

# Small Satellite Capability Analysis



## Translational Performance in Small Satellites

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## ▪ **Relate Satellite Size and Delta-V:**

- Using minimum observables (size/vol) to determine available delta-v
- Find relationships between total delta-v, satellite size, propulsion system % of volume

## What's the Point???

## ▪ **SSA Applications:**

- Characterize maneuvering capability of possible RSO threats

## ▪ **Combine with Other Sub-System Analyses:**

- Integrate studies of each system to make strong deductions about satellite capability based solely on size



## ▪ **Propulsion Systems Selected:**

- Cold Gas, and Monopropellant thrusters
- Electric and Bipropellant not considered due to volume and possible power restrictions

## ▪ **Satellite Mass in terms of System Components:**

- Define component metrics in terms of satellite size

$$m_{sat} = m_{str} + m_{plumb} + m_{thr} + m_{tank}$$

## ▪ **Delta-V Equation:**

- Determine satellite and fuel mass

$$\Delta V = I_{sp} g \ln \left( 1 + \frac{m_{fuel}}{m_{sat}} \right)$$



## Percentage of Sat Mass:

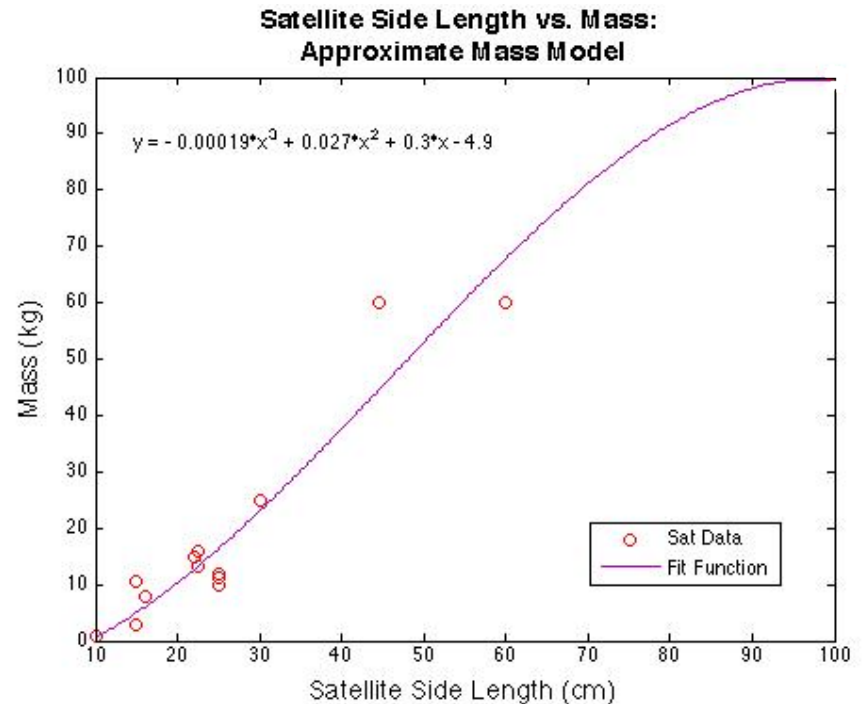
- Define structure mass as percentage of total sat mass:

$$m_{str} = P m_{sat}$$

Where: P= percentage of total mass  
 $m_{sat}$  = mass estimate of satellite

## Plot:

- Red dots show cataloged data from real satellites
- Line is best fit function used to estimate sat mass
- Structure mass selected as 20% of fit function based upon real sat data





## ▪ **Thruster Mass:**

$$m_{thr} = n_{thr} m_n$$

Where:  $n$  = number of thrusters  
 $m_n$  = mass per thruster

## ▪ **Cold Gas Valves:**

- Valve length is limiting factor for satellites below 15cm
- For rest of sat size range, valves chosen by increasing thrust

## ▪ **Monopropellant Hydrazine Valves:**

- Will not fit into less than 13cm satellite
- Can be considered beginning at 21cm where thrusters account for 25% of volume and 10-15% of satellite mass

## ▪ **Considerations:**

- Assumed 6 thrusters for this study (min for 3 translational DOF w/o attitude control)
- Minimum thrust levels may be an issue given environment

# Cold Gas/Monopropellant Valves: Figures

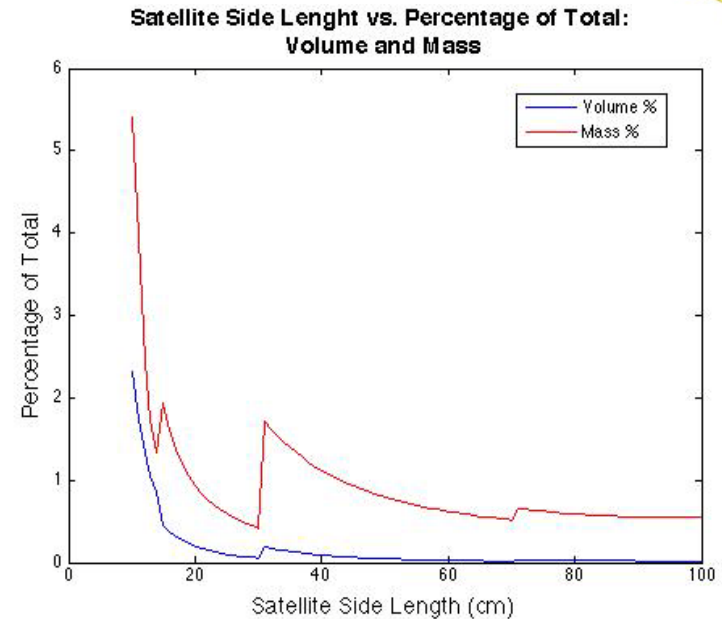
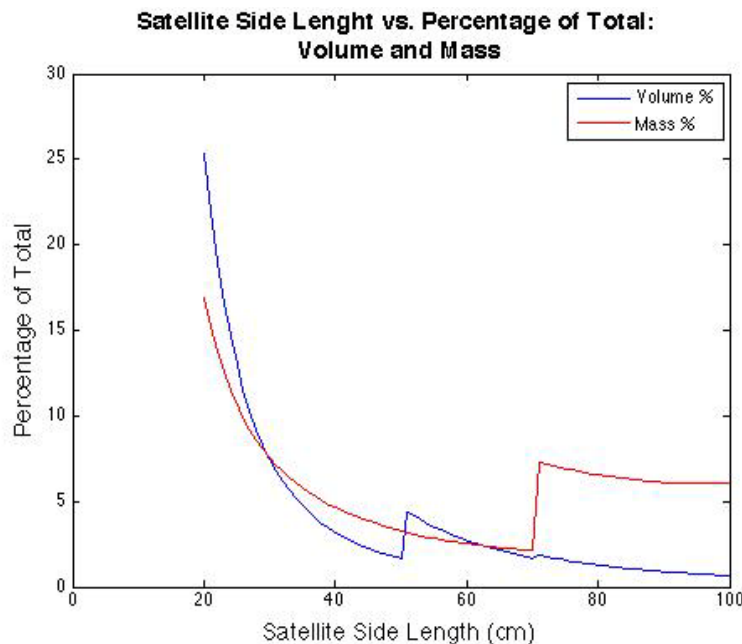


## ■ **Volume:**

- At CubeSat level valves are 2.5%
- Largest valves could fit cubesat at 13% of total volume

## ■ **Mass:**

- At CubeSat level 5.5% of total
- Larger than 15cm valve mass is below 2% of total



## ■ **Volume:**

- At 21cm valves are 25% of total
- <5% of total past 35cm size
- <2% of total past 70cm size

## ■ **Mass:**

- At 21cm valves are 17% of total
- Past 30cm <10% of total



$$m_{plumb} = n_{thr} \mu_{tube} l_{thr} + m_{reg}$$

Where:  $m_{reg}$  = mass of pressure regulation system

$n$  = number of thrusters

$\mu$  = linear density of tubing

$l$  = length of tube needed per thruster

▪ **Plumbing Volume = Tube Length x Cross-sectional Area**

- Add pressure regulator size specs (if necessary)

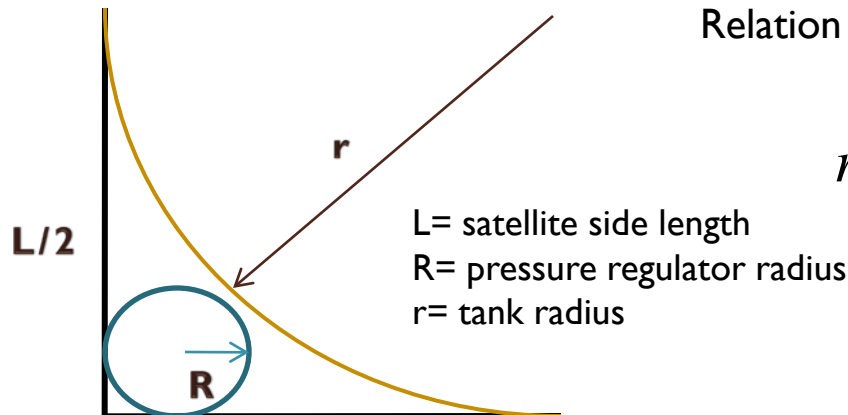
▪ **Pressure Regulator:**

- Determined by operating pressure

- Sizing considerations:

Regulator size may limit tank radius

Relation between regulator rad, tank rad & sat side:



$$r_{\text{tank}} \leq \frac{\sqrt{2L^2}}{2} - \sqrt{2a^2} - 2r_{\text{reg}}$$

$$a = r_{\text{reg}} - \sqrt{\frac{r_{\text{reg}}^2}{2}}$$



### ▪ **Selected System Percentage:**

- Subtract volume of other system components from selected percent of total volume to obtain total tank volume:

$$V_{\text{tank}} = p_{\text{sys}} V_{\text{sat}} - V_{\text{sys}}$$

Where:  $p$  = propulsion system volume percentage  
 $V_{\text{sys}}$  = volume of plumbing and thrusters  
 $V_{\text{sat}}$  = total satellite volume

### ▪ **Tank Thickness:**

- Radius found from total volume
- Thickness estimated using stress equation for sphere
- Defines tank mass

$$\sigma_y = \frac{2pr}{t} \times SF$$

SF = safety factor (2.0)  $p$  = tank pressure  
 $t$  = tank thickness  $r$  = tank radius



# Tank Mass/Volume Continued

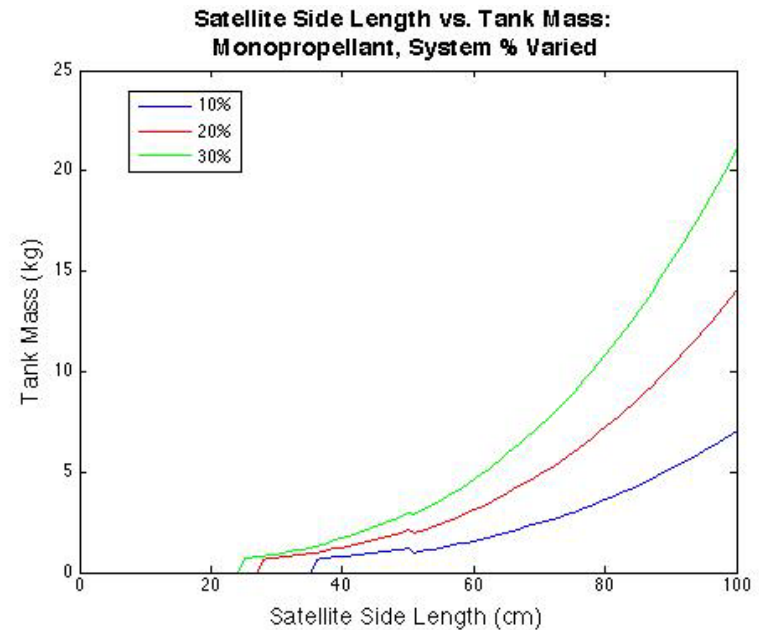
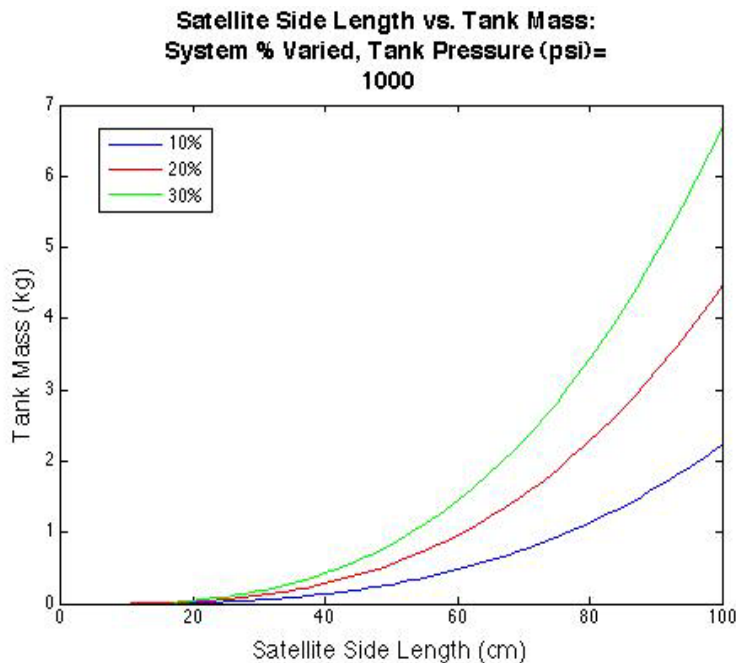


## ▪ **Cold Gas Tank:**

- Increase by 10x in pressure results in 10x increase in mass
- Reduction in fuel volume with increase in pressure
- Volume increases linearly with system percent

## ▪ **Monopropellant Tank Mass:**

- Takes into account mass of pressurant and diaphragm
- 85% of tank volume available for fuel



# Component Comparison to Dry Mass



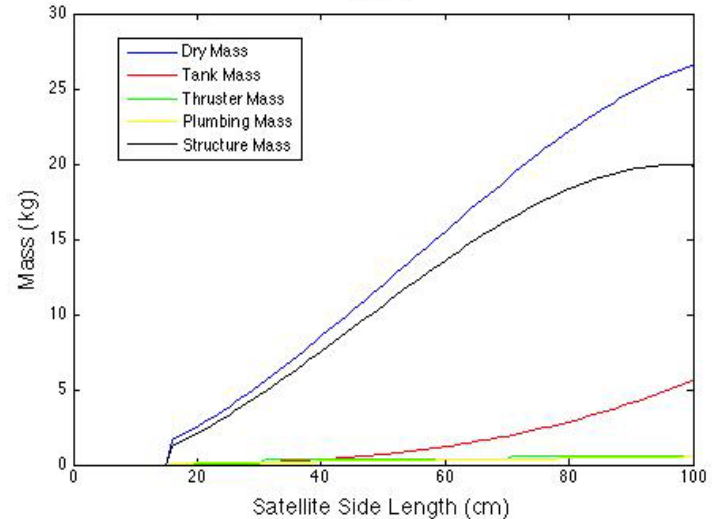
## ▪ **Low Pressure (100's psi):**

- Tank, thrusters, plumbing relatively same, low percentage of total

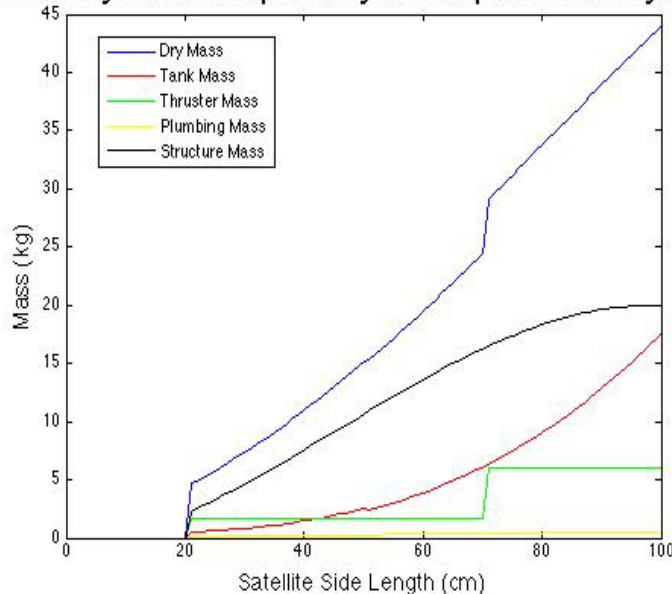
## ▪ **High Pressure (>1000 psi):**

- Tank begins to dominate dry mass
- Shift in min sat size

Satellite Dry Mass and Propulsion System Component Mass:  
Cold Gas Tank Pressure (psi)=  
1000



Satellite Dry Mass and Propulsion System Component Mass: Hydrazine



## ▪ **Monopropellant (System at 25%)**

- Tank and thrusters account for >50% of total mass
- Plumbing mass very small... almost negligible near 100cm



▪ **Fuel Volume:**

- Equal to total tank volume minus tank material volume

▪ **Cold Gas:**

- Entire volume assumed to be available for fuel
- Mass defined as:

$$m_{fuel} = \frac{P_t V_t}{RT}$$

Where: P= tank pressure  
 V= fuel volume  
 R= gas constant  
 T= tank temperature

▪ **Mass Example:**

- Cold gas at 1000 psi
- Maximum mass ~35kg

▪ **Volume Example:**

- Largest volume ~450 liters
- Very small reduction in vol with increase in tank pressure

▪ **Monopropellant:**

- Only 85% of volume available for fuel
- Mass found using total fuel volume and density
- Nearly 10x larger mass than cold gas

## Delta-V Results: Unrestricted Plots



- **100 Psi:**

- Max delta-v  $\approx$  100 m/s
- Max sat mass  $\approx$  25 kg

- **1000 Psi:**

- Max delta-v  $\approx$  500 m/s
- Max sat mass  $\approx$  70 kg

- **10,000 Psi:**

- Max delta-v  $\approx$  900 m/s
- Max sat mass  $\approx$  400 kg!

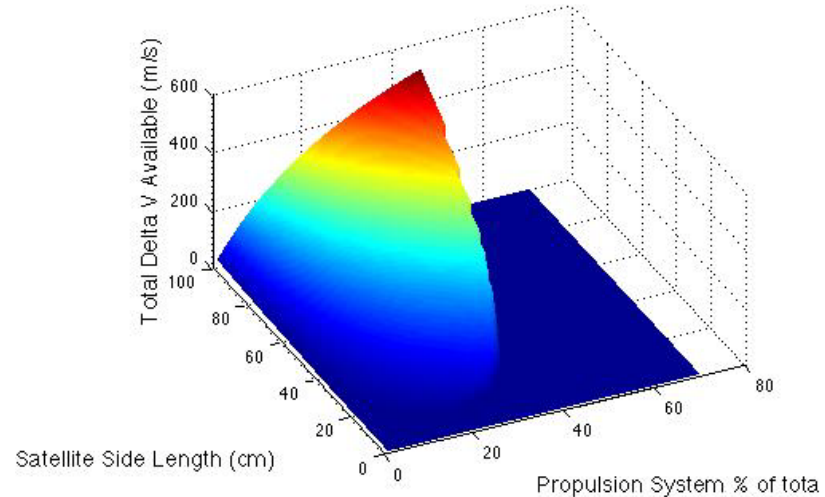
- **Monopropellant:**

- Max delta-v  $\approx$  4.6 km/s
- Max sat mass  $\approx$  450 kg!

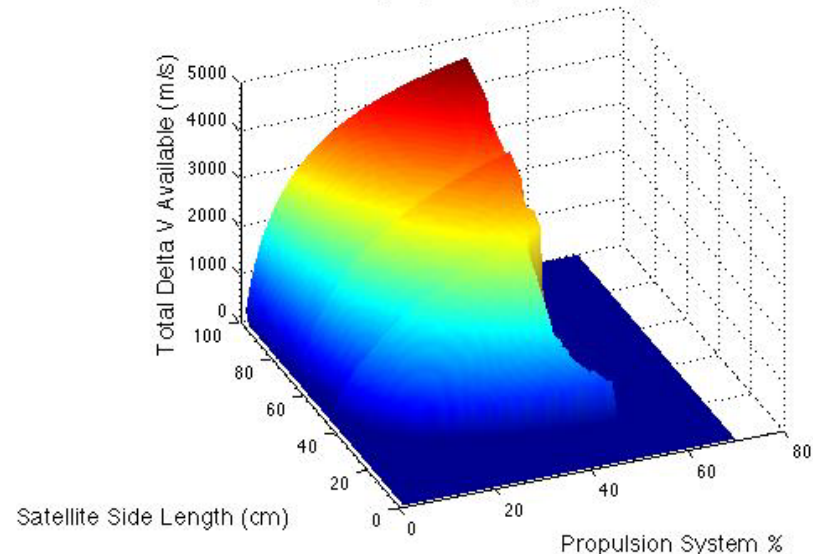
- **Cut Plots:**

- Limit propulsion system to 30% of total mass budget and 40% of total volume

Total Delta V Available vs. Size and System Volume Percent:  
Cold Gas System with Tank Pressure (psi)=  
1000



Total Delta V Available vs. Size and System Volume Percent:  
Monopropellant Hydrazine System

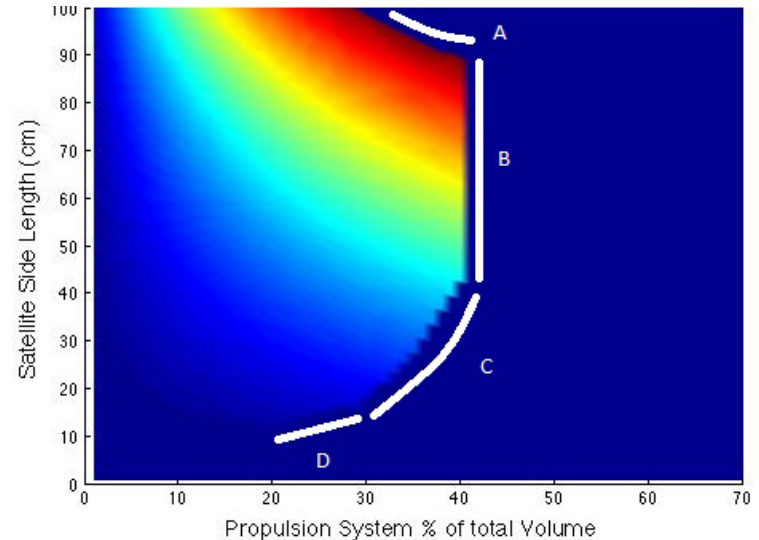


# Delta-V Results: Plots w/limits

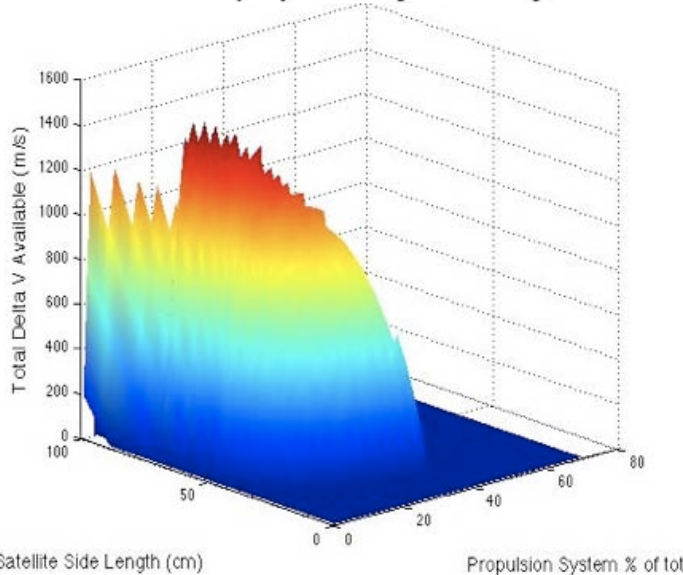


- **Example (1000 psi):**
- Max delta-v  $\approx 397$  m/s
- **Contour A & C:**
- Sat mass = 30% of mass budget
- **Line B:**
- 40% max volume cut-off
- **Contour D:**
- Represents regime where max tank rad is limited by regulator

Total Delta V Available vs. Size and System Volume Percent:  
Cold Gas System with Tank Pressure (psi) = 1000



Total Delta V Available vs. Size and System Volume Percent:  
Monopropellant Hydrazine System



## ▪ **Monopropellant Example:**

- Max delta-v  $\approx 1.5$  km/s
- Decreased delta-v in sats  $> 70$ cm due to mass restriction
- Spikes seen due to incremental increase in tank radius



## ▪ **Cold Gas:**

- Cold gas will not exceed 400 m/s for practical tank pressures
- Cold gas can be considered for entire size range
- Below 15cm Cold gas works for station-keeping only for any tank pressure (for low pressure: below 40cm)

## ▪ **Monopropellant:**

- Monopropellant will not exceed 1.5 km/s for practical satellite mass
- Monopropellant system not practical for satellites >21 cm in side length

## ▪ **Other Findings:**

- Limited capability due to large increases in tank mass with increase in tank pressure
- Reasonable method for determining Delta-V for given satellite size



## 1) ***'Reachability'***

- Connect maximum delta-v capability to reachable orbits

## 2) ***Pointing Accuracy***

- Analyze slewing capabilities of the same systems

## 3) ***Other Propulsion Systems***

- Electric and/or bipropellant systems
- Theoretical or systems in development

## 4) ***Pressure Considerations***

- Performance degradation in cold gas system
- Pressure regulation system in hydrazine system

## 5) ***Tank Shape***

- Compare spherical tanks with cylindrical or other shaped tanks

## 6) ***Satellite Shape***

- Consider non-cubic shaped satellites