ratio: 1

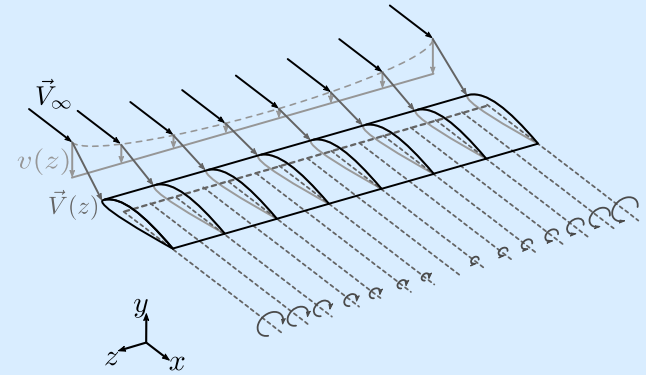
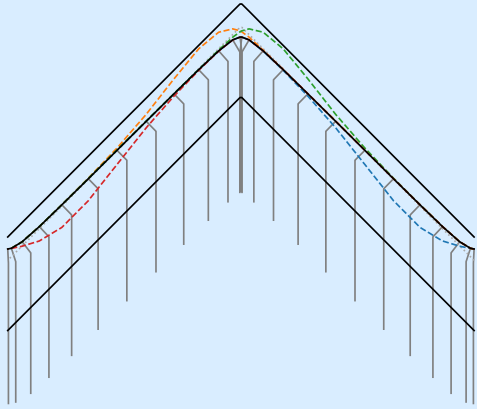


○ Experiment

⋯ Phillips' LL

— General LL

- - - PAN AIR



Thank You

For More Information:

Reid, Jackson T. and Hunsaker, Douglas F., “*A General Approach to Lifting-Line Theory, Applied to Wings with Sweep*”, AIAA SciTech Forum and Exposition, January 2020,

<https://doi.org/10.2514/6.2020-1287>

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