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# Design Considerations for Miniaturized Control Moment Gyroscopes for Rapid Retargeting and Precision Pointing of Small Satellites

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# Motivation

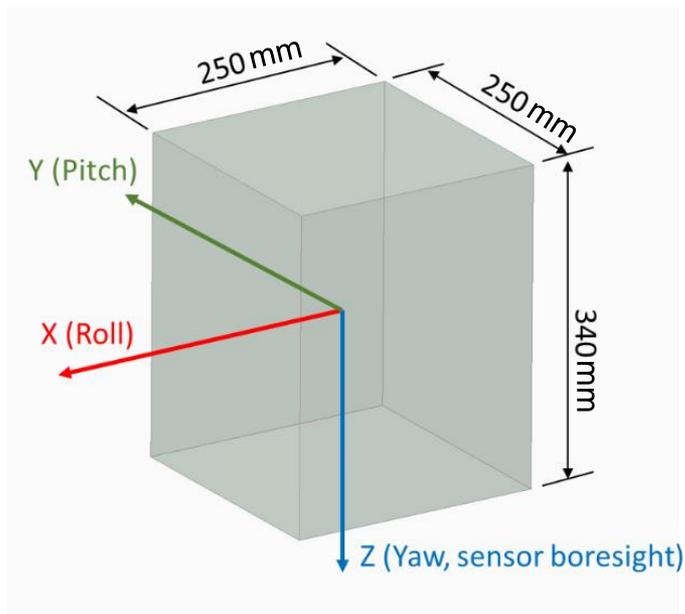
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- With miniaturization and advances in electronics, there is a significant interest in small satellites.
- There is interest in utilizing commercial off-the-shelf (COTS) components in the pico-/nano-satellite community.
- A COTS based ACS capable of rapid reorientation (i.e. high torque) and precision pointing (i.e. high torque precision) can improve mission utility of small satellites.
- An analysis of COTS hardware indicates a CMG-RW hybrid approach is suitable for small satellites.
- A CMG-RW Hybrid approach utilizes torque amplification of CMGs in the rapid retargeting mode and direct torque capability of flywheel motors in precision pointing mode.

# System details

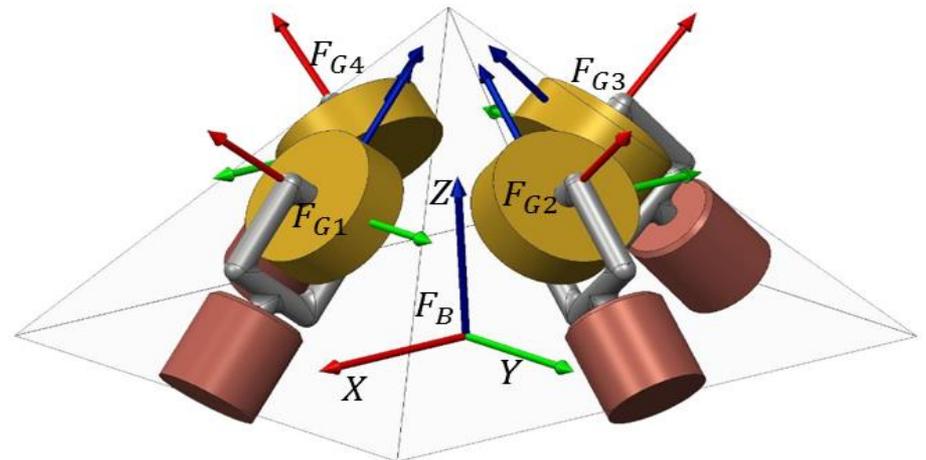
## Satellite

- 12 U size
- 20 kg mass
- 18 W average on orbit power

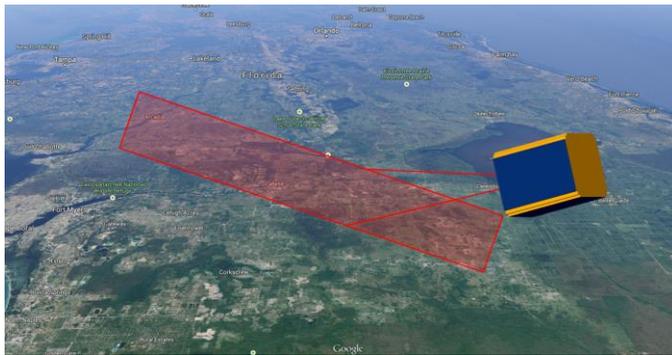


## ACS

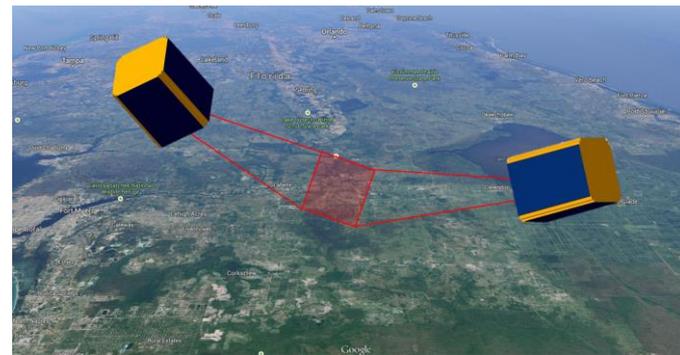
- 4 Hybrid CMGs in pyramidal configuration
- Pyramid angle = 54.74 degrees
- The CMG size, mass and power consumption is constrained by the satellite.



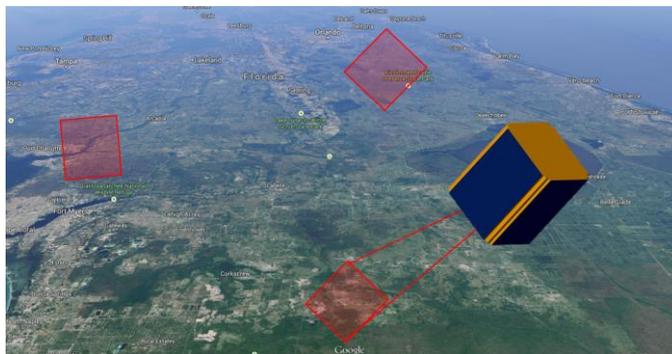
# Satellite slew and pointing requirements



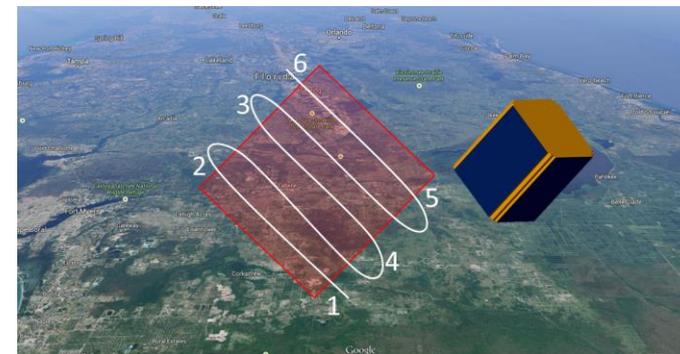
Strip imaging



Stereoscopic imaging



Spot imaging



Area imaging

Orbit altitude ( <i>alt</i> )	350 to 700 km
Slew rate	15 deg/s
Spatial resolution ( <i>w</i> )	25 to 75 m
Angular resolution ( $\psi$ )	$\psi \cong \frac{w}{alt}$ , 7 to 45 arc sec

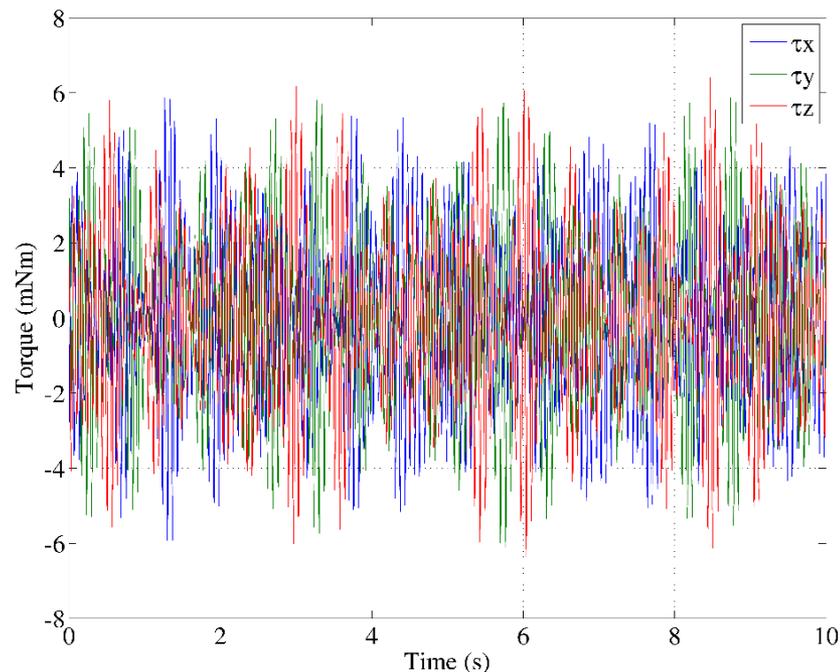
# Torque accuracy assessment

- In the CMG mode, there are three parameters; gimbals speed, flywheel orientation and flywheel speed, which affect the control torque.
- In the RW mode, there are two parameters; flywheel acceleration and flywheel orientation, which affect the control torque.
- Appropriate gimbal and flywheel motors are selected based on the mass/volume/power constraints and simulations are performed to evaluate the effect of these errors on the output torque.

Satellite inertia	$\begin{bmatrix} 0.21 & 0 & 0 \\ 0 & 0.21 & 0 \\ 0 & 0 & 0.3 \end{bmatrix}$	kg·m <sup>2</sup>
Flywheel inertia	$32 \times 10^{-6}$	kg·m <sup>2</sup>
Flywheel speed	12000	RPM

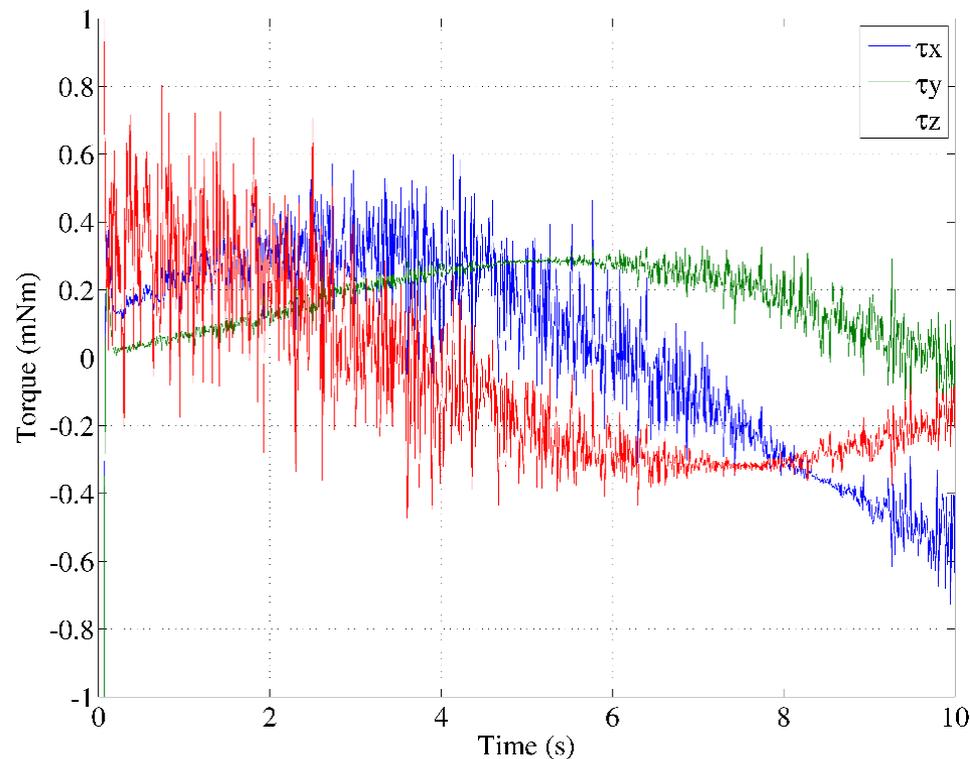
# Effect of flywheel speed variation

- The flywheel speed error is assumed to follow a normal distribution with 2-sigma limit of 12 RPM.
- This error produces highest torque disturbance compared to other error sources
- However, it occurs at flywheel speed (200 Hz) and can be filtered with appropriate damping.



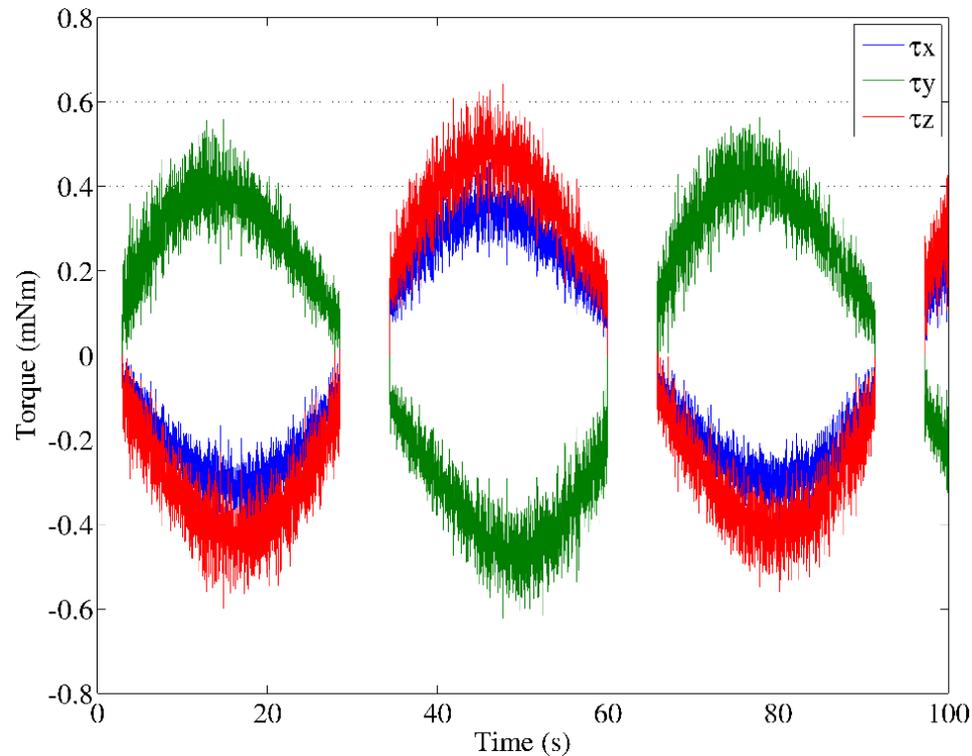
# Effect of gimbals speed/position inaccuracy

- Gimbal speed is assumed to follow a normal distribution with 2-sigma limit of 0.05 deg/s; corresponding error in gimbal position knowledge is 0.01 degrees.



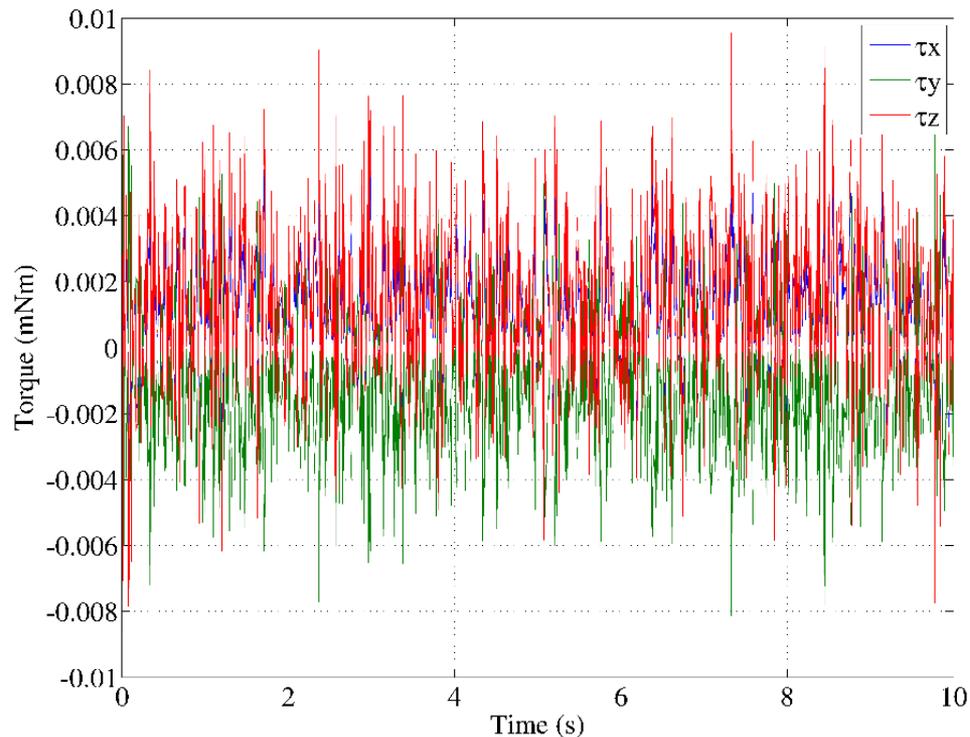
# Effect of gimbal dead zone

- Gimbal speeds slower than 0.25 deg/s are difficult to achieve with COTS components due to stiction. This makes torques smaller than 0.1 mNm unachievable



# Effect of flywheel acceleration error

- Flywheel acceleration error can be controlled within 10% of the commanded acceleration
- At small accelerations, which are expected during hybrid mode, the contribution of this error is lowest



# Hybrid-mode considerations

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- When only RW based attitude control is used, the orientations of the wheels are predetermined and fixed such that torque along any desired direction can be commanded.
- In the hybrid mode, the control strategy switches from CMG to RW mode at the end of rapid slew to provide precision tracking performance.
- There is a possibility of a singular flywheel orientation. That is, the torque produced by the flywheel motors is limited to a plane and control authority in the RW mode is lost.
- Implementation of hybrid mode requires modifications to the existing CMG control laws to avoid singular flywheel orientations.
- A RW singularity parameter is defined and it is used to steer the gimbals away from RW singularities through null motion.

# New steering law – Hybrid mode

- The steering algorithm under consideration is a combination of a GSR (Generalized Singularity Robust) steering law and null motion
- The torque is mapped to the gimbal speeds and flywheel acceleration as follows

$$\dot{\delta} = \alpha(I_w \hat{\Omega})^{-1} [A^T (AA^T + \lambda E)^{-1} \tau + \beta \mathbf{d}]$$

$$\dot{\Omega} = (1 - \alpha) I_w^{-1} B^T (BB^T)^{-1} \tau$$

- $A$  and  $B$  are projection matrices for gyroscopic and direct torques.  $\mathbf{d}$  is the null vector, and  $\alpha$  is the mode switch parameter, which is externally selected.
- $\lambda$  introduces torque error to steer the gimbals away from a CMG singularity and  $\beta$  adds null motion to steer the gimbals away from a RW singularity. They are defined as follows

$$\lambda = \lambda_0 \exp(-\mu_1 \det(AA^T)), \quad \beta = \beta_0 \exp(-\mu_2 \det(BB^T))$$

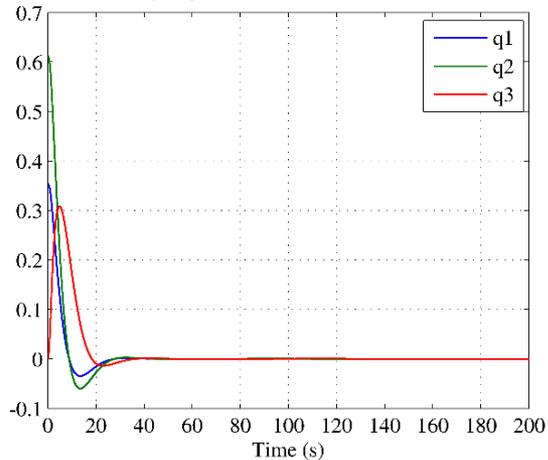
# Results

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- Simulations consist of a rest-to-rest rapid retargeting and precision pointing (R2P2) maneuver.
- The satellite is commanded to reorient by 30 degrees. The initial direction of the sensor boresight vector is  $[1,0,0]^T$  and final direction is  $[\cos(-30),\sin(-30),0]^T$ .
- Simulations incorporate flywheel acceleration errors and gimbal speed/position errors.
- Transition from CMG to RW mode occurs between 100 and 110 seconds by changing the value of  $\alpha$  from 1 to 0.
- The pointing performance of the hybrid steering law is compared with the CMG only GSR steering law.

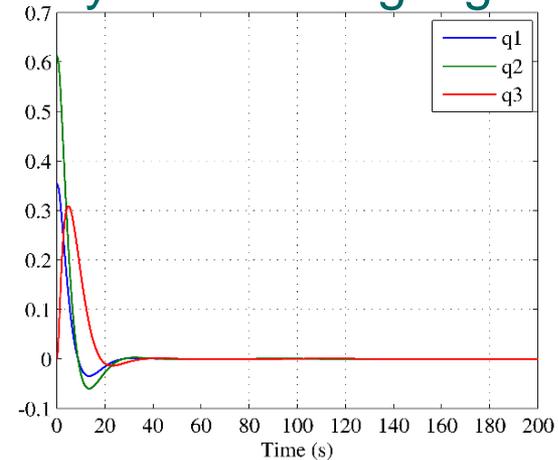
# Results

## GSR inverse

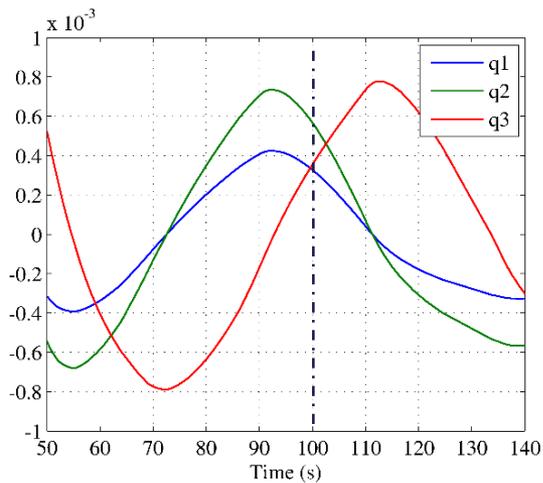


### Quaternion error

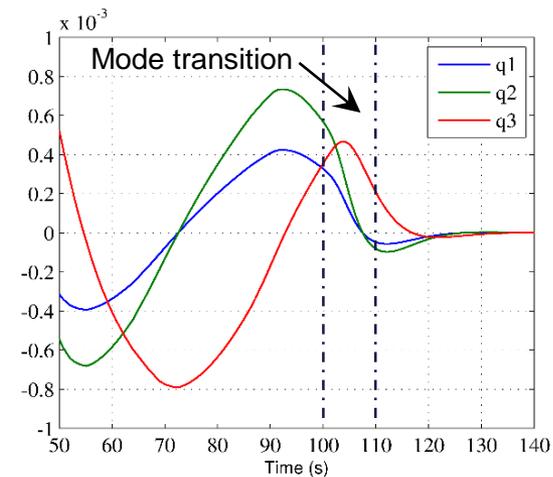
## Hybrid steering logic



### Quaternion error



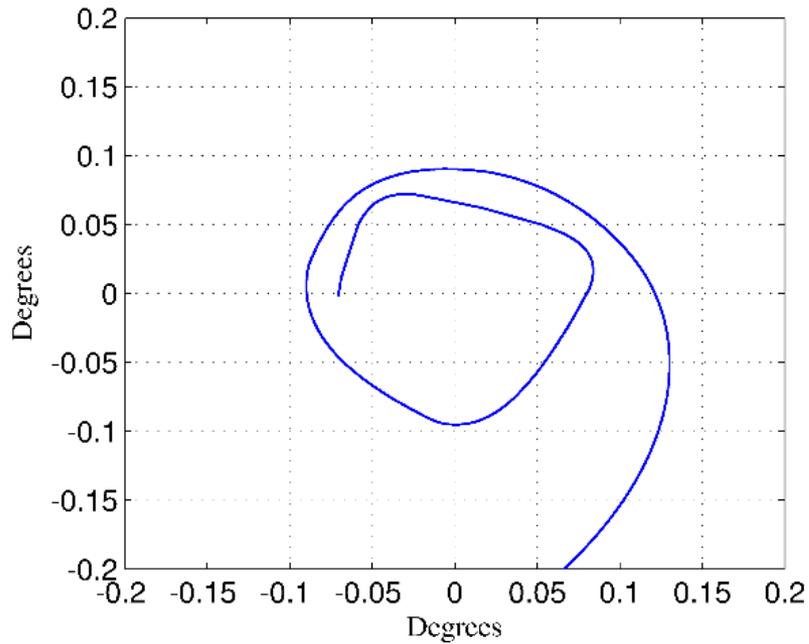
### Quaternion error – steady state region



### Quaternion error – steady state region

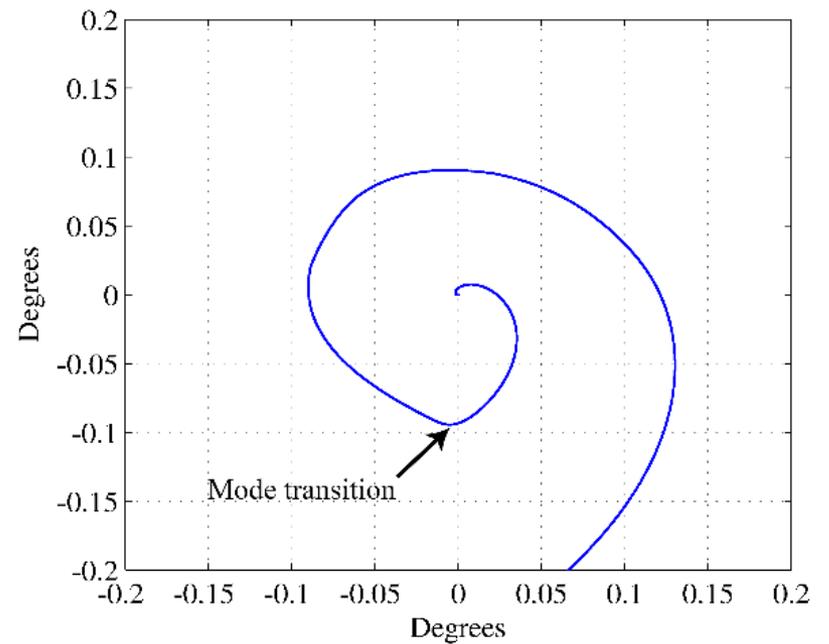
# Results

## GSR inverse



Sensor boresight vector projection

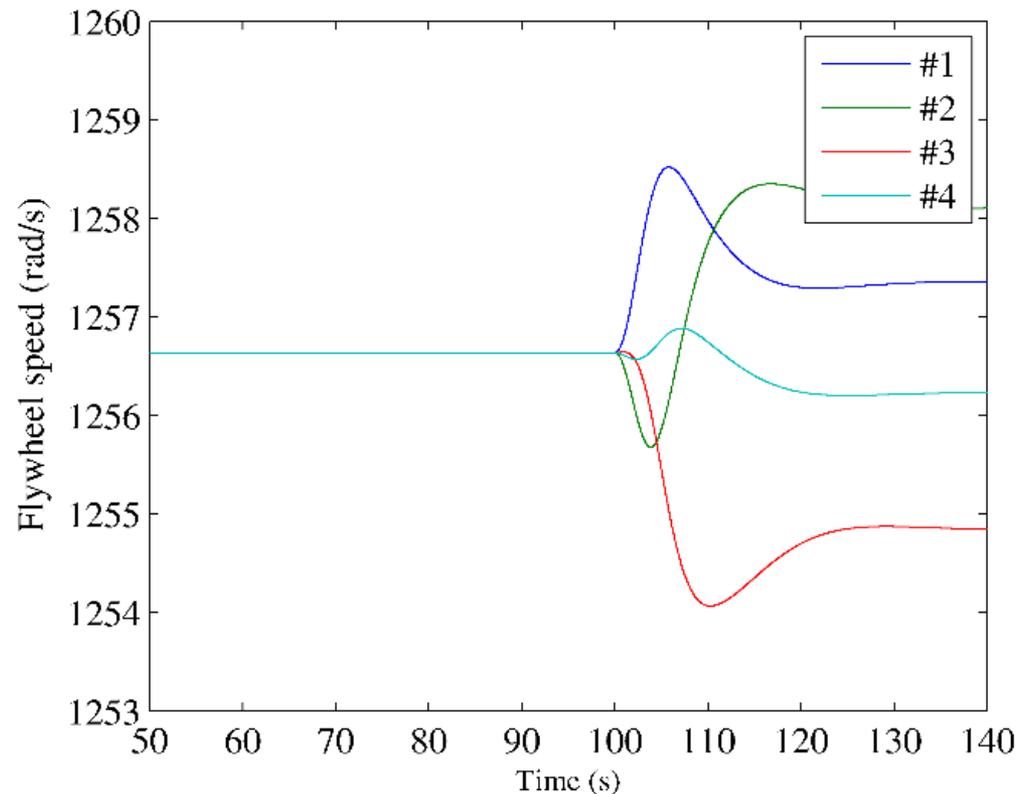
## Hybrid steering logic



Sensor boresight vector projection

# Results

- High torque motors are not required since flywheel speed variations in the RW mode are limited to a few RPMs. Thus, high torque motors are not needed.



Flywheel speed in hybrid mode

# Conclusion and Future Work

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- An ACS suitable for satellites in the 15-20 kg mass range is discussed in this paper with consideration of the size, weight, and power limitations imposed by the satellite.
- An analysis was performed to study the torque errors associated with commercially available (COTS) gimbal and flywheel motors selected to meet the satellite imposed limitations as well as the mission requirements.
- A hybrid steering logic, which uses gyroscopic torque for rapid retargeting and direct torque of flywheel motors for precision pointing, was introduced and was shown through simulations to be a practical solution for rapid retargeting and precision pointing of small satellites using COTS components.
- Future work involves prototyping and experimental testing of this system. Additionally, momentum management strategies will be developed to minimize flywheel speed drifts that may occur after multiple maneuvers.

# Acknowledgement

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Questions?

